

Marshall 1/87

Instantaneous and Time-Dependent
Response and Strength
of Jointless Bridge Beams

by
Francisco P. S. L. Gastal

A thesis submitted to the Graduate Faculty of
North Carolina State University
in partial fulfillment of the
requirements for the Degree of
Doctor of Philosophy

Department of Civil Engineering

Raleigh
1986

Approved By:

A. R. Manson

Adm. Cuyler

Co-Chairman of Advisory Committee

Wm. L. Bingham

Paul Jia

Co-Chairman of Advisory Committee

ABSTRACT

GASTAL, FRANCISCO P.S.L. - Instantaneous and time-dependent response and strength of jointless bridge beams (Under the direction of Dr. Paul Zia and Dr. Ajaya K. Gupta).

The purpose of this study was to develop a generalized numerical solution for the analysis of deck-continuous, composite, multi-span bridge girders without joints. A finite element computer program has been developed, with the capability of performing instantaneous and time-dependent response analyses, and strength analyses, for a general type of bridge beams. Steel, reinforced or prestressed concrete girders, topped by a reinforced concrete deck-slab, under various sequences of construction and with different types of continuity may be equally analyzed by the proposed solution.

An isoparametric beam element and a connection, spring-like element, have been modified for modeling the nonlinear intrinsic characteristics of the materials, as well as accounting for the presence of mild steel reinforcements, prestressing tendons and the effects of cracking. Time-dependent properties of the comprising materials are assumed to follow the simplified models suggested by the American Concrete Institute and Prestressed Concrete Institute. The effects of a superimposed temperature gradient are included also in the analysis.

A thorough description of the problem and of the properties assumed in modeling the materials is given first, followed by the development of the finite element formulation. The proposed solution is validated by

the analyses of ten different beams, with comparisons being made with available analytical and experimental data. Two different cases of deck-continuous, jointless, multi-span beams are investigated and their performances are compared to the extreme situations of non and full continuity. Their behaviors have been found to be very satisfactory under dead and service load conditions. Under vertical loading, the response of a deck-continuous beam may be comparable to the response of a non- or fully-continuous beam, depending primarily on the imposed supporting conditions.

This work is fondly dedicated to my father,
whom I shall not see again, and to my dear wife,
whose love and support have made it all possible.

ACKNOWLEDGEMENTS

The author would like to express his sincere gratitude to Dr. Paul Zia and Dr. Ajaya K. Gupta, who served as co-chairmen of the author's Graduate Advisory Committee, for their most knowledgeable support, constructive criticism and continuous guidance throughout this entire study. It has been a most rewarding experience to work with Dr. Zia and Dr. Gupta in developing and reporting this research.

Special appreciation is also expressed to Dr. William L. Bingham and Dr. Allison R. Manson for their assistance while serving in the Committee.

The financial support provided by the Conselho Nacional de Desenvolvimento Científico e Tecnológico - CNPq and Universidade Federal do Rio Grande do Sul is sincerely appreciated. The cooperation and patience expressed by the Civil Engineering Department of that University is also gratefully acknowledged.

F.Gastal

North Carolina State University

December, 1986

TABLE OF CONTENTS

1. INTRODUCTION

1.1	Background.....	1
1.2	Objective.....	2
1.3	Scope.....	3
1.4	Review of Available Analytical Procedures.....	4
1.5	Outline of Remaining Chapters.....	11

2. MATERIAL PROPERTIES

2.1	Concrete.....	13
2.1.1	Constitutive Relationship for Loading and Unloading.....	13
2.1.1.1	Compressive Behavior.....	13
2.1.1.2	Tensile Behavior.....	25
2.1.1.3	Cyclic Loading.....	27
2.1.2	Types of Strain.....	28
2.1.3	Time-dependent Properties.....	30
2.1.3.1	Creep Under Constant Stress.....	30
2.1.3.2	Creep Under Variable Stress.....	34
2.1.3.2.1	The Effective Modulus Method.....	35
2.1.3.2.2	The Rate of Creep Method.....	36
2.1.3.2.3	The Superposition Method.....	37
2.1.3.3	Shrinkage.....	38
2.1.3.4	Aging.....	41
2.2	Reinforcing Steel.....	44
2.2.1	Constitutive Relationship for Loading and Unloading.....	44
2.3	Prestressing Steel.....	45
2.3.1	Constitutive Relationship for Loading and Unloading.....	45
2.3.2	Relaxation Under Constant Strain.....	47
2.3.3	Relaxation Under Variable Strain.....	48
2.4	Elastomeric Bearing Pads.....	49

3. METHOD OF ANALYSIS

3.1	Introduction.....	53
3.2	Beam Element.....	54
3.2.1	Conventional Beam Element.....	54
3.2.2	Isoparametric Beam Element.....	64
3.2.3	Initial Strains.....	69
3.2.4	Prestressing Effect.....	70
3.2.5	Temperature Effect.....	77
3.2.6	Layered Section.....	78
3.2.7	Coordinate Transformation.....	80
3.2.8	Bearing Supports.....	82
3.2.9	Element Equilibrium Equation.....	82
3.3	Connection Element.....	83
3.4	Global Problem.....	87
3.5	Loading.....	88

3.6	Support Displacements.....	90
3.7	Cracking Model.....	93
3.8	Nonlinear Analysis.....	99
3.8.1	The Load Increment Method.....	99
3.8.2	The Displacement Increment Method.....	102
3.9	Time-Dependent Response Analysis.....	105
3.10	Composite Beam Action.....	108
3.11	Program Flow Diagram.....	109
4.	VALIDATION OF THE ANALYTICAL MODEL	
4.1	Introduction.....	113
4.2	Instantaneous Response and Strength of Non-Composite Beams.....	113
4.2.1	Steel I-Beam.....	113
4.2.2	Reinforced Concrete Rectangular Beam.....	114
4.2.3	Prestressed Concrete I-Beam.....	116
4.3	Instantaneous Response and Strength of Composite Beams.....	121
4.3.1	Prestressed Concrete Double Tee Beam.....	121
4.3.2	Two-span Prestressed Concrete I-Beam.....	125
4.4	Time-Dependent Response of Non-Composite Beams.....	126
4.4.1	Reinforced Concrete Rectangular Beam.....	126
4.4.2	Two-Span Reinforced Concrete Rectangular Beam.....	131
4.4.3	Prestressed Concrete Rectangular Beams.....	131
4.5	Time-Dependent Response of Composite Beams.....	136
4.5.1	Reinforced Concrete Rectangular Beams.....	136
4.5.2	Prestressed Concrete Rectangular Beams.....	139
5.	APPLICATION OF THE ANALYTICAL MODEL TO JOINTLESS BRIDGE BEAMS	
5.1	Introduction.....	146
5.2	Analysis of a Jointless-Deck on Two-Span Beam With Steel Girders.....	147
5.2.1	General Behavior.....	147
5.2.2	Deck Continuity Over Hinged Supports.....	156
5.3	Analysis of a Jointless-Deck on Four-Span Beam With Precast Prestressed Concrete Girders.....	169
5.3.1	Properties.....	169
5.3.2	Modeling.....	173
5.3.3	Results.....	173
6.	SUMMARY, CONCLUSIONS AND RECOMMENDATIONS	
6.1	Summary.....	192
6.2	Conclusions.....	194
6.2.1	Model.....	194
6.2.2	Deck-Continuous Beams.....	195
6.3	Recommendations for Further Research.....	197
7.	LIST OF REFERENCES.....	199

8. APPENDICES

8.1	Input and Output Guide (A).....	206
8.2	Listing of the Program (B).....	219
8.3	Sample Input (C).....	256
8.4	Sample Output (D).....	257

1. INTRODUCTION

1.1 Background

The use of jointless construction (1,2) for composite bridge beams is being recognized as a possible solution for the persistent bridge maintenance problems due to the existence of expansion joints (3,4). Such joints, until not long ago taken as an indispensable design requirement for the proper behavior of bridge beams, have always been a cause for deterioration of such members (5). It is virtually impossible to prevent water and debris from entering these man-made openings, damaging and eventually even completely destroying some vital parts of a bridge (5), such as prestressing cable anchorage systems, beams and bearings.

Maintaining a jointed bridge is often so costly (6,7) that some bridge engineers (2) committed themselves into the daring task of eliminating joints of any sort, in constructing continuous composite bridges. Some short-span structures were initially built with no expansion joints at the intermediate supports, some with even no joints at all, having the beams monolithically attached to the end abutments.

In spite of the skepticism of many, the idea has been successful and those audacious designers envisioned even longer and longer structures. Nearly one thousand feet of joint-free beams have been constructed (2), and no problems due to the absence of joints have been encountered.

Continuous concrete bridges have been built traditionally by using cast-in-place construction (8), molding fully continuous members.

Continuous steel girders were also used with a concrete deck slab eventually cast on top of them. The use of precast concrete construction (8), proven efficient and economical in many cases, brought on the need for a new solution and many concrete bridges were made continuous for live load (9). By inserting massive concrete diaphragms over the piers, the initially simply supported girders become a continuous structure resisting the action of live load. This widely used procedure, however, is not very adequate for steel girders. Thus they have been constructed either as fully or non-continuous structures (10,11).

1.2 Objective

The idea of eliminating structural joints, presents yet another interesting possibility. Continuity could be obtained not by casting expensive fully-continuous beams, nor by casting concrete diaphragms connecting precast girders, but by simply casting a fully-continuous deck over the simply supported girders (2). Such an unconventional constructional procedure, illustrated in Figs. 3.12, 5.2 and 5.17, and referred herein as "Deck-Continuous Beams", may prove to be an economical solution not only for the construction of new bridges but also for the rehabilitation of old ones (6).

The study of the jointless bridge, by virtue of its complexity, requires the analysis of a wide range of variables. However, the study of a single group of jointless continuous composite bridge beams is undoubtedly a first step towards a better understanding of their behavior.

Simple and fully-continuous beams, composite or not, under linear and uncracked conditions, can be analyzed satisfactorily by standard methods of theory of structures. Under non-linear and cracked conditions, however, numerical solutions are generally necessary. When only partial continuity is obtained, as is the case of deck-continuous beams, conventional analytical methods are no longer applicable, even for the most simple situations.

With the concept of ultimate strength design, attention is focused on the determination of actual safety factors along with the proper behavior of bridges not only under service loads but also under overload conditions. Desirable behavior includes the control of cracking, deflections, camber, movements, stresses and so on, which can be obtained only from a thorough analysis including the appropriate non-linear, time-dependent material properties for all stages of loading. The objective of this study is to develop a finite element analysis capable of monitoring all of the above, so as to investigate the behavior of deck-continuous beams.

1.3 Scope

Many numerical procedures using the finite element method can be found in the literature. They are capable of analyzing simple span as well as fully-continuous structures, some proposed for steel structures, others for reinforced or prestressed concrete structures, and even some with more general applicability. The analysis of deck-continuous beams, however, requires some special treatments not found in any of the existing numerical solutions. It also needs the capability of analyzing

different types of continuities, materials and loading effects.

For such a purpose, a finite element numerical solution for the analysis of jointless beams is proposed in the present study. The beams may also be composite, continuous or not, in steel, reinforced or prestressed concrete. Girders may be pre- or post-tensioned, fully or partially prestressed, with bonded tendons. Various constructional sequences may be studied, supporting conditions may be varied, and different loading arrangements assumed. Instantaneous and time-dependent responses are obtained. Time-dependent material properties may be varied, and temperature effects can be included.

1.4 Review of Available Analytical Procedures

This section presents a brief review of the available analytical and numerical procedures which have been proposed for the analysis of reinforced and prestressed concrete beams. Some are merely methods for estimating losses of prestress, others intended for obtaining elastic deformations and also inelastic and time-dependent deflections. A few analytical and numerical techniques, based on the finite and discrete element methods, suitable for the analysis of continuous bridge beams are also mentioned. No chronological order is followed and descriptions are brief. More detailed information can be found in the original works.

1.4.1 GROUNDI

Groundi (12) developed a set of expressions to predict the prestress loss of noncomposite prestressed concrete beams, taking into account

creep and shrinkage of concrete and relaxation of prestressing steel. The effects of ordinary reinforcements were neglected in the procedure.

1.4.2 HUANG

Huang (13) proposed a direct method for estimating prestress losses in pre-tensioned noncomposite members, avoiding a step-by-step method. Several expressions were introduced to account for the effects of creep and shrinkage of concrete and relaxation of prestressing steel.

1.4.3 TADROS

Tadros, et al (14) suggested a procedure for predicting prestress losses, taking into consideration the effects of continuous reduction of prestressing stress due to creep and shrinkage of concrete and relaxation of steel, by a recovery parameter and a relaxation reduction factor.

1.4.4 ZIA

Zia, et al (15) presented equations for estimating prestress losses due to elastic shortening, creep and shrinkage of concrete and relaxation of prestressing steel for both pre- and post-tensioned members with either bonded or unbonded tendons. The equations were applicable to normal design conditions and estimated the various types of prestress loss, rather than a lump sum value.

1.4.5 GHALI and TREVINO

Ghali and Trevino (16), studying the relaxation effect in prestressing steel, proposed a relaxation reduction coefficient to be

employed as a multiplier to the intrinsic relaxation for use in prestressed concrete design. A numerical example was presented showing that the prestress loss due to relaxation in prestressed concrete members is of smaller magnitude than the intrinsic relaxation presented by a free tendon.

1.4.6 TADROS, GHALI and MAYERS

Tadros, Ghali and Mayers (17) proposed a single procedure for the prediction of time-dependent deflections in pre-tensioned precast concrete members. The method accounts for the effects of creep, shrinkage of concrete and relaxation of the prestressing steel, allowing for the presence of non-prestressing steel and considering the tension stiffening effect of concrete. Deflections are obtained by numerical integration of the curvatures. The procedure has been suggested for modification of the method used by the PCI Design Handbook (18).

1.4.7 BRANSON

Based on his previous works, Branson (19) advanced a modified step function method for calculating prestress losses, cambers, and deflections of non-composite and composite prestressed beams. Formulas were given to estimate prestress losses and camber or deflections for different types of structures. The formulas were the summation of the contribution of each factor that affects prestress losses, and cambers or deflections.

The method of analysis, for both instantaneous and time-dependent analyses, is also presented in detail in the book by Branson (20). It includes the effects of aging, creep, shrinkage of concrete and

relaxation of prestressing steel. The effects of non-prestressing steel, cracking of the sections and continuity of the structure are also taken into account. The method is developed for hand calculations, but it is also suitable for computer analysis.

1.4.8 RAO and DILGER

A method of analysis called "The Varying Stiffness Method" was proposed by Rao and Dilger (21) to predict time-dependent responses of simply supported pre-tensioned members, both noncomposite and composite. The method takes into account aging, creep and shrinkage of concrete and relaxation of prestressing steel. In estimating creep strains, the method uses a modified version of the superposition principle. It is also assumed that creep is proportional to stress. Stress-strain relationships of concrete and prestressing steel are assumed linear in the range of stress level of interest.

1.4.9 NAAMAN

Naaman (22) proposed a simplified method for the prediction of time-dependent deflections of prestressed concrete beams, called "The Pressure Line Method". The method considers the beams subjected to a compressive force following the profile of the pressure line instead of that of the tendons. A lump sum estimate of the total time-dependent prestress loss, and its percentage value with time, are assumed a priori, and a single sustained loading comprising the combined effects of sustained external moments and prestressing moments is considered.

1.4.10 PCI

The PCI Committee on Prestress Losses ⁽²³⁾ also recommended a step-by-step method of estimating prestress losses in both pre-tensioned and post-tensioned concrete members. Total prestress losses could also be computed using a simplified method where several equations were given for different types of materials and methods of tensioning.

For composite sections, the effects of differential shrinkage and differential creep between deck slab and precast beams are difficult to obtain. The change of stiffnesses of indeterminate structures due to time-dependent properties of materials may change the bending moments caused by external loads in any section. These effects, however, are not considered in most of the above mentioned prestress loss methods.

Adapting the step-by-step method, the time dependent response problem of prestressed members is reduced to a series of instantaneous, age-corrected, response problems. The instantaneous load responses of a general prestress beam can be best estimated numerically through the use of a digital computer.

1.4.11 SINNO and FURR

Sinno and Furr ⁽²⁴⁾ developed a computer program to predict the time-dependent responses of noncomposite and composite simply supported pre-tensioned beams. The step-by-step procedure together with the rate of creep method were used in estimating prestress losses and camber of the members. The separations method for predicting responses of composite sections, as proposed by Branson ⁽²⁵⁾, was used in estimating the effects of the differential shrinkage and creep. The method assumed

linear stress-strain relationships for both concrete and steel, it did not take into account the effects of concrete aging nor the effects of external loading.

1.4.12 MOSSOSIAN and GAMBLE

Mossosian and Gamble (26) developed a computer program based on a step-by-step procedure which iteratively estimates the time-dependent behaviors of both noncomposite and composite prestressed concrete members. The superposition method and the rate of creep method, taking into account the effect of concrete aging, were used in estimating the creep strains. In developing the computer program, linear stress-strain relationships for both concrete and steel were assumed. The aging effects, creep and shrinkage of concrete were considered, but relaxation of prestressing steel was neglected. The program was later revised and updated by Fadl and Gamble (27), to predict the time-dependent behaviors of noncomposite and composite pre-tensioned girder bridges.

Various versions of the direct stiffness method of structural analysis, in which structural elements are modeled as finite elements or discrete elements, are used widely to solve nonlinear structural problems by an iterative approach. Many finite element computer programs have been written for the analysis of reinforced concrete beams and frames (28,29,30,31,32), although many of them are not suitable for the analysis of precast composite members nor for the analysis of time-dependent behaviors. An extensive list of references may be found in the report by the American Society of Civil Engineers (33).

1.4.13 ATKINS, PIERCE, CHANG, LO and WANG

The discrete element method for the analysis of elastic and inelastic prestressed concrete members was used by Atkins (34), of elastic or inelastic prestressed concrete members with unbonded tendons by Pierce (35), and of composite prestressed concrete members by Chang (36), Lo (37) and Wang (38). These analyses, however, were based on linear stress-strain relationships for both concrete and prestressing steel, and were proposed for obtaining instantaneous responses only.

1.4.14 FREYERMUTH

Based on the work by Mattock and Kaar (39), Freyermuth (9) developed a simplified procedure to account for the effects of differential creep and differential shrinkage in the analysis and design of precast, composite, prestressed concrete girders, made continuous for live load only. In this type of construction, positive moments may develop over the piers due to creep in the prestressed girders, as well as due to loads in the remote spans. This may be partially counteracted by negative moments resulting from differential shrinkage between the cast-in-place deck slab and the precast girders.

Freyermuth's procedure assumes that the effects of creep under prestress and dead load can be evaluated by an elastic analysis assuming that the girders and slab are cast and prestressed as a monolithic continuous beam. The conjugate beam theory is used to calculate the various fixed end restraint moments, due to shrinkage, prestressing and dead loads, and the final restraining moments are then obtained by moment distribution. The moments so obtained are, then, multiplied by

creep factors to allow for the effects of creep. Those creep factors are evaluated in terms of intrinsic creep potential of the concrete materials, volume to surface ratio of the member, and ages of casting and prestressing. It is worth noting that this procedure, if correct, is only applicable to members under service loads with linear and uncracked conditions. Furthermore, as any other elastic analysis, it is not suitable for the case of deck-continuous beams being considered herein.

1.4.15 QIU, CHUNFU and JINHUAN

Qiu, Chunfu and Jinhuan ⁽⁴⁰⁾ have very recently reported a new version of a computer program for the analysis and design of long span prestressed concrete bridges, the SABRIJ-B83. The program, which also uses the "CAD" techniques, is suitable for both static linear and nonlinear analyses of any structural system of bridges which could be considered as plane frames, e.g. continuous-beams, -arches, -trusses, T-frames, cable-stayed and enclosed frames. It also accounts for the effects of various loading conditions, temperature, shrinkage, creep, prestress losses and support settlements. Although showing remarkable versatility, the program SABRIJ-B83, as by its description, may not be suitable for the problem in question, i.e. deck-continuous beams.

1.5 Outline of Remaining Chapters

In the next chapter the mechanical properties of the materials used in this study are described. Methods used in estimating instantaneous uniaxial load responses of concrete, reinforcing steel and prestressing

steel, and time-dependent responses, i.e. aging, creep under constant and variable stresses, and shrinkage of concrete and relaxation of steel, are presented.

Chapter III reviews the fundamental concepts which are used as the basis for the development of the proposed solution. The formulation of two finite elements used are thoroughly described, as well as the methods adopted for the analysis of loading, prestressing, support displacements, temperature and time-dependent effects.

Various example problems illustrating the capability and the validity of the proposed numerical solution are presented in Chapter IV. The instantaneous and time-dependent responses, and strength, of several different beams are analyzed and compared to experimental data reported in the literature.

Chapter V illustrates the applicability of the proposed solution to the study of deck-continuous beams. Two distinct example problems are investigated and particular conclusions are drawn. A summary of the study, final conclusions and some suggestions for further research are found in Chapter VI. Appendices A, B, C and D show input and output details, a complete listing of the developed program and a sample input and output, respectively.

2. MATERIAL PROPERTIES

A composite bridge beam is generally composed of concrete, mild steel, for the girders or for reinforcement, and prestressing steel. In order to accurately predict the behavior of the beam under any loading condition, constitutive relations, i.e. stress-strain-time relationships for the materials that comprise the beam, must be available. In the following sections the expressions representing the uniaxial constitutive laws of concrete, prestressing steel, and reinforcing steel will be briefly reviewed. The presentation will be helpful in determining the material properties for estimating the responses of the structures when only limited experimental data are available.

2.1 Concrete

2.1.1 Constitutive Relationship for Loading and Unloading

2.1.1.1 Compressive Behavior

The instantaneous compressive stress-strain relationship of concrete depends on so many factors that it is not feasible to establish the relationship for a particular concrete from its constituents, curing conditions, and ambient conditions. The common method for determining the relationship is to perform a series of compression tests on cylinders taken from the same mix and stored in the same ambient conditions as the structure. But a complete stress-strain curve of concrete in compression is not easily obtained (41,42,43) . Concrete cylinders under uniaxial compression fail suddenly when loaded beyond their ultimate strength. A specially designed equipment is needed to obtain the descending branch of the stress-strain curve, i.e. the portion

of the stress-strain curve exceeding the strain corresponding to the ultimate strength.

Many empirical expressions representing the complete concrete stress-strain curves have been proposed by several investigators (44,45,46,47) , some will be listed herein, but more extensive references can be found in the reports by Popovics (48) and Sargin (49). Note that the expressions will be changed such that they are consistent with the sign convention used in this thesis, i.e. compressive stress and strain are negative and tensile stress and strain are positive.

Hognestad (44,50) , after extensive tests of concrete columns subjected to combined bending and axial load, proposed a stress-strain relationship composed of a parabolic ascending branch and a straight descending branch, shown in Fig. 2.1.

For $0 \geq \epsilon \geq \epsilon_0$

$$f_c = f_c'' [2 \epsilon/\epsilon_0 - (\epsilon/\epsilon_0)^2]$$

$$E_{ci} = 1\,800\,000 + 460 |f_c'|$$

$$E_c = 2 |f_c''| (1 - \epsilon/\epsilon_0) (1/\epsilon_0)$$

For $\epsilon_0 > \epsilon \geq \epsilon_u$

$$f_c = f_c'' (\epsilon_u - 0.85 \epsilon_0 - 0.15 \epsilon) / (\epsilon_u - \epsilon_0)$$

$$E_c = 0.15 f_c'' / (\epsilon_u - \epsilon_0)$$

Where

ϵ = Concrete compressive strain

f_c = Concrete compressive stress at strain ϵ

f_c'' = Maximum compressive stress = $0.85 f_c''$

f'_c = Concrete cylinder strength

ϵ_0 = Concrete strain at maximum stress f'_c
 $= 2 f'_c / E_{ci}$ in/in

E_{ci} = Initial modulus of elasticity

E_c = Modulus of elasticity at stress f'_c

ϵ_u = Ultimate compressive strain
 $= -0.0038$ in/in

Kent and Park (45,51) , proposed a stress-strain relationship for unconfined or confined concrete, which assumes that the ascending part of the curve is represented by a second degree parabola and that the confining steel has no effect on its shape, nor on the strain at maximum stress. It is also assumed that the maximum stress reached by the concrete is the cylinder strength f'_c . The descending branch of the proposed curve is modeled by straight lines with different slopes for confined and unconfined concretes, as shown in Fig. 2.2 .

The relationship can be represented by the following expressions:

For $0 \leq \epsilon \leq \epsilon_0$

$$f_c = f'_c [2 \epsilon / \epsilon_0 - (\epsilon / \epsilon_0)^2]$$

For $\epsilon_0 < \epsilon \leq \epsilon_{20c}$

$$f_c = f'_c [1 - Z (\epsilon - \epsilon_0)]$$

$$Z = 0.5 / (\epsilon_{50u} - \epsilon_0) , \quad \text{unconfined}$$

$$Z = 0.5 / (\epsilon_{50c} - \epsilon_0) , \quad \text{confined}$$

For $\epsilon_{20c} < \epsilon$

$$f_c = 0.2 f'_c$$

Where

Z = Slope of the descending branch of the stress-strain relationship.

ϵ_{50u} = Strain at $0.5 f'_c$ on the descending branch for unconfined concrete.

ϵ_{50c} = Strain at $0.5 f'_c$ on the descending branch for confined concrete.

The strain ϵ_0 was assumed to be equal to -0.002 in/in, ϵ_{50u} and ϵ_{50c} were found from the analysis of test results from various investigators, e.g. Soliman and Yu (52), Roy and Sozen (53), Bertero and Felippa (54), to be as follows:

$$\epsilon_{50u} = - (3 + 0.002 |f'_c|) / (|f'_c| - 1000) \quad \text{in/in}$$

$$\epsilon_{50c} = \epsilon_{50u} - 0.75\rho (b/s)^{1/2} \quad \text{in/in}$$

Where

ρ = Volumetric ratio of lateral reinforcement to bound concrete

$$= 2 (b + d) A_s / (b d s)$$

b = Width of confined core

d = Depth of confined core

A_s = Cross section of one leg of lateral reinforcement

s = Longitudinal spacing of lateral reinforcement

Lee (46), in his study of inelastic behavior of reinforced concrete members, assumed that both ascending and descending branches of the curve could be represented by a single parabolic curve as:

$$f_c = f_c'' [2 \epsilon/\epsilon_0 - (\epsilon/\epsilon_0)^2] , 0 < \epsilon/\epsilon_0 < 2$$

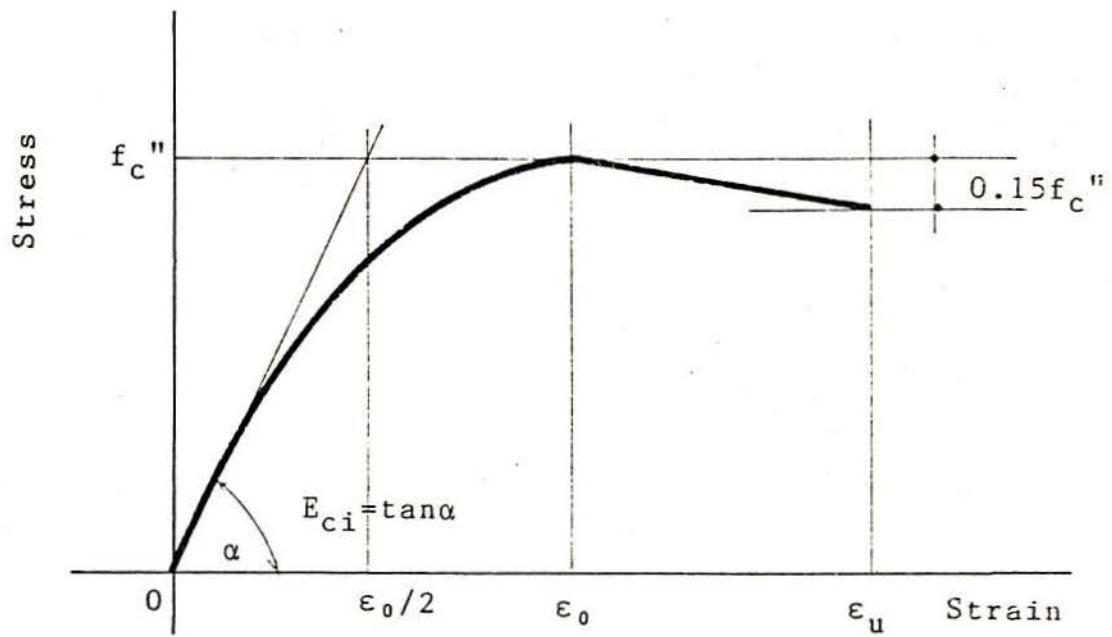


Fig 2.1 - Hognestad's stress-strain curve for concrete in compression.

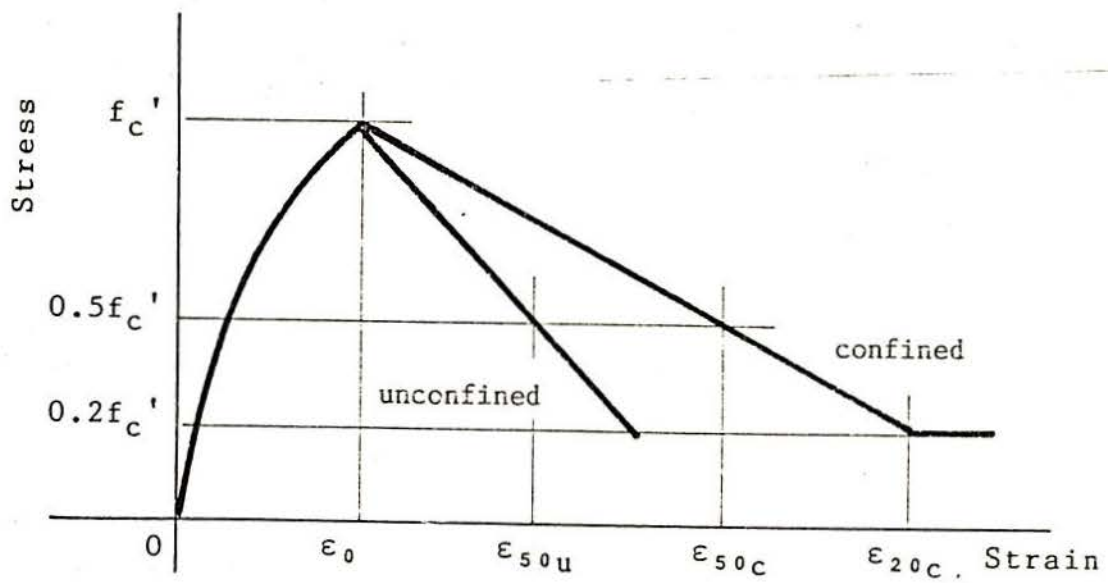


Fig 2.2 - Kent and Park stress-strain relationship for confined and unconfined concrete in compression.

Kriz and Lee (1960), represented the relationship by a quadratic equation as:

$$f_c^2 + a \epsilon^2 + b f_c \epsilon + c f_c + d \epsilon = 0$$

Where the constants a, b, c, and d were empirical and estimated from uniaxial compression test data by solving four simultaneous equations. Those equations were obtained from substituting the values of the stresses correspondent to four specified strain points.

The CEB (55), recommended an expression representing the compressive stress-strain relationship of normal weight concrete as:

$$f_c / f'_c = (kx - x^2) / [1 + (k - 2)x]$$

$$k = E_{ci} \epsilon_0 / f'_c$$

Where

$$x = \epsilon / \epsilon_0$$

$$\epsilon_0 = \text{Strain at maximum stress } f'_c$$

$$E_{ci} = \text{Initial modulus of elasticity}$$

$$= 10450 (|f'_c| + 8)^{1/2}, \text{ MPa}$$

The values of ϵ_0 are found to range from -0.002 to -0.0025 in/in. The value of ϵ_0 of -0.0022 in/in is recommended for the stress-strain curve. The values of the ultimate strain ϵ_u are found to range from -0.0035 to -0.007 in/in, and the values of the stress at ultimate strain to range from $0.75 f'_c$ to $0.25 f'_c$.

The ACI (56) recommends the analysis of uncracked sections, under service loads, by the linear elastic theory assuming a constant relationship between strains and stresses as:

$$\begin{aligned} E_c &= f_c / \epsilon_c \\ &= W^{3/2} .33 (|f'_c|)^{1/2} \end{aligned}$$

Where

f'_c = Concrete cylinder strength in psi

W = Concrete weight, ranging from 90 to 155 lb/cu.ft

For normal weight concrete the modulus of elasticity E_c may be approximated by:

$$E_c = 57000 (|f'_c|)^{1/2}$$

For structural members, under the combined action of bending and axial load, it suggested the use of a rectangular stress block, within the compression zone, for the calculation of their ultimate capacity. This stress block extends, with constant compressive stress f_c'' , from the extreme fiber to a depth "a" into the compression zone, such that

$$f_c'' = 0.85 f'_c$$

$$a = \alpha c$$

$$\alpha = 0.85$$

$$, f'_c \leq 4000 \text{ psi}$$

$$= 0.85 - (0.05/1000) (f'_c - 4000) \geq 0.65 , f'_c \geq 4000 \text{ psi}$$

Where

f'_c = Concrete cylinder strength

f_c'' = Maximum compressive strength

c = Depth of the compression zone

a = Depth of the rectangular stress block

α = Ratio a/c

The resultant force from this rectangular stress block is assumed to coincide with the resultant force from the actual concrete stress distribution in the compression zone.

From the existing experimental data and the stress-strain relationships proposed by various investigators, some of them previously mentioned, the following characteristics of the stress-strain relationship for a normal weight concrete specimen in compression are observed:

a) Compressive stress increases as compressive strain increases, at a decreasing rate, up to the maximum compressive stress, f_c'' , of the concrete, where the slope of the stress-strain curve is equal to zero.

b) The maximum compressive stress, f_c'' , is taken as a fraction of the maximum compressive strength of the specimen f_c' , ranging from 0.85 f_c' to f_c' .

c) Most investigators gave the strain at the maximum compressive stress ϵ_0 independent of the strength and the modulus of elasticity of concrete. ϵ_0 ranges from -0.002 to -0.0025 in/in.

d) For compressive strains greater than ϵ_0 , compressive stresses decrease as compressive strains increase. The descending branch of the stress-strain curve can be adequately represented by a straight line

until the stress drops to a certain level. Concrete can sustain that stress level at relatively large strains, property referred to as ductility. The slope of the descending branch depends on the strength of the concrete and the degree of lateral confinement.

Several expressions have been proposed to estimate the modulus of elasticity for concrete, E_c . Sargin (45) listed the following expressions:

GRAF	$E_c = 4.92 f'_c \cdot 10^6 / (1970 + f'_c)$
ROS	$E_c = 7.82 f'_c \cdot 10^6 / (2133 + f'_c)$
JENSEN	$E_c = 8.00 f'_c \cdot 10^6 / (2000 + f'_c)$
HOGNESTAD	$E_c = 1\,800\,000 + 460 f'_c $
WALKER	$E_c = 66\,000 (f'_c)^{\frac{1}{2}}$
PAUW	$E_c = 33 W^{3/2} (f'_c)^{\frac{1}{2}}$
SAENZ	$E_c = (f'_c)^{\frac{1}{2}} \cdot 10^5 / [1 + 0.006 (f'_c)^{\frac{1}{2}}]$

where, E_c and f'_c are in psi, and W is in pcf.

Pauw's expression for E_c is somewhat more general than the others and was adopted by the ACI (56).

A number of expressions have also been proposed to estimate the ultimate strain of concrete under compression. Some of them are:

HOGNESTAD	$\epsilon_u = 0.0038$
BRANDTZAEG	$\epsilon_u = (6.88 + 0.77 f'_c / 1000) \cdot 10^{-3}$
SALIGER	$\epsilon_u = (1.75 f'_c) \cdot 10^{-6}$

JENSEN	$\epsilon_u = f'_c / (1 - \beta) E_c$
ROS	$\epsilon_u = (3.5 - 2860 / f'_c) \cdot 10^{-3}$
CHANBAND	$\epsilon_u = 0.0036$

where E_c and f'_c are in psi.

The ACI (56) has adopted a more conservative value of $\epsilon_u = 0.003$ in/in.

As it can be seen from this brief review, several different shapes of stress-strain curves have been proposed for the behavior of concrete under compression. From the existing experimental data, it has been observed that none of the proposed stress-strain relationships can fit accurately the actual concrete stress-strain curve for all different loading conditions.

Hognestad's (44) stress-strain relationship (a parabolic ascending part, up to a maximum stress of $f''_c = 0.85 f'_c$ and a straight line descending part, up to an ultimate strain of -0.0038 in/in and $f_c = 0.85 f''_c$) has been adopted by a number of investigators with the result of the analysis in fairly good agreement with experimental data.

The present study does not propose a new stress-strain relationship for concrete under compression, nor does it intend to compare the effects of the use of different relationships on the behavior of the structures studied. However, two different stress-strain relationships for concrete under compression have been adopted and can be used alternatively for performing the analyses.

For a more refined analysis, although somewhat more time consuming,

the Hognestad's stress-strain relationship is chosen. The initial modulus of elasticity for concrete can be approximated by either: the Hognestad's proposed expression

$$E_c = 1\,800\,000 + 460 |f'_c|$$

or by the ACI's adopted expression

$$E_c = 33 W^{3/2} (|f'_c|)^{1/2}$$

when experimental data for this particular property are not available.

For a somewhat less time consuming analysis, or for a preliminary, supposedly less refined, analysis a bilinear stress-strain relationship can be adopted, as shown in Fig. 2.3, and with the following equations:

For $0 < \epsilon < \epsilon_0$

$$f_c = E_{ci} \epsilon$$

For $\epsilon_0 < \epsilon < \epsilon_u$

$$f_c = f'_c$$

where

f_c = Concrete stress at strain ϵ

f'_c = Maximum concrete cylinder strength

E_{ci} = Initial modulus of elasticity

$= 33 W^{3/2} (|f'_c|)^{1/2}$ or as obtained experimentally

$\epsilon_0 = f'_c / E_{ci}$

$\epsilon_u = -0.003$ or as obtained experimentally

The use of any other stress-strain relationship, including the option of some curve fitting in available experimental data, is possible to be incorporated in the proposed analysis, without any major

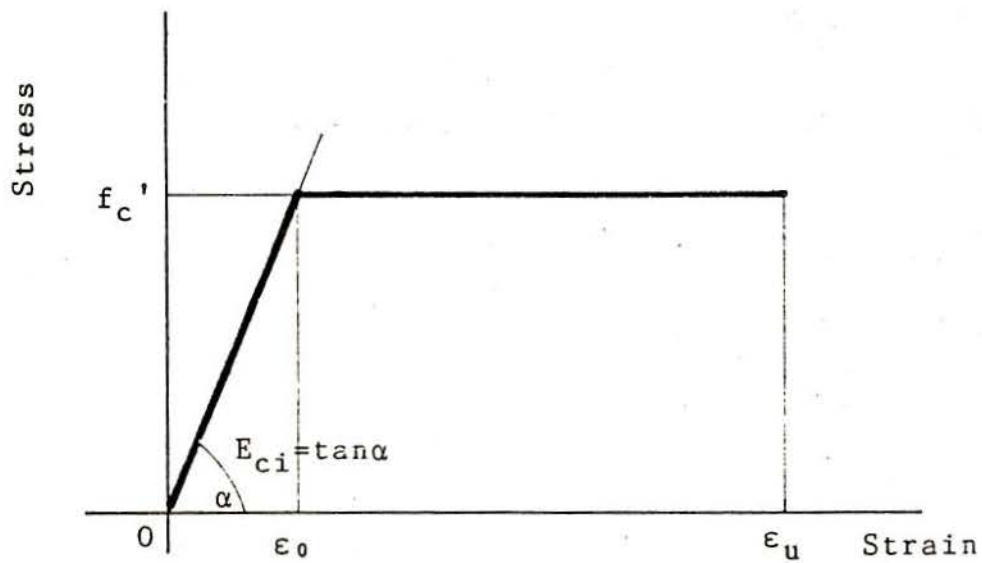


Fig 2.3 - Bilinear stress-strain relationship for concrete in compression.

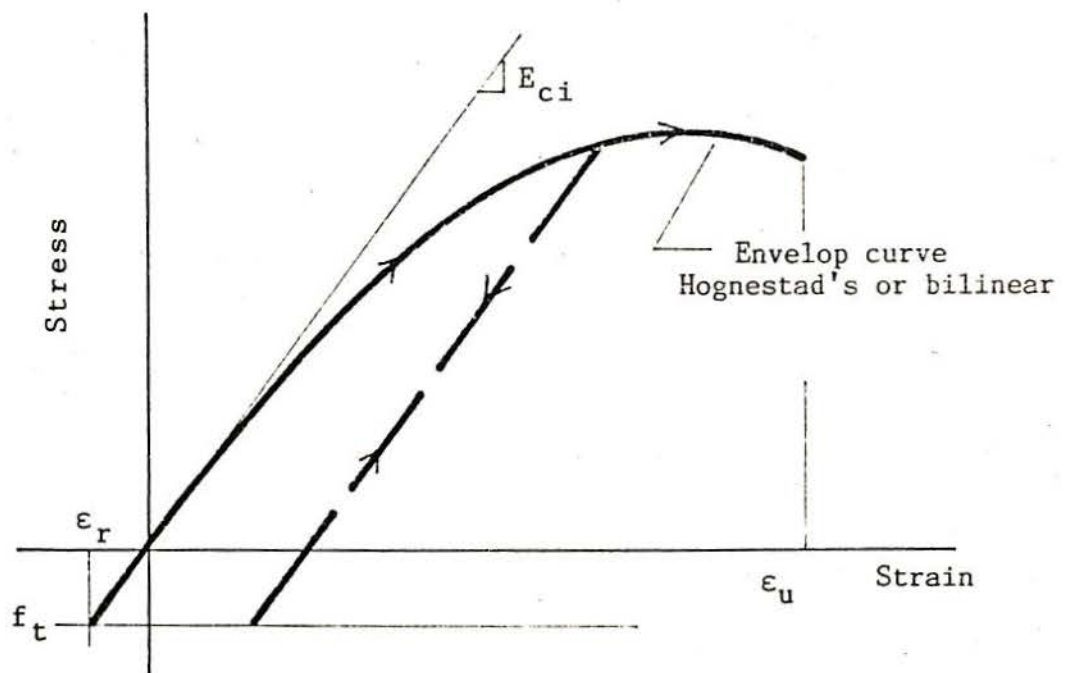


Fig 2.4 - Complete stress-strain relationship for concrete under tension and compression, for loading, unloading and reloading.

programming effort.

For a more accurate modeling of the behavior of concrete in a structure subjected to bending and axial load, the complete stress-strain relationship is needed. The complementary part of the stress-strain curves outlined previously, is referred to as the tensile stress-strain relationship of concrete.

2.1.1.2 Tensile Behavior

Tensile strength of concrete is usually neglected in conventional reinforced concrete theory. Its magnitude is so small that the stress induced by shrinkage in reinforced concrete members may exceed the tensile strength and cracks may develop even before the member is loaded. It does seem logical to neglect its effect in reinforced concrete members. However, in a prestressed concrete member, concrete stress can be controlled in such a way that under service load conditions it rarely exceeds the tensile strength of concrete. Because the stiffness of the member after it is cracked is greatly reduced, to neglect the tensile strength of concrete would greatly affect the prediction of the response of a prestressed beam prior to cracking.

Since the tensile strength of concrete is relatively small, compared to the compressive strength, and stresses in a prestressed concrete beam are mostly in compression, the tensile stress-strain relationship for concrete may be adequately represented as a straight line at a slope equal to the initial modulus of elasticity for concrete E_{ci} up to the modulus of rupture f_r as:

For $0 \leq \epsilon \leq \epsilon_r$

$$f_t = E_{ci} \epsilon$$

For $\epsilon_r > \epsilon$

$$f_t = 0$$

where

f_t = Concrete tensile stress at a strain

E_{ci} = Initial modulus of elasticity

ϵ_r = Concrete strain corresponding to the modulus of rupture

$$= f_r / E_{ci}$$

f_r = Modulus of rupture of concrete

The modulus of rupture is obtained generally by bending tests of short prismatic plain concrete beams, or by splitting tension test of concrete cylinders. The latter is also known as Brazilian test.

The accuracy of the estimate of the modulus of rupture is important, for it directly influences the cracking moment of the sections. The current trend is to express the modulus of rupture as a power function of the maximum cylinder strength as:

$$f_r = a |f'_c|^b$$

The ACI (56) , recommends the value of a as 7.5 for normal weight concrete, 0.85×7.5 for sand-lightweight concrete, and 0.75×7.5 for all-lightweight concrete, and the value of b as $1/2$. However, tensile stress ranging from $6.0 (|f'_c|)^{1/2}$ to $12.0 (|f'_c|)^{1/2}$ is allowed at service load for a prestressed concrete member in flexure. The deflection must be checked by a rational analysis for those higher stress levels which may produce cracking.

Some investigators (57) , based on tests on post-tensioned composite bridge girders, stated that the use of f_r equal to $7.5 (|f'_c|)^{\frac{1}{2}}$ gave good indication of the positive moment cracking potential and $6.0 (|f'_c|)^{\frac{1}{2}}$ worked well for the negative cracking moment and cracking at the junctions between the precast girders and the cast-in-place splice concrete. For the present study, where available experimental data are lacking, the ACI's recommendation would be used for the prediction of the concrete modulus of rupture.

2.1.1.3 Cyclic Loading

The previously mentioned stress-strain relationships for concrete were proposed to model the behavior of the material under a monotonic increase of stress with small strain increments. At any point inside a prestressed or reinforced concrete member, however, there may be a superposition of tensile and compressive strains at different times during the loading history. This may be a consequence of not only the different loading conditions but also the possible redistribution of stresses as well as the effects of time.

After an intensive investigation on concrete cylinders tested under cyclic loading, Sinha, et al (58) have observed that the action of repeated compressive loading produces a pronounced hysteresis effect in the stress-strain curve of concrete. Karsan and Jirsa (59) by testing prismatic concrete specimens, have also observed that the envelope curve of a specimen tested under cyclic loading and unloading coincides with the stress-strain curve for a specimen under monotonic loading to failure. The stress-strain path reached the envelope curve regardless of the strain accumulated prior to a particular loading cycle. Both investigators have developed a series of analytical expressions for the

prediction of intermediate unloading and reloading curves obtained from the hysteresis effect. From the experimental data, however, it can be observed that during unloading and reloading at relatively low levels of strain, the stress-strain curves follow a line which is approximately parallel to the initial tangent to the envelope stress-strain curve. Such a simplification seemed reasonable and has been adopted for this study.

The assumed stress-strain relationship, then, follows a Hognestad's or a bilinear stress-strain curve under monotonically increasing load. When unloading occurs, a straight line parallel to the initial tangent is followed. For reloading, this same line is tracked until reaching the envelope curve which is then followed for further loading. A complete picture of the assumed stress-strain relationship for concrete is shown in Fig. 2.4.

2.1.2 Types of Strain

Total strain in concrete under sustained load at any time may be considered as consisting of two types: instantaneous strain and time-dependent strain. Different definitions of the strain types may be used by different investigators. In this study, the following definitions will be used.

Instantaneous strain - The instantaneous, elastic or inelastic strain, is the strain that occurs during the changing of load. The stress-strain relationship follows a previously defined stress-strain curve. In the event of the changing of the stress-strain relationship,

with time, the stress-strain curve at the time of consideration will be followed.

Time-dependent strain - The time-dependent strain is the one that occurs in excess of the instantaneous strain. It can be further subdivided into two components: creep or creep recovery, the increase or decrease in strain with the time under sustained load or removal of load, and shrinkage strain, the change in strain with time due to the change in moisture content of concrete.

Creep or creep recovery and shrinkage occur simultaneously and are not independent of one another, thereby limiting the application of the principle of superposition. Shrinkage tends to increase the magnitude of creep and vice-versa (60,61) . However, for convenience and simplicity, they are usually assumed to be independent and additive.

Shrinkage is regarded as the portion of time-dependent strain occurring in a specimen due to the change in moisture content of concrete, if the specimen is not loaded. Creep or creep recovery is regarded as the portion of time-dependent strain in excess of shrinkage, caused by sustained load or removal of sustained load.

It is rather difficult, if not impossible, to experimentally obtain the effect of creep alone in a continuously loaded concrete specimen. It is necessary to assure that no shrinkage occurs during the process which can only be accomplished by keeping in the specimen the same original moisture content. By loading the specimen, however, this moisture content may be varied and some load induced shrinkage (61) may occur, increasing the strain supposedly attributed to creep. On the

other hand, there is no such interaction problem in pure shrinkage tests, in which the specimen is free of load.

Commonly, two separate tests are conducted, one for pure shrinkage and one for combined creep and shrinkage, and the results are linearly subtracted, attributing the difference to pure creep. The interaction between creep and shrinkage is therefore neglected and the resultant creep coefficients may be overestimated.

2.1.3 Time-dependent Properties

2.1.3.1 Creep Under Constant Stress

Creep of concrete under constant sustained stress follows a specific pattern. Experimental evidence indicates that the creep strain occurring over a given period of time is proportional to the applied stress, up to some limiting stress level. Researchers are in conflict with respect to the stress level at which the linearity between creep and the applied stress ceases. Some indicate loss of linearity at stresses as low as $0.2 f'_c$, others suggest a value of $0.5 f'_c$ and even $0.9 f'_c$. Rate of creep decreases with time providing that stress is not high enough to cause progressive internal cracking, which leads to time failure. Creep tends to approach a finite limiting value. Although some experimental data show that creep deformation continues over periods as long as thirty years, the rate of creep at later ages is so small that it would not cause any significant deformation.

Attempts have been made to represent the creep-time response of concrete with mathematical functions so that the amount of creep under

sustained load may be estimated without performing long term creep measurements. Extensive references may be found in the report by Corley (62), ACI committee 209 (63) and the book by Neville (60).

Four different types of creep functions have been proposed by various investigators: power functions, logarithmic functions, exponential functions and hyperbolic functions.

The ACI Committee 209 (63), based on the work by Branson and Christiason (64), represented the creep-time relationship by a hyperbolic function as:

$$C_t = C_u t^b / (a + t^b)$$

The empirical constants, a and b , and the ultimate creep coefficient C_u are functions of material properties, geometry, ambient conditions and the time of loading. The values of a are found to range from 6 to 30, b ranges from 0.4 to 0.8 and C_u from 1.3 to 4.15. To estimate creep a standard creep equation is recommended,

$$C_{t,t'} = C_u (t - t')^{0.6} / [10 + (t - t')^{0.6}]$$

The equation is for concrete with 4 in or less slump, in 40 percent ambient relative humidity, with minimum thickness of 6 in or less, with loading age of 7 days. Concrete is moist cured or steamed cured for 1 to 3 days. The suggested average value of C_u is 2.35. In the above expressions t and t' are expressed in days and stand for age of concrete and age of concrete when loaded, respectively.

Correction factors are suggested for concrete under different conditions, as listed below.

For moist cured concrete -

$$CC_{LA} = 1.25 t'^{-0.118} , t' > 7 \text{ days}$$

For steamed cured concrete -

$$CC_{LA} = 1.13 t'^{-0.118} , t' > 7 \text{ days}$$

where CC_{LA} is the creep correction factor for age of concrete at loading t' days. Ambient relative humidity greater than 40 percent -

$$CC_H = 1.27 - 0.0067 H , H > 40 \%$$

where CC_H is the creep correction factor for ambient relative humidity H percent. Minimum thickness of the member -

$$CC_T = 1.14 - 0.023 T , \text{ for } < 1 \text{ year}$$

$$CC_T = 1.10 - 0.017 T , \text{ for ultimate}$$

where CC_T is the creep correction factor for member thickness T in in.

Slump test, S in in -

$$CC_S = 0.82 + 0.067 S$$

where CC_S is the creep correction factor for consistency of concrete.

Percent of fine aggregate by weight -

$$CC_F = 0.88 + 0.24 F$$

where CC_F is the creep correction factor for percent of fine aggregate F of concrete. Air content, A , in percent -

$$CC_A = 1.0 , A < 6 \%$$

$$CC_A = 0.46 + 0.09 A , A > 9 \%$$

where CC_A is the creep correction factor for air content A of concrete.

The PCI Committee on Prestress Losses (23) , recommended a method in determining prestress losses using a series of curves. The prestress loss due to creep may be converted in to the equivalent creep strain by dividing the loss by the modulus of elasticity of the prestressing steel (28.10^6 psi). Creep may then be written as follows:

$$(\epsilon_c)_{t,t'} = (c_\epsilon)_u CC_T CC_{LA} (g_c)_t f_c$$

where

CC_T = Correction factor for size and shape of member,
a function of volume to exposed surface ratio.

CC_{LA} = Correction factor for age of loading and length of curing.

$(g_c)_t$ = Function representing creep with time evaluated at time t.

For the curves representing the factors CC_T , CC_{LA} and the function $(g_c)_t$, refer to reference (23) .

The ultimate creep strain per unit stress, $(c_\epsilon)_u$ may be estimated as follows:

Normal weight concrete, moist cured not exceeding 7 days-

$$(c_\epsilon)_u = 3.455 \cdot 10^{-6} - 7.273 \cdot 10^{-13} E_c > 4.00 \cdot 10^{-6}$$

Normal weight concrete, accelerated curing -

$$(c_\epsilon)_u = 2.291 \cdot 10^{-6} - 7.273 \cdot 10^{-13} E_c > 4.00 \cdot 10^{-6}$$

Lightweight concrete, moist cured not exceeding 7 days -

$$(c_\epsilon)_u = 2.764 \cdot 10^{-6} - 7.273 \cdot 10^{-13} E_c > 4.00 \cdot 10^{-6}$$

Lightweight concrete, accelerated curing -

$$(c_\epsilon)_u = 2.291 \cdot 10^{-6} - 7.273 \cdot 10^{-13} E_c > 4.00 \cdot 10^{-6}$$

where $(\epsilon_c)_u$ is in in/in/psi.

The most complete creep prediction procedures are those recommended by the ACI Committee 209 (63), the PCI Committee on Prestress Losses (23), and the CEB (55). The latter two are not listed here.

In practice, creep-time response of a specimen can be conveniently estimated using one of these procedures with minimal data. Because of the scattering of the experimental data, as suggested by the range of the empirical constants for the function recommended by the ACI Committee 209, this procedure may not give enough accuracy. It may be preferable, although costly, to perform a short term test simulating the actual atmospheric conditions, and use the creep-time curve in the form of one of the recommended methods as a basis for estimating the creep-time response.

The expression in the form recommended by the ACI Committee 209, has been adopted by many investigators (21,28,64,65) with satisfactory results. In this study, the measured data on creep response will be used when available. In the absence of the long-term measurements, the ACI Committee 209 recommendations will be adopted.

2.1.3.2 Creep Under Variable Stress

The creep functions previously mentioned, represent the experimental data of concrete under a state of constant stress. In reality, under a variable arrangement of loading, stress in every part of the structure is changing, gradually or abruptly, with time. Although attempts have

been made, with considerable success, to use a single creep function to predict creep under gradually varying sustained stress, rather poor results were obtained in the case of abruptly changing stresses. Several techniques have been proposed to handle this situation.

It is assumed that there is a creep function representing creep-time relation of concrete under a constant stress, and assuming that creep is proportional to the applied stress, several methods are available to estimate the amount of creep under time-dependent stress. They may be divided into three broad categories: a) Creep depends on the stress at the time of consideration only. b) Rate of creep depends on the stress at time of consideration, and c) Rate of creep depends on the complete history of the stress application. The following are the most commonly used methods.

2.1.3.2.1 The Effective Modulus Method

This is probably the simplest and most widely used method. It uses an elastic approach, taking into account creep effects, exclusive of shrinkage, by using the effective modulus instead of the normal modulus of elasticity. The effective modulus is a function of time and can be defined as:

$$(E_{\text{eff}})_t = (E_c)_t / (1 + C_t)$$

where

$(E_{\text{eff}})_t$ = Effective modulus of elasticity of concrete at time t

$(E_c)_t$ = Modulus of elasticity of concrete at time t

C_t = Creep coefficient at time t .

The effective modulus method is of the first category, creep at any time depends on stress at that instant only. Stress history is disregarded. Upon the removal of stress complete creep recovery is assumed, which is rarely the case for concrete. The method will overestimate creep under gradually increasing stress and underestimate creep under gradually decreasing stress (66). Satisfactory results will be obtained for creep under approximately constant stress.

2.1.3.2.2 The Rate of Creep Method

Assuming that rate of creep at any age of concrete is independent of the time at which concrete is loaded, creep may be estimated as:

$$(\epsilon_c)_{t_n} = \sum_{i=0}^n (f_c)_i (\Delta c_\epsilon)_i$$

where

n = number of time increments in the interval of time

t_n = time at the end of time increment n

$(f_c)_i$ = concrete stress within time increment i

$(\Delta c_\epsilon)_i = (c_\epsilon)_{t_i} - (c_\epsilon)_{t_{i-1}}$, specific creep increment
in the time increment i

The method takes into account, to some extent, the history of the applied stress. Since the rate of creep in concrete decreases with the age of concrete, the method will underestimate the amount of creep due to stress applied at later ages. The rate of creep method, will underestimate creep under gradually increasing stresss and vice-versa. No creep recovery will be predicted upon the removal of load. Under constant stress, the method will give adequate accuracy.

2.1.3.2.3 The Superposition Method

The superposition method is of the third category, rate of creep depends on the complete history of the applied stress. According to Ross (66) , the superposition hypothesis may be stated as: The strain produced in concrete at any time t by stress increment applied at time $t' < t$ is independent of the effects of any stresses applied either earlier or later than the time t' . The stress increments may be either positive or negative, assuming that creep in tension and compression are equal for equal stresses, which is approximately true for concrete. For the principle of superposition, it is not easy to write a general equation, as done for the rate of creep method, but a numerical solution for any case is not a complicated matter.

Several investigators have compared the accuracy of the creep predictions, using different methods of analysis. Ross (66) have compared, in their original forms, the effective modulus method, the rate of creep method, and the superposition method with the measurements of creep under gradually increasing and decreasing stresses, and under severely variable stresses. The effective modulus method gave the poorest results. The rate of creep method gave results comparable to the superposition method. The first one underestimated creep under gradually increasing stress and vice-versa, the latter gave errors in the opposite sense. For severely variable stresses, both methods estimated creep approximately the same magnitude as the experimental data. However, the lack of creep recovery in the rate of creep method, upon removal of the stress, led to the error in the general shape of the

strain-time response curve. The trend of the strain-time response curve predicted by the superposition method agreed well with the data.

In the present study, both the rate of creep and the superposition methods are utilized, since the effective modulus method does not completely suit the needs of the problems analyzed.

2.1.3.3 Shrinkage

As in the creep-time relationship, shrinkage increases with time at a decreasing rate, providing that there is no change in ambient conditions. Shrinkage also tends to approach a finite value. While the final value of shrinkage of concrete depends on many factors, i.e. the composition of concrete, time of exposure to the atmosphere conditions, size and shape of the specimen, etc, the shape of the shrinkage-time curves for various concretes under different conditions are remarkably similar. It is then convenient to express the shrinkage-time relationship as a product of the ultimate shrinkage and a function of time, as done for the case of creep.

Although shrinkage has been noticed and studied from as earlier as the beginning of the century (67) , Ross (66) , was probably the first one to express the shrinkage-time relationship as a mathematical function. Since then, several investigators have proposed many different models and mathematical functions to represent the shrinkage-time relationship of concrete, and used with satisfactory results.

Based on the work by Branson and Christiason (64) , the ACI Committee 209 (63) recommended the following expression to predict

shrinkage:

$$(\epsilon_{sh})_t = (\epsilon_{sh})_u t^b / (a + t^b)$$

For normal, sand-lightweight and all-lightweight concretes, both moist and steamed cured, and using type I and type III cements, the constants a and b, were found to range from 20 to 150 and from 0.9 to 1.1 respectively. The ultimate shrinkage $(\epsilon_{sh})_u$ was found to range from -415.10^6 in/in to -1070.10^6 in/in.

Standard shrinkage equations are suggested. The equations are for concrete with 4 in or less slump, placed in ambient relative humidity of 40 percent with minimum member thickness of 6 in or less.

Shrinkage of concrete after 7 days of moist curing -

$$(\epsilon_{sh})_t = (\epsilon_{sh})_u t / (35 + t)$$

Shrinkage of concrete after 1 to 3 days of steam curing -

$$(\epsilon_{sh})_t = (\epsilon_{sh})_u t / (55 + t)$$

The suggested average value for $(\epsilon_{sh})_u$ is -800.10^6 in/in for moist cured concrete and -730.10 in/in, for steam cured concrete. The following corrections are used for concrete with other conditions:

Shrinkage correction factor for ambient humidity greater than 40 percent

$$CS_h = 1.4 - 0.01 H, \quad 40 < H < 80$$

$$CS_h = 3.0 - 0.03 H, \quad 80 < H < 100$$

Shrinkage correction factor for member thickness -

$$CS_t = 1.23 - 0.038 T, \quad \text{for 1 yr. of drying}$$

$$CS_t = 1.17 - 0.029 T \quad , \quad \text{for ultimate value}$$

Shrinkage correction factor for consistency of concrete -

$$CS_s = 0.89 - 0.041 S \quad , \quad \text{where } S = \text{slump in in}$$

Shrinkage correction factor for cement content of concrete -

$$CS_b = 0.75 + 0.034 B$$

where B is the number of 94 lb sacks of cement per cubic yard.

Shrinkage correction factor for aggregate content of concrete -

$$CS_f = 0.3 + 0.014 F \quad , \quad F < 50$$

$$CS_f = 0.9 + 0.002 F \quad , \quad F > 50$$

where F is the percent of fine aggregate by weight.

Shrinkage correction factor for air content -

$$CS_a = 0.95 + 0.008 A$$

where A is the air content in percent.

For shrinkage of concrete moist cured one day, a correction factor of 1.2 is used. A linear interpolation may be used between 1.2 at 1 day and 1.0 at 7 days.

The PCI Committee on Prestress Losses (23) recommended equations to calculate prestress losses due to shrinkage. By dividing the values of the prestress loss due to shrinkage by the modulus of elasticity of the prestressing steel, (28.10^6 psi), those values may be written in terms of the equivalent shrinkage strain as:

$$(\epsilon_{sh})_t = (\epsilon_{sh})_u CS_t (\epsilon_s)_t$$

where

$$(\epsilon_{sh})_t = \text{Shrinkage strain at time } t$$

$(\epsilon_{sh})_u$ = Basic value for ultimate shrinkage

CS_t = Correction factor for shape and size of member

$(g_g)_t$ = Function representing the development of shrinkage with time, evaluated at time t

The basic value for ultimate shrinkage $(\epsilon_{sh})_u$ may be written as:

For normal weight concrete -

$$(\epsilon_{sh})_u = -9.643 \cdot 10^{-6} + 1.071 \cdot 10^{-10} E_c < -4.29 \cdot 10^{-6}$$

For lightweight concrete -

$$(\epsilon_{sh})_u = -1.464 \cdot 10^{-6} + 3.571 \cdot 10^{-10} E_c < -4.29 \cdot 10^{-6}$$

The values are in in/in. The correction factor for the shape and size of the member CS_t and the shrinkage-time function, (g_g) can be found in tables and curves shown in the PCI publication (23).

The expressions in the form proposed by the ACI Committee 209, have been used by several investigators (49,64,65) with satisfactory results. In the present study, the measured values of ultimate shrinkage, from the comparable specimens, will be used when available. In the absence of such experimental data, the ACI committee 209 recommendations will be used.

2.1.3.4 Aging

Concrete under normal ambient conditions gains strength with age because of further hydration of the cement. A study of fifty year properties of concrete by Washa and Wendt (68), showed the increase in

strength of concrete to reach a peak value at the ages of about 10 to 50 years, depending on the storage conditions and the type of cement used, and showed strength decrease thereafter. The average increase in compression strength at the age of fifty years is about 10 to 40 percent of the strength of the comparable specimens at the age of 28 days. Although the increase in strength is usually neglected in design, for more accuracy, the effect will be included in the present study.

Compressive strength tests of concrete cylinders are usually made at the age of 7 or 28 days. Several investigators have attempted, almost all of them with experimental data, to relate the strength of concrete at a later age to the strength at a standard early age. The relationship depends on many factors, such as water-cement ratio, mix proportion, qualities of cement, curing conditions, and cross-sectional shape. For a particular mix, age strength relationship of concrete may be expressed as a function of the age of concrete and curing conditions. Several empirical expressions have been proposed by many investigators. In this study, the ACI Committee 209 recommendations (63) will be adopted.

Based on the work by Branson and Christiason (64), the ACI Committee 209 recommends the use of a hyperbolic function for the prediction of the aging effect on the strength of concrete

$$(f'_c)_t = (f'_c)_{28} \frac{t}{a + b t}$$

From the measurement of some 88 specimens, of normal weight, sand-lightweight, and all-lightweight concrete, using both moist curing and steam curing, and type I and type III cements, the values of the constant a are found to range from 0.5 to 9.25, and the constant b from

0.67 to 0.98.

The following values have been suggested for different types of cement and curing conditions.

Moist cured concrete and type I cement -

$$(f'_c)_t = (f'_c)_{28} \ t / (4.00 + 0.85 \ t)$$

Moist cured concrete and type III cement -

$$(f'_c)_t = (f'_c)_{28} \ t / (2.30 + 0.92 \ t)$$

Steamed cured concrete and type I cement -

$$(f'_c)_t = (f'_c)_{28} \ t / (1.00 + 0.95 \ t)$$

Steamed cured concrete and type III cement -

$$(f'_c)_t = (f'_c)_{28} \ t / (0.70 + 0.98 \ t)$$

The stress-strain curves of concrete, as previously discussed, can be expressed as a function of the cylinder compressive strength of concrete, f'_c . For consistency, every key value should be estimated from the strength of concrete at the time of consideration. Without redefining the general shape of the curve, a stress at any strain, at different ages, may be found from modified curves taking into account the aging factor $(f'_c)_t / (f'_c)_{28}$.

The factors are applied in such a way that the initial and instantaneous modulus, and the stress and maximum compressive strength of the modified curve will be the same as those of the actual curve at that age. The strain limits, however, will not be modified in the new curves.

2.2 Reinforcement Steel

2.2.1 Constitutive Relationship for Loading and Unloading

Instantaneous stress-strain relationship of steel is usually obtained from uniaxial tensile tests of a sample taken from the steel of interest. Unlike concrete, the tensile stress-strain curve of steel can be obtained up to the ultimate strain of the material, with relative ease. The stress-strain curve is commonly assumed to have symmetry about the origin, i.e. the stress-strain response in compression is the same as in tension. Since there is no aging effect in steel, the stress-strain relationship can be used to represent the instantaneous tensile and compressive response without any modification.

As commonly used in design and analysis the stress-strain relationship of mild steel may be approximated by a perfect elasto-plastic, bilinear curve, as shown in Fig. 2.5, with results presenting a very acceptable degree of accuracy.

For the case of unloading and reloading of the reinforcement steel, it is well known that this material presents the effect of hysteresis, although much less pronounced than in the case of concrete. However, an usual simplification is to assume that the unloading and reloading curves follow straight lines, parallel to the initial loading curve, inscribed within the envelope, monotonically obtained stress-strain relationship (58,69) .

In the present study, both simplifications have been assumed, and the adopted stress-strain relationship for loading, unloading and reloading is sketched in Fig. 2.5.

2.3 Prestressing Steel

2.3.1 Constitutive Relationship for Loading and Unloading

As will be seen in a later chapter, the approach used in this study requires stresses in the member to be obtained from the strains. The problem is less complicated in the case of steel, since there is no change in strain of steel due to aging and moisture content. The total strain in steel may be considered as the sum of instantaneous and relaxation strains. Relaxation will be defined as the time-dependent loss of stress of steel under relatively constant strain. Relaxation strain will be defined as the reduction in strain that gives the reduction in stress equal to relaxation, utilizing the instantaneous stress-strain relationship of the material.

As with the case of mild steel, the instantaneous stress-strain relationship for prestressing steel is obtained from uniaxial tensile tests. This material, however, presents a somewhat different stress-strain curve, in the sense that there is no well-defined yield point and it shows a comparatively smaller ductility range.

A simplified tri-linear stress-strain curve seems to be a reasonable approximation for the stress-strain relationship under monotonic tensile stressing of prestressing steel, and it has been adopted in this study. As the case of concrete and reinforcing steel, the stress-strain relationships for unloading and reloading have been assumed as straight lines parallel to the initial loading curve. The assumed and simplified stress-strain relationship for the prestressing steel, in tension, for loading, unloading and reloading, is shown in Fig. 2.6.

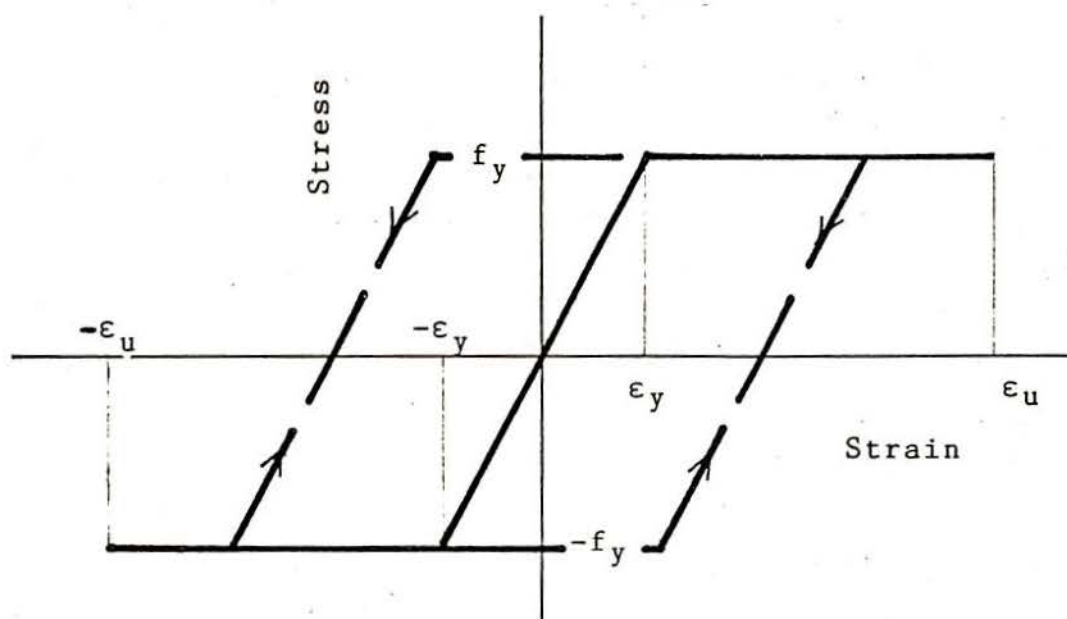


Fig 2.5 - Elasto-plastic stress-strain relationship for reinforcing steel.

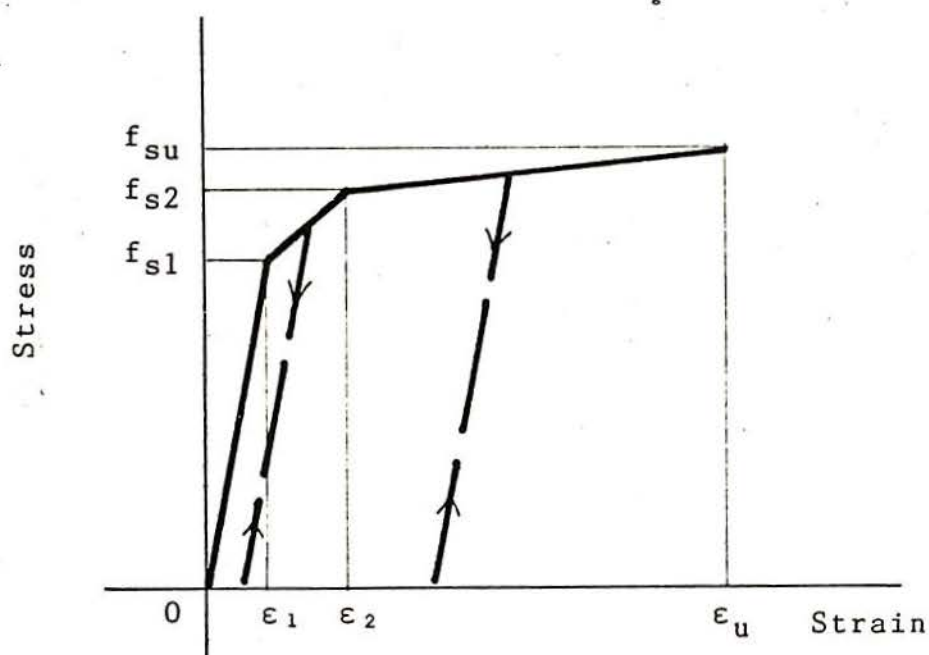


Fig 2.6 - Tri-linear stress-strain relationship for prestressing steel.

2.3.2 Relaxation Under Constant Strain

For prestressed concrete members, the relaxation of steel is of great concern. Initially the stress in prestressing steel is as high as 0.8 of its ultimate strength. At this level, relaxation over a long period of time may be as high as 15 percent of its initial stress (70). Although relaxation does not decrease the flexural strength of a bonded prestressed member, it affects the servicibility of the member.

Relaxation is a function of type of steel, initial stress-strength ratio, and temperature. It is also affected to some extent by rate of loading. High temperature may increase long-term relaxation several times, but under ordinary ambient conditions the temperature effect is negligible. The effect of rate of loading may also be neglected, since it has been shown that the rate of loading has an effect at the initial stress-strength ratio of about 0.8 to 0.94 (70), well above the stress level that would occur under service load.

Many papers have been published reporting relaxation test results and some investigators have attempted to describe relaxation as mathematical functions, like power functions, quadratic functions and logarithmic functions.

The PCI Committee on Prestress Losses (23) recommended the relaxation expression from Magura, et al (71), with the distinction between stress-relieved and low-relaxation steels. The following expressions are recommended:

For stress relieved steel -

$$(f_r)_{t,t_1} = (f_s)_t - (f_s)_{t_1}$$

$$= (f_s)_t [(\log 24t - \log 24t_1) / 10] [(f_s)_t / f_{sy} - 0.55]$$

$$(f_s)_t / f_{sy} > 0.60, \quad f_{sy} = 0.85 f_{su}$$

For low-relaxation steel -

$$(f_r)_{t,t_1} = (f_s)_t - (f_s)_{t_1}$$

$$= (f_s)_t [(\log 24t - \log 24t_1) / 45] [(f_s)_t / f_{sy} - 0.55]$$

$$(f_s)_t / f_{sy} > 0.60, \quad f_{sy} = 0.90 f_{su}$$

where

$(f_s)_t$ = Stress in prestressing steel at time t in days

$(f_r)_{t,t_1}$ = Relaxation stress of prestressing steel
between times t and t_1 in days

f_{sy} = Specified yield stress of steel

f_{su} = Ultimate strength of steel

In this study the above expressions are used.

2.3.3 Relaxation Under Variable Strain

Strain variation in prestressing steel is not as severe as stress variations in concrete and reinforcing steel. In an ordinary prestressed concrete member, the change in strain of prestressing steel under service load rarely exceeds 20 percent of the initial strain. Consequently, not much attention had been paid to relaxation under variable strain. Most of the relaxation data were obtained under constant strain, and the relaxation functions previously mentioned were based on this type of data. Under varying strain, however, Ghali and Trevino (16) have shown that the relaxation in prestressed concrete steel is of smaller magnitude than the intrinsic relaxation which occurs

when a tendon is stretched with constant strain, and it is assumed (23) that a method equivalent to the rate of creep method is adequate to handle the situation of variable strain. It was decided then, in the present study, to use a method equivalent to the rate of creep method in determining the relaxation of prestressing steel under variable strain.

2.4 Elastomeric Bearing Pads

Bearing pads are widely used in all kinds of precast structures. Their main purpose is to distribute vertical loads over the bearing area and to reduce force build-up at the connections by permitting some small displacements and rotations. In the case of bridge girders, especially for accommodating the temperature variation, their use has proven beneficial and often may be necessary for satisfactory performance.

Several different materials and compositions have been used for the manufacturing of structural bearing pads such as AASHTO-grade chloroprene pads, made of pure neoprene and recently also mixed with reinforcing fibers; cotton-duck fabric reinforced pads, used for high compressive stress; tempered hardboard pads, used in hollow core slabs; TFE (trade name Teflon) coated pads, often used for large horizontal movements. For bridge girders, chloroprene pads laminated with alternated layers of bonded steel or fiberglass are widely used.

The design of such pads is influenced by many factors (18), like material used, hardness characteristics, shear modulus, ambient temperature and relative humidity variation, amount of pressure to be transmitted and overall characteristics of the structure where the pad

is to be used. Not many publications are found presenting experimental data from tests on bearing pads (72) , and few concern design recommendations for such connections (18,72,73) .

The PCI (18) based on the work from Iverson, et al (73) , presents some recommendations for the selection and design of elastomeric bearing pads. Referring to Fig. 2.7, the compressive stress f which depends on the hardness characteristic of the material and ambient temperature, is limited to a maximum of 1000 psi.

$$f = V / b w \leq 1000 \text{ psi}$$

The maximum allowed compressive stress, for 15 percent strain, is obtained according to the shape factor S ,

$$S = w b / 2 t (w + b)$$

and the maximum unfactored shear force N is obtained from

$$N = \Delta w b G_t / t$$

where

f = Unfactored compressive stress, in psi

V = Unfactored vertical reaction, in lb

N = Unfactored horizontal reaction, in lb

W = Dimension parallel to the beam span, in in

b = Dimension perpendicular to the beam span, in in

t = Total thickness of the pad, in in

G_t = Long-term shear modulus, in psi

$$= G / 2$$

G = Shear modulus

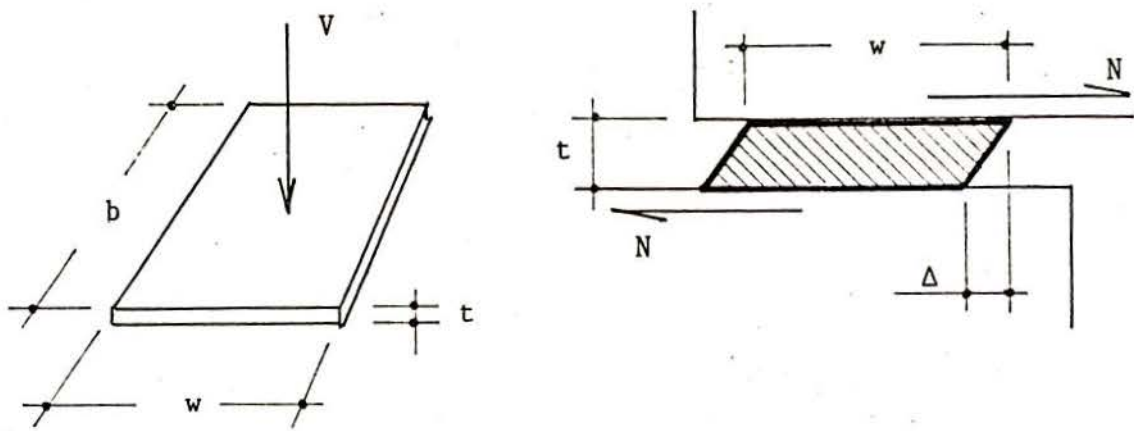


Fig 2.7 - Bearing pads.

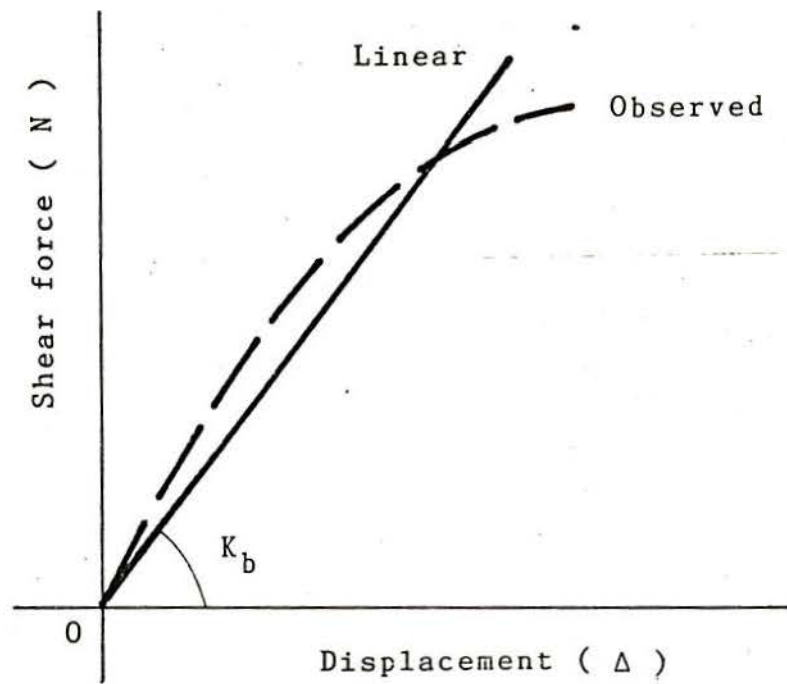


Fig 2.8 - Linear shear-deformation relationship for bearing pads.

Δ = Shear deformation, in in

The shear force-deformation relationship ($N - \Delta$) presented by those pads, as shown in the work by Vinje (72) , is nonlinear. Assuming that they are properly designed and working within the service load range of the structure, a linear relationship may be assumed, neglecting the nonlinear effect on the value of the horizontal reaction N . In the present study, a linear force-deformation relationship as shown in Fig. 2.8 is assumed for modeling the support bearing pads, and their stiffness coefficient is obtained as:

$$N = K_b \Delta$$

$$K_b = G_t A / t$$

where

N = Unfactored horizontal reaction, in lb

Δ = Maximum expected shear deformation in in

A = Contact area of the bearing pad, in in²

t = Total pad thickness, in in

G_t = Long-term shear modulus, in psi

K_b = Shear stiffness of the bearing pad, in lb.in³

Where experimental data for the bearing shear stiffness is available, this value will be used. In the absence of such data, the value obtained as shown above will be assumed.

3. METHOD OF ANALYSIS

3.1 Introduction

A general composite beam may have a variable cross-section along its length. Its constituent members may be simply supported over one span or continuous over two or more spans. Continuity may be fully obtained by casting a continuous girder and deck or by connecting individual one-span girders to one another through diaphragms over the intermediate supports. Girders may be, otherwise, indirectly connected to its companion by casting a continuous deck slab. Loads and restraints may be applied in any of the three directions, i.e. the member axial direction, the transverse direction and the rotational direction. Applied loads may be concentrated or linearly distributed. The beam may be of reinforced concrete, prestressed concrete or steel. The amount of reinforcing steel in various layers and the magnitude and location of the prestressing force may also vary along the length. Response analysis of such a structure may encounter a considerable amount of complexity when nonlinear and time-dependent effects are also introduced and analytical closed-form solutions are not possible. A numerical solution, however, seems to be a suitable approach.

Many numerical solutions for the analysis of beams are found in the literature. Some, using the finite element technique, are adequate for reinforced concrete members (28,29,30,31,32,33) and others based on the discrete element method are applied to prestressed concrete members (34,35,36,37,38). However, none was found broad enough as to suit the needs of the problem under consideration, as discussed in Chapter 1.

In this chapter a method of analysis based on the finite element technique is presented. Two elements are formulated and used for modeling beams and deck-continuity among the beams. Beam elements may be used for the analysis of either steel, reinforced concrete, prestressed concrete or composite steel-concrete members. Connection elements, however, are used only for modeling reinforced concrete deck slabs. Both instantaneous and time-dependent responses of a beam may be obtained by the proposed solution. Linear and nonlinear ranges of behavior are captured in one single analysis where loading and restraints are predefined according to the actual stages of construction.

3.2 Beam Element

3.2.1 Conventional Beam Element

The formulation of a conventional beam element is well known and can be found in many books on finite element methods. For purpose of illustration, however, it is shown in this section and used for comparison with the formulation of the isoparametric beam element adopted in this thesis.

Let us for the time being consider a two-noded three degrees-of-freedom per node beam element as shown in Fig. 3.1, having a cross-section with a vertical plane of symmetry. The behavior of such an element relies on the three basic assumptions that follow:

(a) The direct strains in the transverse direction y are negligibly small.

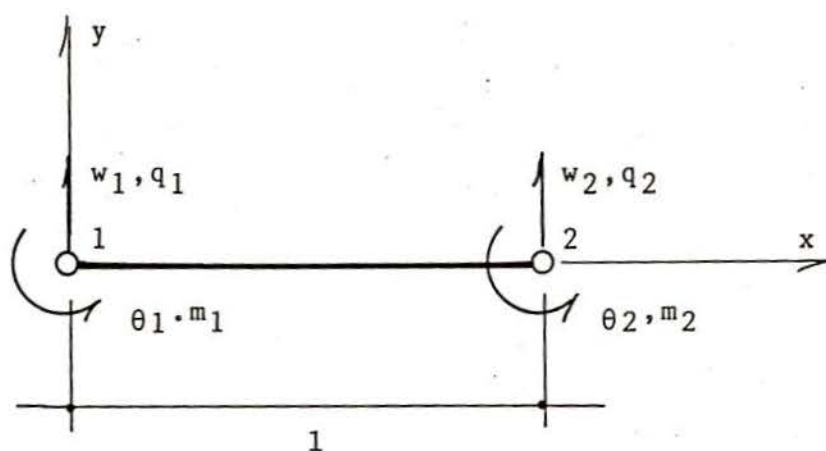


Fig 3.1 - Conventional beam element.

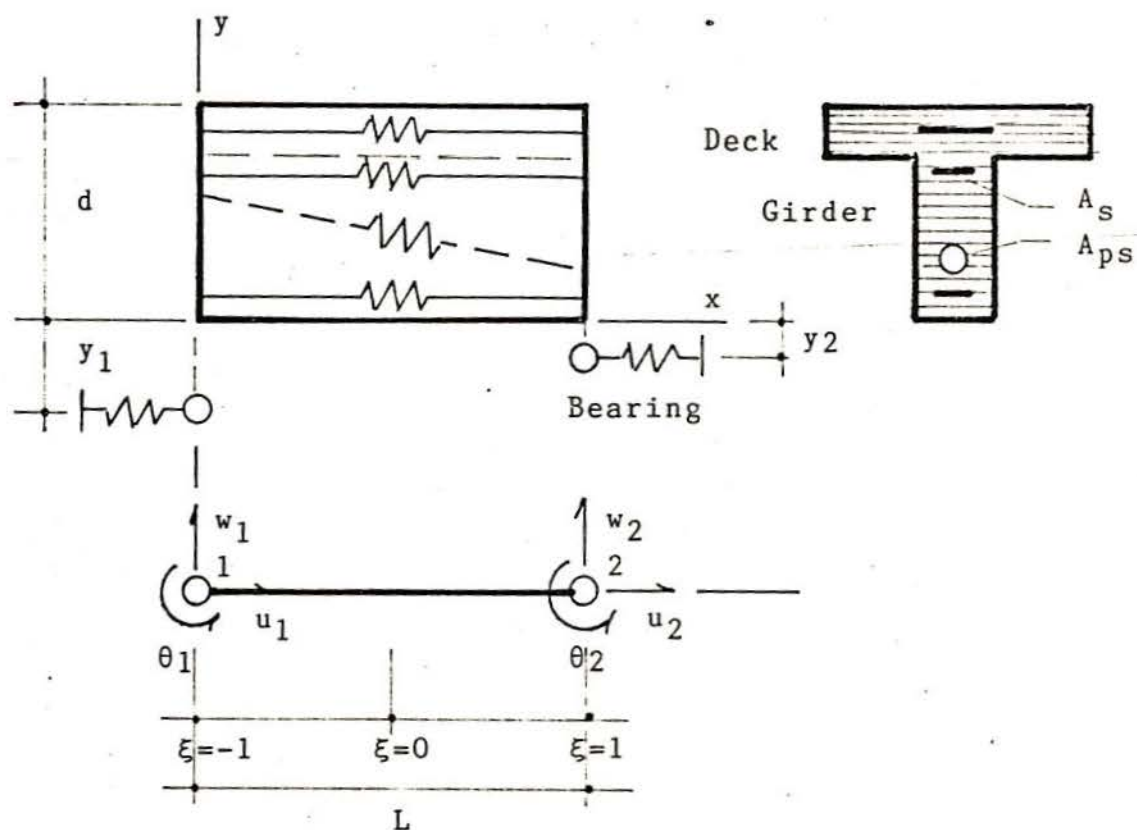


Fig 3.2 - Isoparametric beam element.

(b) A plane cross-section normal to the longitudinal axis of the beam remains plane after the beam deforms. Such is true when the transverse shear strain is constant through the thickness of the beam.

(c) A normal to the longitudinal axis of the beam, in the vertical plane of symmetry, remains normal to the longitudinal axis after deformation. It is thus implied that not only assumption (b) holds but that the transverse shear deformation is negligibly small, $\gamma_{xy}=0$. Assumption (a) above leads to the following.

$$\frac{\partial w}{\partial y} = 0 \quad 3.1$$

Accordingly the transverse displacement w is a function of the coordinate x alone. From assumptions (b) and (c) one have

$$\frac{\partial u}{\partial y} = - \frac{dw}{dx} \quad 3.2$$

Since w is not a function of y , eq. 3.2 may be integrated to give.

$$u = - \left(\frac{dw}{dx} \right) y + u_0(x) \quad 3.3$$

in which $u_0(x)$ is the longitudinal displacement in the direction of the reference axis x . The longitudinal strain ϵ_x is obtained by taking the derivative of the longitudinal displacement u in the equation above, leading to

$$\epsilon_x = - \left(\frac{d^2 w}{dx^2} \right) y + \frac{du_0}{dx} \quad 3.4$$

or

$$\epsilon_x = \kappa y + \epsilon_{x0}, \quad \kappa = - \frac{d^2 w}{dx^2}, \quad \epsilon_{x0} = \frac{du_0}{dx}$$

The beam is in a state of plane stress. For a linear, elastic, isotropic material the stress-strain relationship is given by

$$\begin{Bmatrix} \sigma_x \\ \sigma_y \end{Bmatrix} = \frac{E}{1 - \nu^2} \begin{bmatrix} 1 & \nu \\ \nu & 1 \end{bmatrix} \begin{Bmatrix} \epsilon_x \\ \epsilon_y \end{Bmatrix} \quad 3.5$$

It is known that the direct stress in the transverse direction σ_y , is negligibly small. Therefore, we assume $\sigma_y=0$ which with eq. 3.5 gives

$$\epsilon_y = -\nu \epsilon_x \quad 3.6$$

and

$$\sigma_x = E \epsilon_x \quad 3.7$$

In developing the strain-displacement relationship above we have assumed $\epsilon_y=0$, which is inconsistent with the assumption $\sigma_y=0$ made in the stress-strain relationship. This apparent inconsistency can be explained as follows. Neither ϵ_y nor σ_y are exactly equal to zero, but both are quite small. In using these assumptions, however, we should avoid using the condition $\epsilon_y=0$ for evaluating $\sigma_y [= \nu E \epsilon_x / (1 - \nu^2)]$, and using the condition $\sigma_y=0$ for evaluating $\epsilon_y [= -\epsilon_x]$. A further justification of the above assumptions is that they lead to a beam theory which adequately agrees with the observed behavior.

According to eqs. 3.4 and 3.7, the longitudinal stress σ_x is written as

$$\sigma_x = E \kappa y + E \epsilon_{x0} \quad 3.8$$

and a normal force F , in the longitudinal direction, can be obtained by integrating the above stresses over the element cross-section as

$$F = \int \sigma_x dA = x \int E y dA + \epsilon_0 \int E dA \quad 3.9$$

Taking the reference axis of the above integration as the cross-section neutral axis and assuming that no axial force F is applied to the element, eq. 3.10 follows.

$$\epsilon_{x0} = \frac{du_0}{dx} = 0 \quad 3.10$$

Assuming no rigid body motion is present, displacement $u_0 = 0$. From assumption (a) it is concluded that $w = w(x)$. In the conventional beam element the transversal displacement field is represented by a cubic polynomial in x .

$$w = a + bx + cx^2 + dx^3 = (x) \{a\} \quad 3.11$$

$$(x) = (1 \ x \ x^2 \ x^3), \quad \{a\}^T = (a \ b \ c \ d)$$

The nodal displacements at nodes 1 and 2, vertical displacements w_1 and w_2 and rotations θ_1 and θ_2 respectively, may be expressed in terms of the coefficients of the assumed polynomial and the length of the element as

$$\{d\} = [A] \{a\}$$

or

$$\begin{Bmatrix} w_1 \\ \theta_1 \\ w_2 \\ \theta_2 \end{Bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 1 & l^2 & l^3 \\ 0 & 1 & 2l & 3l \end{bmatrix} \begin{Bmatrix} a \\ b \\ c \\ d \end{Bmatrix} \quad 3.12$$

In other words, the coefficients a, b, c and d of the polynomial defining the vertical displacement at any point within the element may be obtained in terms of the nodal displacements as

$$a = w_1$$

$$b = \theta_1$$

$$c = [3 (w_2 - w_1) - 2l (\theta_1 + \theta_2)] / l^2$$

$$d = [-2 (w_2 - w_1) + l (\theta_1 + \theta_2)] / l^3$$

3.13

For obtaining the vertical displacements w in terms of the nodal displacements, a set of shape functions N are defined as

$$w = (N) \{ d \} , \quad N = (x) [A]^{-1}$$

or

$$w = \frac{1}{l^3} \begin{Bmatrix} l^3 - 3lx^2 + 2x^3 \\ l^3x - 2l^2x^2 + lx^3 \\ 3lx^2 - 2x^3 \\ -l^2x^2 + lx^3 \end{Bmatrix}^T \begin{Bmatrix} w_1 \\ \theta_1 \\ w_2 \\ \theta_2 \end{Bmatrix}$$

3.14

Rotations θ , defined as the incremental rate of the vertical displacements w with respect to the horizontal coordinate x, are obtained by differentiating the shape functions (N) in eq. 3.14 as

$$\theta = \frac{d}{dx} (N) \{ d \} = (N') \{ d \}$$

or

$$\theta = \frac{1}{l^3} \begin{Bmatrix} -6 l x + 6 x^2 \\ l^3 - 4 l^2 x + 3 l x^2 \\ 6 l x - 6 x^2 \\ -2 l^2 x + 3 l x^2 \end{Bmatrix}^T \begin{Bmatrix} w_1 \\ \theta_1 \\ w_2 \\ \theta_2 \end{Bmatrix} \quad 3.15$$

Curvatures χ are obtained as the second derivative of the vertical displacements w , or the incremental rate of the rotations θ with respect to the axial coordinate x as

$$\chi = \frac{d^2 w}{dx^2} = - \frac{M}{EI}$$

or

$$\chi = - \frac{d^2}{dx^2} (N) \{d\} = (N'') \{d\} = (B) \{d\} \quad 3.16$$

or

$$\chi = \frac{1}{l^3} \begin{Bmatrix} -6 l + 12 x \\ -4 l^2 + 6 l x \\ 6 l - 12 x \\ -2 l^2 + 6 l x \end{Bmatrix}^T \begin{Bmatrix} w_1 \\ \theta_1 \\ w_2 \\ \theta_2 \end{Bmatrix}$$

Normal strains ϵ_x , which vary linearly through the depth of the element according to eqs. 3.7 and 3.10, may be obtained from the curvature χ as

$$\epsilon_x = \chi y$$

or

3.17

$$\epsilon_x = (B) \{d\} y$$

Observing the linear stress-strain relationship assumed, shown in eq. 3.7, the normal stresses σ_x are derived from the normal strains ϵ_x as

$$\sigma_x = E (B) \{ d \} y \quad 3.18$$

By applying to an element a set of arbitrary virtual displacements $\{\delta d\}$, normal strains $\delta\epsilon_x$ are therefore developed and may be expressed as

$$\delta\epsilon_x = (B) \{ \delta d \} y \quad 3.19$$

The internal work done by the stresses σ_x may then be obtained as

$$\delta W_i = \int_V \sigma_x \delta\epsilon_x dv$$

or

3.20

$$\delta W = \int_V \sigma_x (B) \{ \delta d \} y dv$$

Under the action of the external nodal forces $\{f\}$ and the applied virtual displacements $\{\delta d\}$, some external work is performed and may be expressed as

$$\delta W_e = \{ f \} \{ \delta d \}$$

or

$$\delta W_e = (q_1 \ m_1 \ q_2 \ m_2)^T \begin{Bmatrix} w_1 \\ \theta_1 \\ w_2 \\ \theta_2 \end{Bmatrix} \quad 3.21$$

As an equilibrium requirement, both internal and external work must be the same. Since $\{\delta d\}$ is arbitrary eqs. 3.20 and 3.21 give

$$\{ f \} = \int_V \sigma_x (B) y \, dv \quad 3.22$$

By substituting eq. 3.18 into eq. 3.22

$$\{ f \} = \int_V E (B) \{ d \} (B) y^2 \, dv$$

or 3.23

$$\{ f \} = \left[\int_V E (B)^T (B) y^2 \, dv \right] \{ d \}$$

The element stiffness matrix $[k]$, defined as the relation between applied forces $\{f\}$ and the nodal displacements $\{d\}$ is then expressed as

$$[k] = \int_V E (B)^T (B) y^2 \, dv$$

or 3.24

$$[k] = \int_1 EI (B)^T (B) \, dx$$

When stiffness EI is constant throughout the element the stiffness matrix may be expressed as

$$[k] = EI \int_1 (B)^T (B) \, dx \quad 3.25$$

The coefficients of the (4×4) stiffness matrix are obtained by substituting (B) , as shown in eq. 3.16, into eq. 3.25 and performing the linear integration as shown for the first coefficient k_{11}

$$k_{11} = EI \int_0^1 \frac{1}{l^2} (-6l + 12x)^2 \, dx = \frac{12 EI}{l^3} \quad 3.26$$

By applying an equivalent procedure, the remaining coefficients may be obtained and the final stiffness matrix is shown as

$$[k] = \begin{bmatrix} 12 & 6l & -12 & 6l \\ 6l & 4l^2 & -6l & 2l^2 \\ -12 & -6l & 12 & -6l \\ 6l & 2l^2 & -6l & 4l^2 \end{bmatrix} \frac{EI}{l^3} \quad 3.27$$

The derivation shown above models the behavior of a two-noded conventional beam element with two degrees-of-freedom per node, as shown in Fig. 3.1. Its formulation considers a beam element without any axial force and deformations. It is customary to include a horizontal degree-of-freedom at the two nodes if the axial forces are present. If the reference axis coincides with the neutral axis of the beam, as previously assumed, it can be shown that the axial and bending stiffness terms are mutually uncoupled. In order to apply support conditions and axial forces, which may not be at the neutral axis, a linear transformation may be used.

$$u(\text{ at } y) = u(\text{ at neutral axis }) - y\theta \quad 3.28$$

This, however, presents a problem as pointed out by Gupta and Ma (74). The axial displacement along the reference axis varies linearly with the x coordinate. On the other hand, the transverse displacement is cubic in x and consequently the rotational displacement is quadratic. According to eq. 3.28, u for any nonzero value of y is therefore quadratic. This creates an inconsistency, and renders the element unfit for cases when the transformation required in eq. 3.28 needs to be

applied. Therefore, the conventional beam element has been discarded for use in the present study.

3.2.2 Isoparametric Beam Element

Since their first appearance, in the sixties (75), isoparametric beam elements have shown remarkable versatility, they have proven effective in two- and three-dimensional structural analyses and non structural applications as well. They are named isoparametric for their property of expressing the displacement field and the coordinate transformation through the same (ISO) set of interpolation functions (parameters), commonly known as shape functions. Their general formulation can be found in most finite element books (76,77,78). Here, we will restrict ourselves to presenting the formulation of the one-dimensional beam element adopted.

As in the conventional beam element, here too, we assume that the direct strains in the transverse direction y are negligibly small and that the plane cross-section normal to the longitudinal axis of the beam remains plane after the beam deforms ($\gamma_{xy} = \text{constant along } y$). Unlike the conventional beam element, normal to the longitudinal axis of the beam, in the vertical plane of symmetry, are not assumed to remain normal after deformation. Further, the direct stress in the normal direction is assumed to be negligibly small, giving $\sigma_x = E\epsilon_x$, as in the conventional beam element.

Referring to Fig. 3.2, taking u_i , w_i and θ_i , $i = 1, 2$, as the nodal degrees-of-freedom in the x direction, y direction and rotational

direction respectively, the displacements at any point within the element can be expressed in terms of the shape functions as

$$u(y) = \sum_i N_i u_i - y \sum_i N_i \theta_i$$

$$w = \sum_i N_i w_i \quad 3.29$$

$$\theta = \frac{\partial u}{\partial y} = - \sum_i N_i \theta_i$$

The nodal coordinates can as well define the global coordinates at a point in the element, through the use of the same shape functions as

$$x = \sum_i N_i x_i \quad 3.30$$

The interpolation or shape functions are defined in terms of the local coordinate ξ as

$$(N) = (N_1 \ N_2) = \left(\frac{1-\xi}{2} \ \frac{1+\xi}{2} \right) \quad 3.31$$

The strain field is obtained as the first derivative of the displacements and also expressed in terms of the shape functions appear as

$$\epsilon_x = \frac{\partial u}{\partial x} = \sum_i \frac{\partial N_i}{\partial x} u_i - y \sum_i \frac{\partial N_i}{\partial x} \theta_i$$

$$\epsilon_y = \frac{\partial w}{\partial y} = \sum_i \frac{\partial N_i}{\partial y} w_i = 0 \quad 3.32$$

$$\gamma_{xy} = \frac{\partial u}{\partial y} + \frac{\partial w}{\partial x} = - \sum_i N_i \theta_i + \sum_i \frac{\partial N_i}{\partial x} w_i$$

which in matrix notation leads to the definition of the [B] matrix as follows

$$\begin{Bmatrix} \epsilon_x \\ \gamma_{xy} \end{Bmatrix} = \sum_i \begin{bmatrix} \frac{\partial N_i}{\partial x} & 0 & -y \frac{\partial N_i}{\partial x} \\ 0 & \frac{\partial N_i}{\partial x} & -N_i \end{bmatrix} \begin{Bmatrix} u_i \\ w_i \\ \theta_i \end{Bmatrix} \quad 3.33$$

or

$$\{ \epsilon \} = [B] \{ d \}$$

from which ζ is deleted because it is assumed to be zero. The nodal displacement vector consists of nodal degrees-of-freedom and is given by

$$\{ d \}^T = (u_1 \ w_1 \ \theta_1 \ u_2 \ w_2 \ \theta_2) \quad 3.34$$

The shape functions are expressed in terms of the local coordinate ζ , so the derivation chain rule is invoked

$$\frac{\partial N_i}{\partial x} = \frac{\partial N_i}{\partial \xi} \frac{\partial \xi}{\partial x} \quad 3.35$$

$$\frac{\partial x}{\partial \xi} = \sum_i \frac{\partial N_i}{\partial \xi} x_i = \left(\frac{\partial N_1}{\partial \xi} \ \frac{\partial N_2}{\partial \xi} \right) \begin{Bmatrix} x_1 \\ x_2 \end{Bmatrix}$$

and the scale factor between the two coordinate systems is defined as

$$\frac{\partial \xi}{\partial x} = \frac{2}{l} \quad 3.36$$

The [B] matrix is then obtained as

$$[B] = \begin{bmatrix} -\frac{1}{l} & 0 & \frac{y}{l} & \frac{1}{l} & 0 & -\frac{y}{l} \\ 0 & -\frac{1}{l} - \frac{1-\epsilon}{2} & 0 & \frac{1}{l} & -\frac{1+\epsilon}{2} & 0 \end{bmatrix} \quad 3.37$$

According to eq. 3.37 the transverse shear strain γ_{xy} varies linearly with ζ and therefore with x . The direct strain ϵ_x does not vary with ζ or x , which would be caused by a state of constant moment and axial force. The shear strain distribution is inconsistent with the moment distribution and is known to render the element stiffness matrix too stiff in shear (79). The spurious shear strains and stresses have been called parasitic and the effect on the element stiffness matrix shear-locking. It can be shown that eq. 3.33 evaluates the shear strain accurately at $\zeta = 0$, which points to the remedy of the problem: setting $\zeta = 0$ in eq. 3.37. Therefore the matrix $[B]$ becomes

$$[B] = \begin{bmatrix} -\frac{1}{l} & 0 & \frac{y}{l} & \frac{1}{l} & 0 & -\frac{y}{l} \\ 0 & -\frac{1}{l} - \frac{1}{2} & 0 & \frac{1}{l} - \frac{1}{2} & 0 & 0 \end{bmatrix} \quad 3.38$$

As stated earlier, a uniaxial stress-strain relationship is used. Therefore, the stress-displacement relationship may be defined as

$$\{\sigma\} = [E] \{\epsilon\} = [E] [B] \{d\}$$

where

$$[E] = \begin{bmatrix} E & 0 \\ 0 & G \end{bmatrix}, \quad G = \frac{E}{2(1+\nu)} \quad 3.39$$

Normal strains $\{\delta\epsilon\}$ corresponding to a virtual displacement vector $\{\delta d\}$ are given by

$$\{ \delta \epsilon \} = [B] \{ \delta d \} \quad 3.40$$

and the internal work done by the stresses may be obtained as

$$\delta W_i = \int_V \{ \sigma \} \{ \delta \epsilon \} dv \quad 3.41$$

or by substituting eqs. 3.39 and 3.40 into eq. 3.41 as

$$\delta W_i = \int_V [E] [B] \{ d \} [B] \{ \delta d \} dv \quad 3.42$$

Under the action of the external nodal forces $\{ f \}$, where

$$\{ f \} = (f_1 \ q_1 \ m_1 \ f_2 \ q_2 \ m_2)^T \quad 3.43$$

and the applied virtual displacements $\{ \delta d \}$, some external work is performed by those nodal forces and may be written as

$$\delta W_e = \{ f \}^T \{ \delta d \} \quad 3.44$$

By equating 3.41 and 3.44, seeking equilibrium between internal and external works, the nodal forces may be expressed as

$$\{ f \} = \int_V [E] [B] \{ d \} [B] dv \quad 3.45$$

or

$$\{ f \} = [\int_V [B]^T [E] [B] dv] \{ d \}$$

which define the element stiffness matrix $[k]$ as

$$[k] = \int_V [B]^T [E] [B] dv \quad 3.46$$

The coefficients of the $[k]$ matrix are obtained by performing the integration in eq. 3.46 as shown for the first coefficient k_{11}

$$k_{11} = \int_V \left(-\frac{1}{l} \right)^2 E dv = \frac{1}{l^2} \int_1 EA dx = \frac{EA}{l} \quad 3.47$$

By applying a similar procedure to the coefficients the complete matrix is obtained as

$$[k] = \begin{bmatrix} \frac{EA}{l} & 0 & -\frac{ES}{l} & -\frac{EA}{l} & 0 & \frac{ES}{l} \\ & \frac{GA}{l} & \frac{GA}{2} & 0 & -\frac{GA}{l} & \frac{GA}{2} \\ & & \frac{EI}{l} + \frac{GA}{4} & \frac{ES}{l} & -\frac{GA}{2} & -\frac{EI}{l} + \frac{GA}{4} \\ & & & \frac{EA}{l} & 0 & -\frac{ES}{l} \\ & & & & \frac{GA}{l} & -\frac{GA}{2} \\ & & & & & \frac{EI}{l} + \frac{GA}{4} \end{bmatrix} \quad 3.48$$

symmetric

where

$$EA = \int E \, dA, \quad ES = \int E y \, dA \quad \text{and} \quad EI = \int E y^2 \, dA$$

In the development of the isoparametric beam element it is not necessary to take the reference x-axis along the neutral axis. Therefore, the integral for ES is not necessarily zero.

3.2.3 Initial Strains

When studying the effects of prestressing and temperature variation in bridge beams, these effects are applied by specifying initial strains to an element. Such procedure is rather simple and may be shown as follows.

Let us assume that an initial strain vector $\{\epsilon_0\}$ is specified to a beam element as shown in Fig. 3.2. According to eq. 3.39, the final state of stress may be written as

$$\{\sigma\} = [E] \{\epsilon - \epsilon_0\} \quad 3.49$$

where $\{\epsilon\}$ is the current strain vector of the system exclusive of the effects contained in $\{\epsilon_0\}$. Equating 3.39 and 3.45 the vector of nodal forces may be written as

$$\{f\} = \int_V [B]^T \{\sigma\} dv \quad 3.50$$

and substituting 3.49 into 3.50 as

$$\{f\} = \int_V [B]^T [E] \{\epsilon\} dv - \int_V [B]^T [E] \{\epsilon_0\} dv \quad 3.51$$

The first term in eq. 3.51 may be identified with eq. 3.45 whereas the latter term may, accordingly, be written as a vector of nodal forces like

$$\{f\} = [k] \{d\} - \{f_0\}, \quad \{f_0\} = \int_V [B]^T [E] \{\epsilon_0\} dv$$

or

$$\{f\} + \{f_0\} = [k] \{d\} \quad 3.52$$

The vector of nodal forces $\{f_0\}$ represents the effect of the specified strains $\{\epsilon_0\}$ on the element. Thus, according to eq. 3.52, it can be added to the current vector of nodal forces $\{f\}$.

3.2.4 Prestressing Effect

As mentioned earlier in this chapter the precast or cast-in-place girders of a bridge structure may be of prestressed concrete, among other methods of construction. Prestressing forces are taken into

account by specifying initial prestressing strains in the tendons. The tendons initial strains ϵ_{po} are defined as the strains due to prestressing forces before releasing of the forces, i.e. the prestressing strain at the zero deflection state of the member. Since the initial prestressing force in a tendon is usually known, the strain that produces that stress level can be obtained from the stress level and the instantaneous stress-strain relationship of the tendon steel as shown in Section 2.3.1 as

$$\epsilon_{po} = - \frac{N_{po}}{A_p E_p} \quad 3.53$$

where

N_{po} = Initial prestressing force, including friction loss, if any.

A_p = Cross-sectional area of the tendons.

E_p = Modulus of elasticity of the prestressing steel.

After transfer of the prestressing forces and throughout the life of the member the cable forces vary continually in time and along the length of the cable as well. To introduce this variational effect into the analysis a procedure has been devised so as to introduce the constant presence of the prestressing tendons into the mathematical formulation of the elements that model the member. In such a way any variation in the elements displacement field is automatically imposed upon the tendons, and vice-versa. The variable tendon force may be expressed as

$$N_p = E_p A_p (\epsilon_{pd} - \epsilon_{po}) \quad 3.54$$

where ϵ_{pd} is the current strain at the level of the prestressing steel due to effects other than prestressing.

By assuming that:

- i) the tendon profiles can be represented by their centroidal lines,
 - ii) tendons may be approximated as straight within the length of an element,
 - iii) the tendon force may be taken as constant within each element,
 - iv) complete bond exists between the tendons and the concrete,
- the following relations between displacements at the element nodal points and displacements at the extremities of the tendon can be drawn, according to Fig. 3.3.

$$u_{pi} = u_i - \theta_i y_{pi} \quad 3.55$$

$$w_{pi} = w_i, \quad i = 1, 2$$

The axial displacements of the cable, at points 1 and 2, may also be expressed in terms of the nodal displacements by

$$\Delta_i = (u_i - \theta_i y_{pi}) \cos \alpha - w_{pi} \sin \alpha \quad 3.56$$

The relationship between the tendon strains and the nodal displacements is

$$\epsilon_{pd} = \frac{1}{l_p} (\Delta_2 - \Delta_1) = (B_p) \{d\}, \quad l_p = l / \cos \alpha \quad 3.57$$

where

$$(B_p) = \frac{1}{l_p} \begin{Bmatrix} -\cos \alpha \\ \sin \alpha \\ y_{p1} \cos \alpha \\ \cos \alpha \\ -\sin \alpha \\ -y_{p2} \cos \alpha \end{Bmatrix}^T$$

According to Section 3.2.3, the vector of nodal forces due to

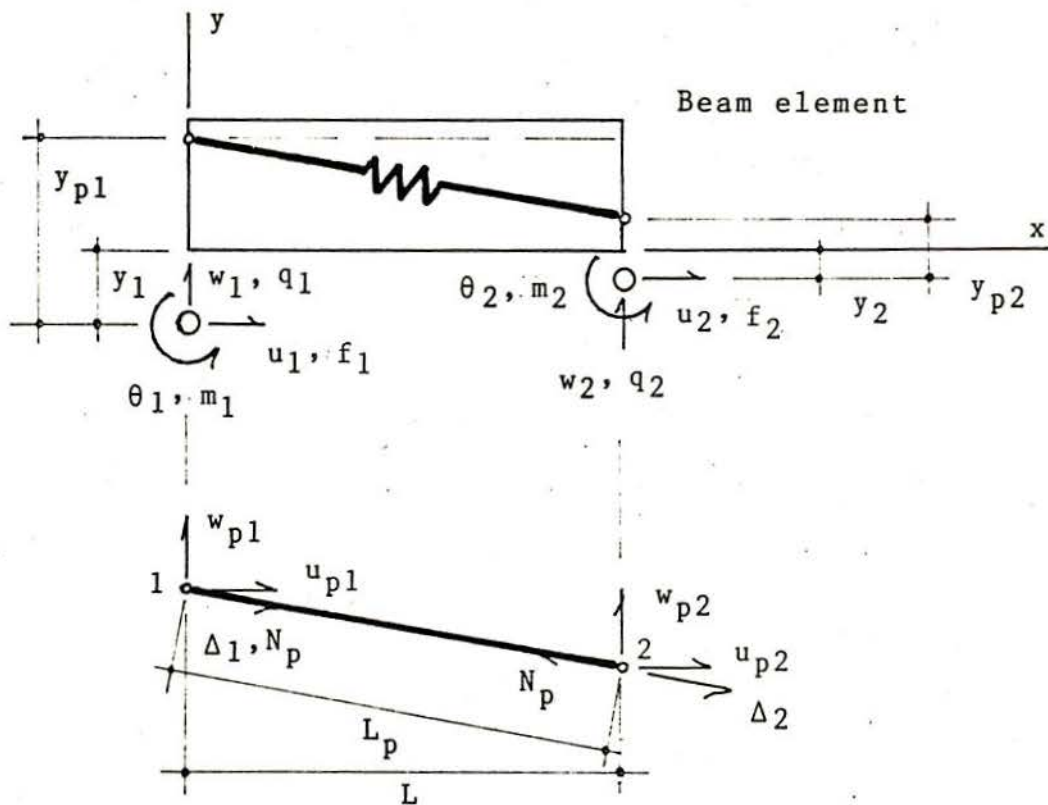


Fig 3.3 - Prestressing cable model.

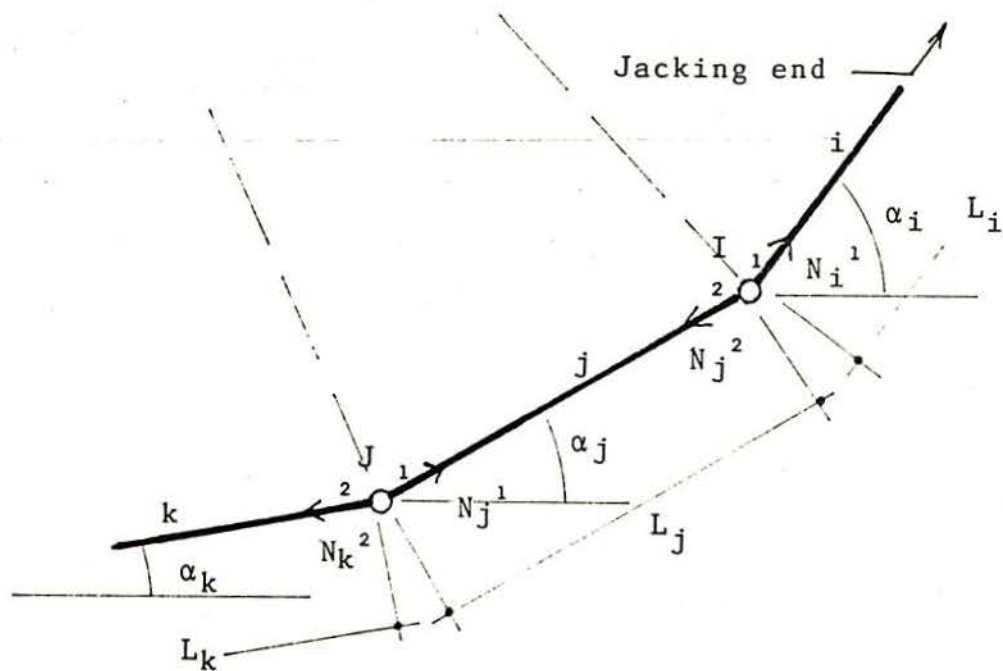


Fig 3.4 - Prestressing force variation due to friction.

$$[k_p] = \frac{E_p A_p}{L} = \begin{bmatrix} \cos^3 \alpha & -\sin \alpha \cos^2 \alpha & -y_{p1} \cos^3 \alpha & -\cos^3 \alpha & \sin \alpha \cos^2 \alpha & y_{p2} \cos^3 \alpha \\ \sin^2 \alpha \cos \alpha & y_{p1} \sin \alpha \cos^2 \alpha & \sin \alpha \cos^2 \alpha & -\sin^2 \alpha \cos \alpha & -y_{p2} \sin \alpha \cos^2 \alpha & \\ y_{p1}^2 \cos^3 \alpha & y_{p1} \cos^3 \alpha & -y_{p1} \sin \alpha \cos^2 \alpha & -y_{p1} y_{p2} \cos^3 \alpha & \\ \cos^3 \alpha & -\sin \alpha \cos^2 \alpha & -y_{p2} \cos^3 \alpha & \\ \sin^2 \alpha \cos \alpha & y_{p2} \sin \alpha \cos^2 \alpha & \\ y_{p2}^2 \cos^3 \alpha & \end{bmatrix}$$

prestressing may be expressed as

$$\{ f_p \} = \{ f_{pd} \} + \{ f_{po} \} = [k_p] \{ d \} \quad 3.58$$

where

$\{ f_{pd} \} =$ Nodal forces due to variation of the prestressing force N_p caused by deformation of the member.

$\{ f_{po} \} =$ Nodal forces due to initial prestressing force N_{po} and further losses from relaxation.

$$= \int_v (B_p)^T E_p \epsilon_{po} dv$$

$$= - l_p (B_p)^T N_{po}$$

$[k_p] =$ Stiffness matrix of the tendon as shown in page 74

$$= \int_v (B_p)^T E_p (B_p) dv$$

$$= A_p E_p l_p (B_p)^T (B_p)$$

Initially, the vector $\{ f_{po} \}$ is used to perform an analysis of the beam system to evaluate the initial strains $\{ \epsilon_{po} \}$ in the beam element. Subsequently, any changes in the value of N_p are automatically accounted for in the analyses of the assembled beam-prestressing tendon system. In pre-tensioned beams all analyses are performed by including the tendon stiffness matrix $[k_p]$ into the beam element stiffness matrix $[k]$. Therefore, losses due to elastic shortening in the member are obtained. On the other hand, in post-tensioned members the above mentioned stiffness matrices are superposed only after the first analysis has been performed, i.e. after the effects of initial prestressing have been obtained.

The post-tensioned tendons, due to the curvature of the profile and also due to out-of-plane deflection or wobble, present a variation of the prestressing force along its length, even before this force is transferred to the concrete member. This loss of the prestressing force, due to friction, is a function of the stress in the tendon, its profile, wobble and the coefficients of friction between the tendons and the surrounding materials.

The PCI Committee on Prestress Losses (23) recommends an expression to estimate the variation of the prestressing force, for a single end force, as follows:

$$N_{p1} = N_{p0} e^{-(\mu\phi + kx)} \quad 3.59$$

where

N_{p1} = steel force at a point

N_{p0} = steel force at the jacking end

e = base of the Neperian logarithm

μ = curvature friction coefficient

k = wobble friction coefficient

ϕ = total angular change of prestressing tendon profile, in radians, from jacking end to the point of interest

x = length along the prestressing tendon from jacking end to the point of interest

In the numerical solution, once the continuous cable profile is discretized into straight segments within the length of each element, the application of eq. 3.59 must be adapted for the calculation of the end forces applied at each nodal point. Referring to Fig. 3.4, assume a string of elemental cable segments, i , j and k , for which the jacking

end is positioned somewhere before segment i. And further assume that the change in the angular direction between two consecutive nodal points, I and J, can be expressed by the average of the changes of the angular directions at nodes I and J, weighted by the length of the adjacent elements as

$$\phi_j = \phi_{ij} \frac{l_j}{l_i + l_j} + \phi_{jk} \frac{l_j}{l_j + l_k} \quad 3.60$$

where

$$\phi_{ij} = | \alpha_i - \alpha_j |, \quad \phi_{jk} = | \alpha_j - \alpha_k | \quad 3.61$$

The prestressing force at the center of the element N_j can then be obtained as the average of the forces at the nodal points I and J, N_j^1 and N_j^2 respectively as

$$N_j = \frac{1}{2} (N_j^1 + N_j^2) = \frac{1}{2} N_j^2 [1 + e^{-(\mu \phi_j + k l_j)}] \quad 3.62$$

where N_j^2 has been previously obtained when calculating the force in element i, since equilibrium must be maintained at the nodes and consequently $N_j^2 = N_i^1$.

3.2.5 Temperature Effect

Bridges are usually exposed to the variable climatic conditions. Depending on its geographic location, temperature variation may be quite extensive not only due to seasonal changes but also within a daily cycle. Numerous random factors contribute to temperature distribution on a bridge, namely: the surrounding air temperature, the solar energy striking a surface, convection caused by the wind and various forms of

precipitations. As those conditions change continuously temperature distribution varies with position and time.

Hoffman, et al (80), studying temperature effects on a experimental segmental concrete bridge, have shown that the vertical temperature gradient among the cross-sections is highly nonlinear although little variation has been noticed in the longitudinal and transversal directions. This highly unpredictable phenomenon, according to some investigators (80,81,82), is somewhat neglected in today's design codes, though it is frequently the main cause of structural distress if inadequate provisions are considered in design. In jointless long span bridge construction this effect is of paramount importance.

In the present study thermal effects are analyzed considering a given temperature distribution over the composite cross-section, though stationary in time and nonvariable along the length of the member. A nonlinear temperature gradient is approximated by a bilinear variation as shown in Fig. 3.5, with the input values of the temperatures at top, deck-girder interface and bottom, T_1 , T_2 and T_3 respectively.

The inclusion of temperature effects in a finite element solution is straight forward and its formulation can be found in most books (76,77). Temperature variation at any given point ΔT induces a thermal strain ϵ_T , which may result in a stress-free strain or cause an additional stress, provided that free deformation is prevented. Assuming α as the coefficient of thermal expansion of the material, the final strains may be expressed as

$$\epsilon_T = \alpha \Delta T$$

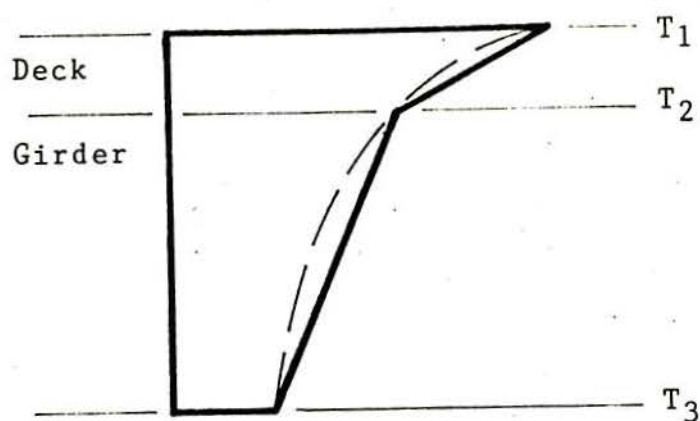


Fig 3.5 - Temperature variation in the cross-section.

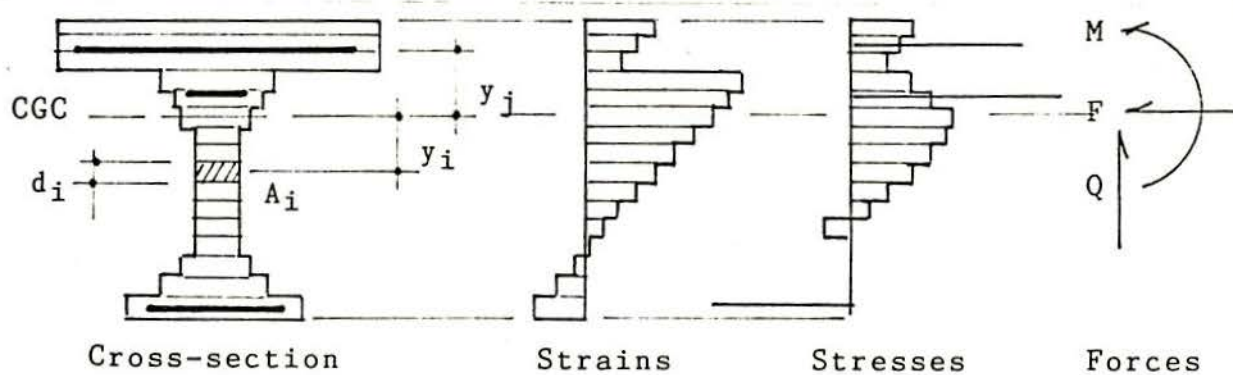


Fig 3.6 - Layered cross-section and stress and strain distributions.

These strains are treated as initial strains as described in Section 3.2.3.

3.2.6 Layered Section

To simplify the discussion, stiffness of the isoparametric beam element has been derived in Section 3.2.2 as if the element consists of one material having constant modulus of elasticity. In reality the beam cross-section consists of two distinct materials, concrete and steel. (Stiffness of the prestressing tendons has been evaluated separately in Section 3.2.4.) Further, the modulus of concrete may vary due to variation in stresses and strains along the y-direction within an element. To account for the variation in material and the modulus along depth, a numerical approach is used to perform integration on the section of an element. The element is divided into several layers, each consisting of one material. Further, depth of each layer is kept sufficiently small such that the stresses within the layer may be assumed constant. Therefore, each layer has a distinct modulus. According to Fig. 3.6, integrals in eq. 3.48 are then replaced by

$$\overline{EA} = \int E \, dA = \sum_i E_i A_i$$

$$\overline{ES} = \int E y \, dA = \sum_i E_i y_i A_i \quad 3.64$$

$$\overline{EI} = \int E y^2 \, dA = \sum_i E_i y_i^2 A_i$$

3.2.7 Coordinate Transformation

Beams rarely have their supports located at the level of their neutral axis, as commonly assumed in basic structural analysis. Supports are generally provided at the bottom face of the beams and some times even below the bottom flange, as in the case of steel rocker bearings. For accurately modeling the actual supporting conditions of a general beam the adopted elements have their nodes located at a variable position within the vertical planes containing their extreme sections, as shown in Fig. 3.2. The coefficients of the stiffness matrix in eq. 3.46 may be obtained by performing the necessary integrations with respect to the section neutral axis, to the bottom surface as shown in eq. 3.48 or to any other horizontal axis chosen. It is found reasonable to obtain the matrix $[k]$ with respect to the bottom surface of the element, as a general rule. Should the nodes be located at a variable position y from this surface a linear transformation is performed as shown below.

Assuming that $\{d\}$ are the displacements of a node positioned at the bottom surface of the element and $\{\bar{d}\}$ are the displacements of a point positioned at a general location y from this surface, the following relations can be drawn.

$$u = \bar{u} - y\bar{\theta}$$

$$w = \bar{w} \tag{3.65}$$

$$\theta = \bar{\theta}$$

or for the element

$$\begin{Bmatrix} u_1 \\ w_1 \\ \theta_1 \\ u_2 \\ w_2 \\ \theta_2 \end{Bmatrix} = \begin{bmatrix} 1 & 0 & -y_1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & -y_2 \\ 0 & 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{Bmatrix} \bar{u}_1 \\ \bar{w}_1 \\ \bar{\theta}_1 \\ \bar{u}_2 \\ \bar{w}_2 \\ \bar{\theta}_2 \end{Bmatrix} \quad 3.66$$

which leads to the definition of the transformation matrix $[A]$ as

$$\{d\} = [A] \{\bar{d}\} \quad 3.67$$

Using the principle of virtual work one can show that

$$\{\bar{f}\} = [A]^T \{f\} \quad 3.68$$

Regardless where the nodes are located the equilibrium equation can still be written as

$$\{f\} = [k] \{d\} \quad 3.69$$

or

$$\{f\} = [\bar{k}] \{\bar{d}\}$$

where $[\bar{k}]$ is the transformed element stiffness matrix for the case where the nodes are shifted to a general position away from the bottom surface. By substituting eqs. 3.67 and 3.68 into eq. 3.69, the new transformed element stiffness matrix is obtained as

$$[\bar{k}] = [A]^T [k] [A] \quad 3.70$$

where $[k]$ is the element stiffness matrix as defined in eq. 3.48 and $[A]$ is the transformation matrix defined in eq. 3.68.

3.2.8 Bearing Supports

Bearing supports are widely used in bridge beams, as explained in Section 2.4. In the present study bearing supports are modeled as uniaxial spring-like elements attached to the respective nodal points as shown in Fig. 3.2. As such, their axial stiffnesses $[k_b]$ are calculated with the procedure outlined in Section 2.4 and added to the corresponding degrees-of-freedom of the element stiffness matrix, as shown in the following section.

3.2.9 Element Equilibrium Equation

The elements formulated previously are subjected to nodal forces from the externally applied loading and due to initially prescribed strains. Displacements at the nodal points are related to these nodal forces through the following equilibrium equation.

$$\{ f \} + \{ f_o \} = [k_e] \{ d \} \quad 3.71$$

where

$\{ f \}$ = Vector of externally applied nodal forces.

$\{ f_o \}$ = Force vector generated from the initial strains due to prestressing, temperature variation and time-depended effects.

$[k_e]$ = Stiffness matrix of the composed element as shown in Fig. 3.2 obtained by superposition of the stiffness matrices of the isoparametric beam element, prestressing tendon and bearing supports, from eqs. 3.48 and 3.58 and Section 3.2.8 respectively.

$$[k_e] = [k] + [k_p] + [k_b]$$

3.3 Connection Element

A connection element is used to model the single deck connection between two adjacent girders or the deck connection to the end abutment, if any, when no joints are provided in these regions. These connections are very short in length when compared to the dimensions of the cross-section of the beam. They are found to vary in the range of 2 to 6 inches, whether a diaphragm is provided or a gap exists between the two girders (9,39). The deck has a very small moment of inertia when compared to that of the composite section, especially for the case of concrete girders. It seems reasonable to model the deck connection by a spring like element, which has only axial stiffness and is located at the centroidal line of the deck, away from the centroidal line of the composite section. Although the flexural stiffness of the deck is being disregarded at the connection, the predominant effect of the presence of the deck is accounted for by the rotational restriction provided by the spring, in its offset position from the centroid of the composite section.

The formulation of the connection element is remarkably simpler than the one presented for the beam element and is obtained as follows. Referring to Fig. 3.7, consider that u_1 , w_1 , θ_1 , and u_2 , w_2 , and θ_2 , are the displacements of the nodal points 1 and 2, respectively, which are shared by the connection element and the two adjacent beam elements. Consider also that u_1^* and u_2^* are the two horizontal displacements at the centroidal points A and B, at the opposite faces of

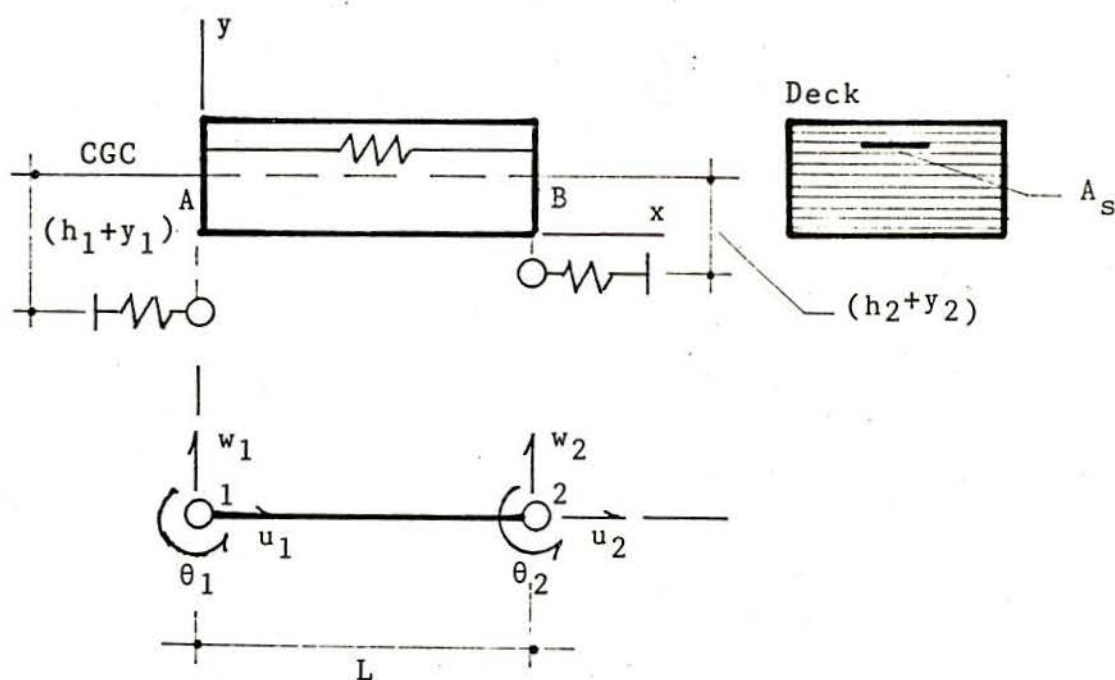


Fig 3.7 - Connection element.

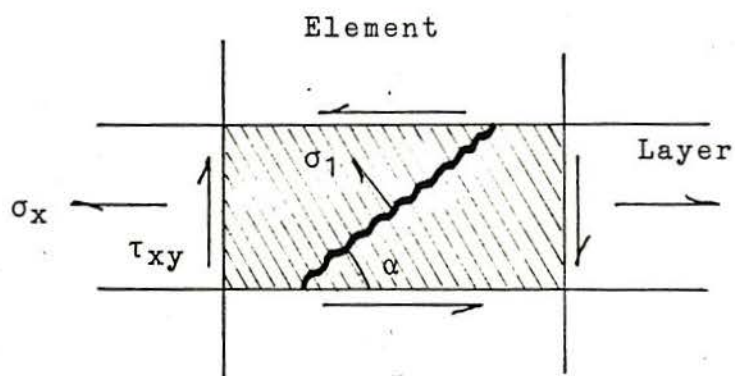


Fig 3.8 - Cracking stress and position.

the connection element. These two sets of displacements can be related to one another by the transformation matrix $[T]$ as

$$\begin{Bmatrix} u_1^* \\ u_2^* \end{Bmatrix} = \begin{bmatrix} 1 & 0 & -(h_1 + y_1) & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & -(h_2 + y_2) \end{bmatrix} \begin{Bmatrix} u_1 \\ w_1 \\ \theta_1 \\ u_2 \\ w_2 \\ \theta_2 \end{Bmatrix}$$

3.72

or

$$\{ d^* \} = [T] \{ d \}$$

The same transformation matrix can be used to relate the nodal forces $\{ f \}$ to the horizontal normal forces $\{ f^* \}$ applied at the centroidal points A and B as

$$\{ f \} = [T] \{ f^* \} \quad 3.73$$

The element equilibrium equation is written as

$$\{ f^* \} = [k_c^*] \{ d^* \} \quad 3.74$$

where the axial stiffness matrix $[k_c^*]$ is defined by

$$[k_c^*] = \frac{EA}{L} \begin{bmatrix} -1 & 0 \\ 0 & -1 \end{bmatrix} \quad 3.75$$

By equating 3.72, 3.73 and 3.74 the element equilibrium equation relating nodal forces and displacements is given by

$$\{ f \} = [k_c] \{ d \} \quad 3.76$$

where the matrix $[k_c]$ is obtained as

$$[k_c] = [T]^T [k_c^*] [T] \quad 3.77$$

As for the beam element the contribution of the bearing stiffness $[k_b]$ at the nodal points is considered by superposing this value to the element stiffness matrix. The final connection element stiffness matrix can be written as

$$[k_c] = \begin{bmatrix} \frac{EA}{L} + k_b & 0 & -\frac{EA}{L}(h_1+y_1) & -\frac{EA}{L} & 0 & \frac{EA}{L}(h_2+y_2) \\ 0 & 0 & 0 & 0 & 0 & 0 \\ \frac{EA}{L}(h_1+y_1)^2 & \frac{EA}{L}(h_1+y_1) & 0 & -\frac{EA}{L}(h_1+y_1)x & & \\ & & & & & (h_2+y_2) \\ \frac{EA}{L} + k_b & 0 & -\frac{EA}{L}(h_2+y_2) & & & \\ 0 & 0 & & & & \\ \text{symmetric} & & & & & \frac{EA}{L}(h_2+y_2)^2 \end{bmatrix}$$

3.78

where

EA = Axial stiffness of the element considering concrete and steel reinforcements.

h_1, h_2 = Distance from the CGC of the deck section to the bottom

surface of the adjacent beam elements, at nodes 1 and 2.

y_1, y_2 = Distances from the nodal points 1 and 2 to the bottom surface of the adjacent elements.

3.4 Global Problem

Using the finite elements formulated in previous sections a member is modeled as several discrete elements connecting end-to-end at nodal points. It is idealized as a straight line passing through these nodal points, each of which having three degrees-of-freedom. The global stiffness matrix of the system is obtained by appropriate assembly of the stiffness matrices of the individual beam elements as shown in eq. 3.70, and connection elements if any, as shown in eq. 3.78. Both elements share a single nodal point and therefore their stiffness matrices are superposed at the common degrees-of-freedom.

The elements are used to represent material and cross-section properties of the member. Loads and restraints in any of the three directions are lumped and applied only at the nodal points. The global equilibrium equation of the system is written as

$$\{ F \} + \{ F_0 \} = [K] [D] \quad 3.79$$

where

F = Assembled vector of applied loads.

F_0 = Force vector generated from initial strains.

$[K]$ = Global stiffness matrix.

D = Vector of nodal displacements.

Under the action of loads, a solution for displacements is performed. Displacements are used for the calculation of strains and, in turn, for obtaining stresses. Element resisting forces, obtained by integrating stresses over the cross-section are eventually transformed back into nodal forces to seek equilibrium of the system. Moments, axial and shear forces are constant within the length of each element and thus their distributions along the length of the member are linearly approximated. The more elements are used for modeling the member, the more accurate is the approximation. Reactions are calculated at the nodal supports and correspond to the resisting forces shared by the elements connected at these nodal points.

Response analysis of a member may include both linear and nonlinear ranges of behavior. Nonlinearity is introduced by the assumed nonlinear properties of the materials as well as due to cracking of the sections as explained in following section. The solution for displacements is performed by an incremental method using the tangent stiffness matrix of the system, either by increments of load or displacement as described in Section 3.8. Time-dependent response analysis is discussed in Section 3.9.

3.5 Loading

A structural member behaves according to the imposed loading and constraints. In the case of composite precast construction these loadings and constraints are very well defined qualitatively, quantitatively, and in time. A numerical analysis, therefore, has to properly model each and all of these conditions in sequence and carrying

the current state of the member from one loading stage to the next. In this study, the following seven different loadings are considered

- Prestressing
- Girders Dead Load
- Deck Dead Load
- Live Loads
- Support Displacements
- Temperature
- Time-Dependent Effects

Each of the above loadings is applied upon the structure at a predefined time or time interval and subdivided into a specified number of steps whether of load, displacement or time. Prestressing and temperature are applied as equivalent nodal loads as explained in sections 3.2.4 and 3.2.5 respectively. Support displacements will be discussed in Section 3.6 and time-dependent effects in Section 3.9.

Dead loads are linearly distributed along the member and are divided into two categories: girder dead load and deck dead load. The latter includes not only the weight of the deck slab but also of any permanent component like diaphragms, wearing course, cubs and rails, etc. Both dead loads, often applied at different ages of the structure, are modeled as equivalent nodal loads.

Live loads represent any non permanent external action applied to the members due to traffic, wind, earthquakes, etc. Here, however, only vertically and statically applied loads are assumed. Live loads are usually concentrated or distributed within limited regions. In this study the inclusion of any distributed or concentrated live load is

accepted. In the analysis, however, they are also modeled by equivalent nodal loads. Within the solution, the response under the action of such loads may be obtained by using the Method of Load Increments as well as by using the Displacement Increment Method, both described in following sections.

In many structural analyses, it is essential to evaluate the strength of a member, i.e. the member response to the ultimate load level. The Displacement Increment Method is suitable for the purpose, according to the reasons mentioned in Sections 3.8.1 and 3.8.2. Appendices A and C show in more detail how to input live and dead loads into the program.

3.6 Support Displacements

Structures are often very sensitive to support displacements. A simple beam would rarely be affected by any small prescribed displacement at the supports. A continuous beam, however, may drastically change its response behavior should its supporting conditions be altered. Vertical displacements at a support of a beam may occur due to a settlement of the supporting structure or an intentional adjustment of one or more of the supporting points.

Two different procedures have been commonly used for the solution of a structural systems under support displacements, and they are briefly outlined as follows. Consider the equilibrium equation of a system, as shown in eq. 3.80, for which some of the degrees-of-freedom have prescribed displacements $\{D_1\}$. Then the remaining displacements $\{D_2\}$

and the nodal loads associated with the prescribed degrees-of-freedom $\{F_2\}$ are unknowns. The system stiffness matrix is then partitioned accordingly as

$$\begin{bmatrix} [K_{11}] & [K_{12}] \\ [K_{21}] & [K_{22}] \end{bmatrix} \begin{Bmatrix} \{D_1\} \\ \{D_2\} \end{Bmatrix} = \begin{Bmatrix} \{F_1\} \\ \{F_2\} \end{Bmatrix} \quad 3.80$$

and the unknown displacements and loads can be obtained by solving the following set of equations, respectively.

$$[K_{22}] \{D_2\} = \{F_2\} - [K_{21}] \{D_1\} \quad 3.81$$

and

$$\{F_1\} = [K_{11}] \{D_1\} + [K_{12}] \{D_2\}$$

The above procedure, though mathematically correct, increases enormously the computational work involved in solving the system. Not only the stiffness matrix has to be partitioned, as in eq. 3.80, but also there is one more set of multiplications to be performed, as in eq. 3.81, a process that might be repeated numerous times for a nonlinear system. However, a more economical and as precise procedure may be used to solve the same problem, regarding the level of accuracy of the problem studied and acknowledging the possibility of numerical weaknesses.

Assume, for convenience of illustration, the same structural system solved by the above procedure, for which one or more degrees-of-freedom have prescribed displacements, D_i, D_j, \dots , where i, j, \dots , represent supporting nodal points. Eq. 3.80 may be written as

$$\begin{bmatrix} \dots & & \\ & K_{ii} & \\ & & \dots \\ & & & K_{jj} & \\ & & & & \dots \end{bmatrix} \begin{Bmatrix} \dots \\ D_i \\ \dots \\ D_j \\ \dots \end{Bmatrix} = \begin{Bmatrix} \dots \\ F_i \\ \dots \\ F_j \\ \dots \end{Bmatrix} \quad 3.82$$

Where the stiffness matrix $[K]$ does not need to be partitioned and is used as for the solution of any other loading condition. Furthermore, assume that the coefficients of the stiffness matrix, K_{ii} , K_{jj} , ..., are altered so that they become extremely greater than the other coefficients of the same lines of the matrix, i.e. the remaining coefficients of the equilibrium equations of the nodes in question as

$$K_{ii} = \beta K_{ii}, \quad i = 1, 2 \quad 3.83$$

where β is a convenient large number as 10^{12} for instance, and in the load vector $\{F\}$ the corresponding elements, F_{ii} , F_{jj} , ..., are also altered accordingly so that

$$F_i = \beta K_{ii} D_i, \quad i = 1, 2 \quad 3.84$$

Then, the system of equations 3.82 may be usually solved by any process being employed in the numerical procedure and applied to the remaining loading cases. This procedure, which is more economical than the one described previously has been successfully used by some investigators (83) and is applied in this study.

3.7 Cracking Model

In the analysis of concrete structures the low tensile strength of concrete and the ensuing cracking that results therefrom is of paramount importance. Cracking effect in finite element analysis of reinforced concrete structures was first introduced by Ngo and Scordelis (29) through the use of a predefined discrete crack system. Nilson (30) proposed a model for progressive crack propagation by separating elements at each side of a node and, consequently, having to deal with a continuous change in the topology of the mathematical model.

A second approach was later introduced by Rashid (84) who in studying the behavior of prestressed concrete pressure vessels, proposed the so-called smeared cracking model. In such a model, rather than representing a single crack, many finely spaced cracks perpendicular to the principal strain direction are assumed to occur. This approach has been used by a majority of investigators (33) who acknowledged its main features of permitting an automatic generation of cracks without the redefinition of the finite element topology and the complete generality in possible crack directions.

In the present study, regarding the class of structures analyzed and the type of analysis proposed, the smeared cracking model has been adopted due to its proven efficiency and easy application. Cracking is considered through a strain criteria. It is assumed to happen when the principal strain at a point ϵ_1 reaches the concrete rupture strain ϵ_r . Cracks are expected to be oriented perpendicularly to the direction of the principal stress as shown in Fig. 3.8. Considering that normal strains in the vertical direction are disregarded in the formulation

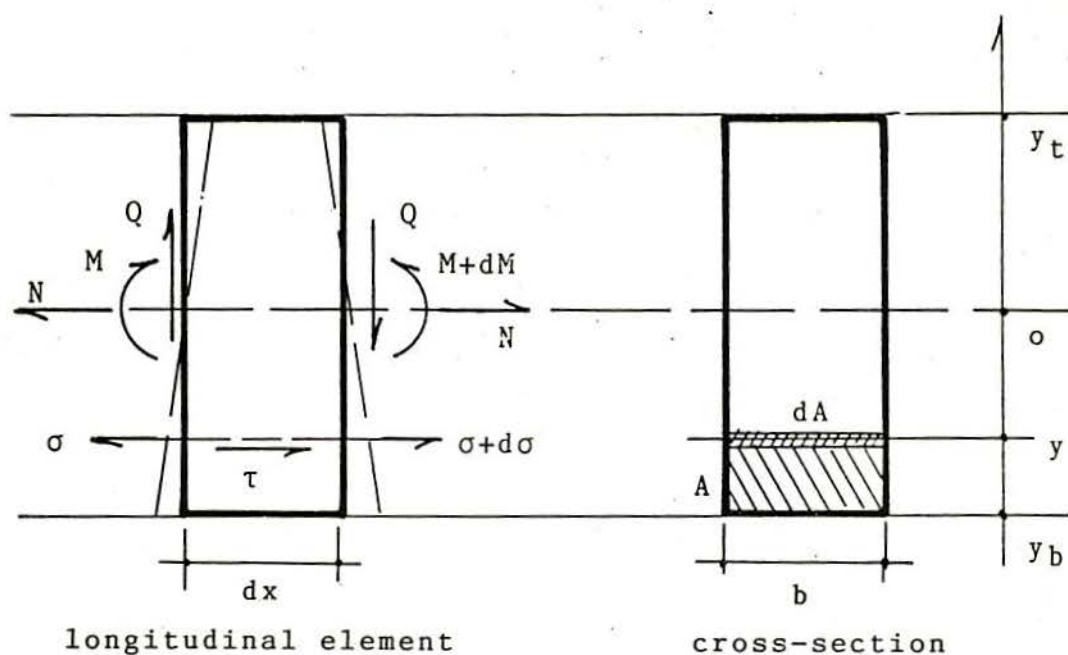


Fig 3.9 - Stress distributions on the cross-section.

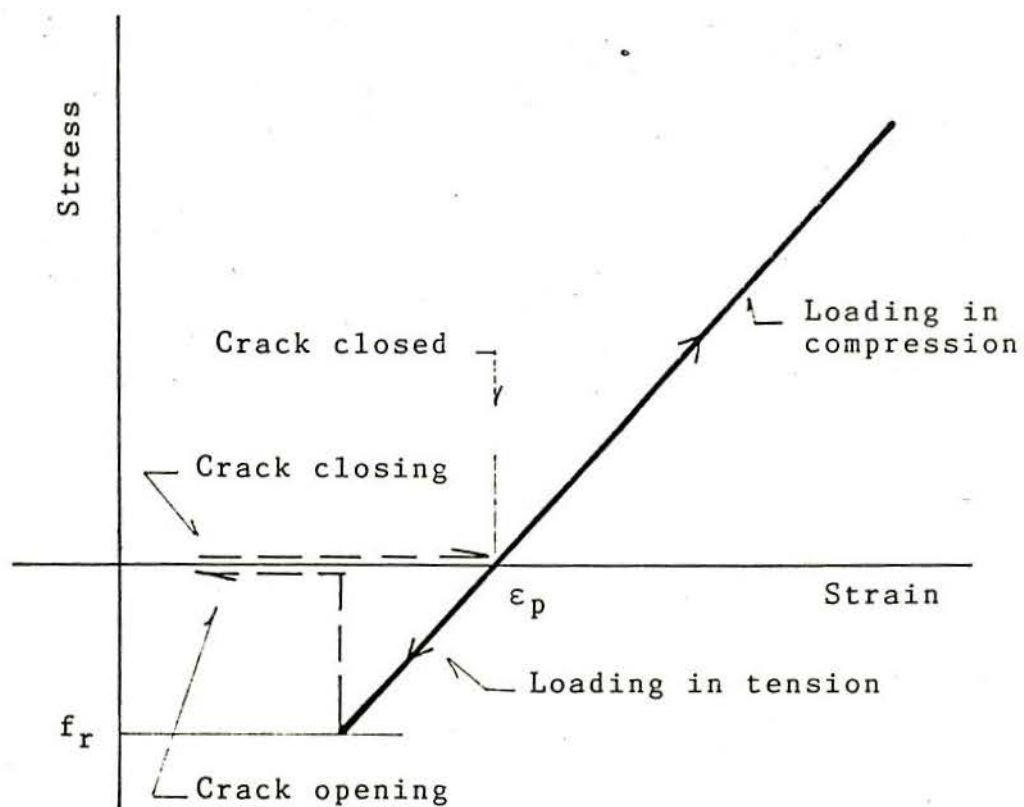


Fig 3.10 - Crack formation and closing.

of the element, as explained in Sections 3.2.1 and 3.2.2, the principal strain at a point may be obtained as

$$\epsilon_1 = \frac{1}{2} [\epsilon_x + (\epsilon_x^2 + \gamma_{xy})^{1/2}], \quad \epsilon_x = \frac{\sigma_x}{E}, \quad \gamma_{xy} = \frac{\tau_{xy}}{G} \quad 3.85$$

and its orientation α by

$$\alpha = \frac{1}{2} \tan^{-1} \left(\frac{\gamma_{xy}}{\epsilon_x} \right) \quad 3.86$$

where ϵ_x and γ_{xy} are the normal strain in the axial direction and the shear strain, respectively. From eq. 3.37 and 3.38 it is observed that the normal strain ϵ_x varies linearly through the depth of the element whereas the shear strain γ_{xy} is constant. The assumption of constant γ_{xy} in the element cross-section is reasonable for modeling the global behavior of the member under a bending mode of deformation. However, shear strains do vary along the depth of the beam, according to the distributions of shear stresses and material properties.

The local distribution of shear stresses may be obtained by equating the equilibrium of an infinitesimal beam element as shown in Fig. 3.9. At a general position y from the section neutral axis the normal strain developed under the applied forces may be written as

$$\epsilon_x = \frac{N}{EA} + \frac{M}{EI} y = \epsilon_{x0} + \kappa y = \begin{pmatrix} 1 & y \end{pmatrix} \begin{Bmatrix} \epsilon_{x0} \\ \kappa \end{Bmatrix} \quad 3.87$$

and the corresponding normal stress as

$$\begin{aligned} \sigma_x &= E \epsilon_{x0} + E \kappa y \\ &= E \begin{pmatrix} 1 & y \end{pmatrix} \begin{Bmatrix} \epsilon_{x0} \\ \kappa \end{Bmatrix} \end{aligned} \quad 3.88$$

The axial force N and bending moment M may be obtained by integrating the above stresses as

$$\begin{aligned} N &= \int_{y_b}^{y_t} \sigma_x dA = \epsilon_{x0} \overline{EA} + x \overline{ES} \\ M &= - \int_{y_b}^{y_t} \sigma_x y dA = - \epsilon_{x0} \overline{ES} - x \overline{EI} \end{aligned} \quad 3.89$$

where

$$\overline{EA} = \int_{y_b}^{y_t} E dA, \quad \overline{ES} = \int_{y_b}^{y_t} E y dA \quad \text{and} \quad \overline{EI} = \int_{y_b}^{y_t} E y^2 dA \quad 3.90$$

Equation 3.89 may also be written in matrix form as

$$\begin{Bmatrix} N \\ M \end{Bmatrix} = \begin{bmatrix} \overline{EA} & \overline{ES} \\ -\overline{ES} & -\overline{EI} \end{bmatrix} \begin{Bmatrix} \epsilon_{x0} \\ x \end{Bmatrix} \quad 3.91$$

or

$$\begin{Bmatrix} \epsilon_{x0} \\ x \end{Bmatrix} = \frac{1}{\overline{ES}^2 - \overline{EA} \overline{EI}} \begin{bmatrix} -\overline{EI} & -\overline{ES} \\ \overline{ES} & \overline{EA} \end{bmatrix} \begin{Bmatrix} N \\ M \end{Bmatrix} \quad 3.92$$

Substituting eq. 3.92 into eq. 3.88 and proceeding with a matrix multiplication, the normal stress may be written as

$$\sigma_x = \frac{E}{\overline{ES}^2 - \overline{EA} \overline{EI}} [(-\overline{EI} + \overline{ES} y) N + (-\overline{ES} + \overline{EA} y) M] \quad 3.93$$

According to Fig. 3.9 the equilibrium between normal and tangential stresses may be equated as

$$\tau_{xy} b dx = - \int_{y_b}^y d\sigma_x dA \quad 3.94$$

and therefore the shear stress is given by

$$\tau_{xy} = -\frac{1}{b} \int_{y_b}^y \frac{d\sigma_x}{dx} dA \quad 3.95$$

By assuming the reference axis y for the integrals in eq. 3.90 as the section centroidal axis as shown in Fig. 3.9, $ES = 0$. Taking the derivative of eq. 3.93 and substituting into eq. 3.95 the shear strain is obtained as

$$\tau_{xy} = \frac{1}{b} \int_{y_b}^y \left(\frac{E}{EA EI} \right) \left(-EI \frac{dN}{dx} + EA y \frac{dM}{dx} \right) dA \quad 3.96$$

Normal force N is constant through the element and the variation of the bending moment M with x is represented by the total shear force Q . The integration in eq. 3.96 leads to eq. 3.97 and using the expression in eq. 3.90 becomes

$$\tau_{xy} = \frac{Q}{b} \left(\frac{ES y}{EI} \right) \quad 3.97$$

Should material properties E be constant through the depth, eq. 3.97 would become the common expression for the distribution of shear stresses

$$\tau_{xy} = \frac{QS}{bI} \quad 3.98$$

where S stands for the first moment of area of the area A in Fig. 3.9 and I stands for the moment of inertia of the section. Both S and I are calculated with respect to the centroidal axis of the section. The above expression generally leads to a parabolic shear stress distribution. In the present study, material properties do vary throughout the sections as a consequence of the nonlinear stress-strain relationships assumed

for the materials. Therefore, the shear stress and consequent shear strain distributions must be obtained from eq. 3.97, where the quantities $\bar{E}S_y$ and $\bar{E}I$ carry the effects of material nonlinearity. For computing the principal strain at a general point or layer, as in eq. 3.85, the shear strain γ_{xy} is then obtained as

$$\gamma_{xy} = \frac{\tau_{xy}}{G} = \frac{Q}{bG} \left(\frac{\bar{E}S_y}{\bar{E}I} \right) \quad 3.99$$

where G is the shear modulus of the material at the point of interest, taken as $G = E/2(1+\nu)$.

The above procedure accounts for the variation of the material properties not only with the different materials that may comprise the beam but also within the same material. Once a crack is formed one or more layers of an element are considered cracked, their axial stiffnesses are disregarded by setting the modulus of elasticity to zero. The analysis then proceeds and crack propagation is obtained by applying the same procedure to the consecutive layers.

In a structural member, however, even when monotonic loading is applied it is possible for some stress redistribution to take place causing some regions of the member to unload. This phenomenon may be due to intrinsic nonlinear stress-strain characteristics of the materials, or the cracking process, or the time-dependent effects that exist, and may cause some cracks to close. If that should happen a strain quantity ϵ_p is observed, see Fig. 3.10, and crack closing is obtained whenever this value is surpassed when concrete is able to pick up compressive stress normal to the closed crack.

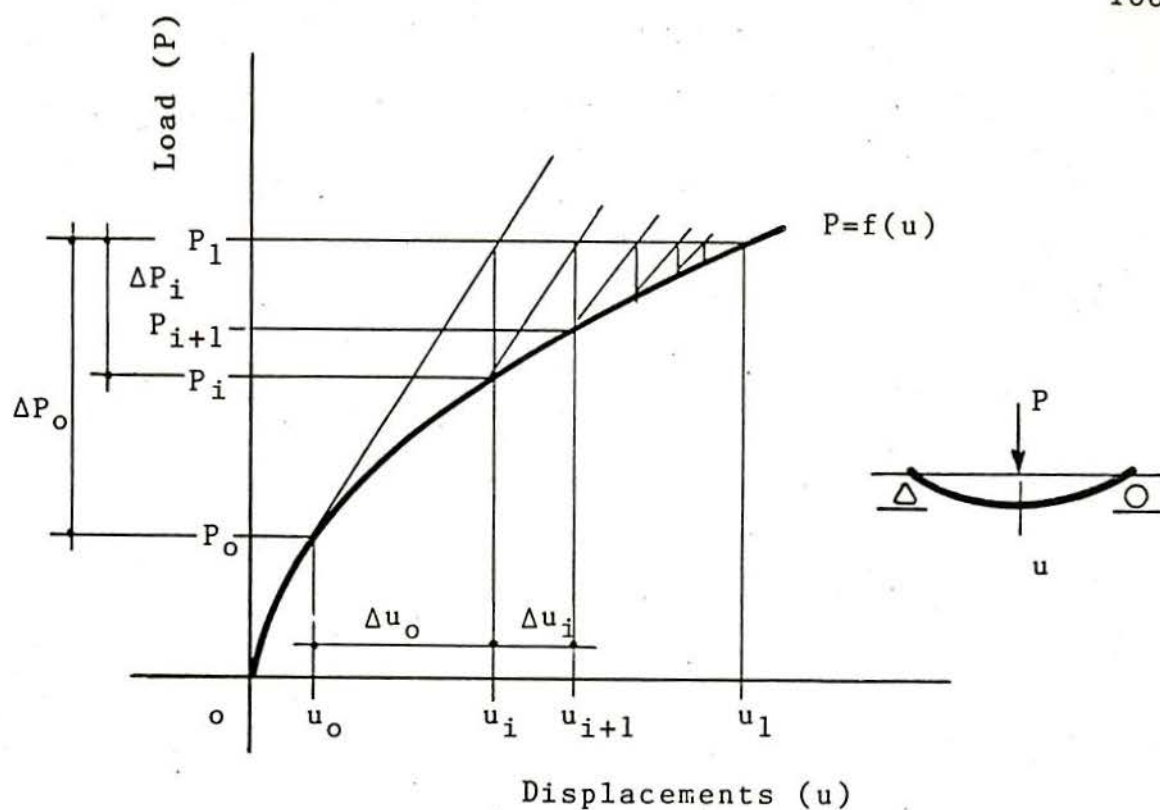
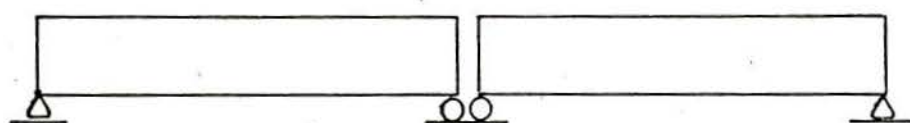
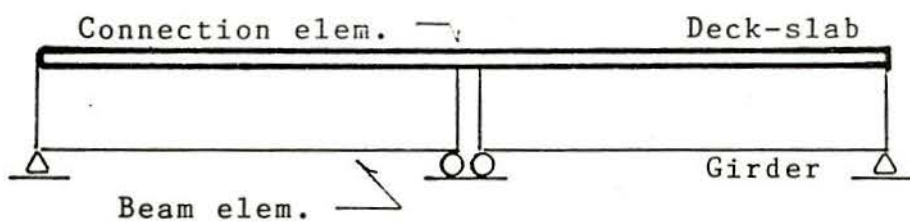


Fig 3.11 - Load Increment Method.



PRECAST GIRDERS - SIMPLY SUPPORTED

PRECAST GIRDERS AND CAST-IN-PLACE
DECK-SLAB - COMPOSITE BEAMFig 3.12 - Sequence of construction of a
two-span composite beam.

3.8 Nonlinear Analysis

3.8.1 The Load Increment Method

The Load Increment Method for nonlinear analysis uses an iterative procedure in which the loads applied to the system are successively corrected until an equilibrium position is obtained. It is a variation of the direct stiffness technique where the incremental stiffness matrix based on the current position of the system is used, instead of a constant stiffness matrix, and equivalent to the modified Newton-Raphson Method.

For illustration of the method, consider a single degree-of-freedom system as shown in Fig. 3.11. Assume that the load-deformation relationship of the system can be represented by the function

$$P = f(u) \quad 3.100$$

and further assume that the current state of the system is at the load level p and at the deformation u_0 . It is required to determine the deformation at the new load level p_1 , u_1 . A new step starts with a predefined load increment ΔP_0 . By assuming that the load deformation relationship is linear at that deformation level and, therefore, using the tangent stiffness at that level as the stiffness of the system a deformation increment is calculated as Δu_0 . The current deformed state is then obtained as

$$u_i = u_0 + \Delta u_0 \quad 3.101$$

and the resisting internal forces at this deformation level as

$$P_i = f(u_i) \quad 3.102$$

For a nonlinear system p_i will rarely be equal to p_1 and the difference

$$\Delta P_i = P_1 - P_i \quad 3.103$$

is the equilibrium error or residual load vector. The residual vector is then compared with the specified tolerance limit. If this limit is exceeded the residual load vector is used as the additional load applied to the system, at the trial deformation level of u_i . This process is repeated until the equilibrium error is within the specified limits. The solution is then assumed to be converged for the load level p_1 . The same process is followed for the next load step, if any, when the tangent stiffness matrix is updated. The solution will then converge when an equilibrium state of the system, under the applied load, is obtained.

Under some circumstances such as the case where the new load level exceeds the maximum capacity of the system, or the new load is less than the capacity but with some unusual shape of the load-deformation relationship, the solution may diverge. An unusual shape of the load-deformation relationship in the case of structural members may be the nearly horizontal plateau observed at the level of their maximum capacity.

3.8.2 The Displacement Increment Method

The nonlinear response of a structural member, within some limiting points, can be predicted by using various numerical techniques like the Newton-Raphson Method and its modified version, the Incremental Stiffness Method, the first and second order Self Correcting Method,

etc. When these methods are used in terms of the incremental load vectors convergence may become difficult to achieve, whenever the sought track has some particular shape as mentioned in the previous section. In the analysis of concrete structures the load-deflection curves may frequently present sudden drops due to instantaneous reduction in stiffness, as a consequence of cracks. They are also frequently characterized by possessing a flat plateau which may follow large increments in displacements, an important phenomenon for the measure of ductility. The displacement increment technique, however, has proven very effective in capturing the complete load-deformation curve including these particular drops and plateau. A few different versions of the method are found in the literature (85,86,87) and some investigators have reported using it with satisfactory results (88).

For illustration purpose, assume the equilibrium equation of a structural system relating displacements and applied loads as

$$[K] \{D\} = \{F\} \quad 3.104$$

If an incremental procedure is adopted, eq. 3.104 may be written as

$$[K] \{\Delta D\} = \Delta\alpha \{F\} \quad 3.105$$

where $[K]$ is in general a symmetric banded matrix of order n , here taken as the tangent matrix evaluated at the beginning of a new step, $\{\Delta D\}$ is the vector of n unknown displacements, $\{F\}$ the known load vector with n components and $\Delta\alpha$ an unknown factor applied to the load vector.

For applying the Displacement Increment Method to the system in question a single degree-of-freedom is conveniently chosen. A specified displacement ΔD_2 is incrementally applied to the nodal point until the

system reaches equilibrium at a desired load level. The displacement vector in eq. 3.105 may then be partitioned into two components, where $\{\Delta D_1\}$ is the unknown incremental displacement vector for the remaining degrees-of-freedom of the system, as in eq. 3.106. The stiffness matrix of the system and the applied load vector from eq. 3.105 may then be partitioned accordingly

$$\begin{bmatrix} [K_{11}] & \{K_{12}\} \\ (K_{21}) & K_{22} \end{bmatrix} \begin{Bmatrix} \{\Delta D_1\} \\ \Delta D_2 \end{Bmatrix} = \Delta\alpha \begin{Bmatrix} \{F_1\} \\ F_2 \end{Bmatrix} \quad 3.106$$

Eq. 3.106 can also be written as

$$[K_{11}] \{\Delta D_1\} = \Delta\alpha \{F_1\} - \{K_{12}\} \Delta D_2 \quad 3.107$$

$$(K_{21}) \{\Delta D_1\} = \Delta\alpha F_2 - K_{22} \Delta D_2 \quad 3.108$$

A direct method of solving eqs. 3.107 and 3.108 would lead to the use of a non-symmetric matrix, which is not very effective. Nevertheless, by further partitioning the unknown displacement vector as

$$\{\Delta D_1\} = \Delta\alpha \{\Delta D_1\}^0 + \{\Delta D_1\}^1 \quad 3.109$$

eq. 3.107 can be solved in two simple steps as

$$[K_{11}] \{\Delta D_1\}^0 = \{F_1\} \quad 3.110$$

and

$$[K_{11}] \{\Delta D_1\}^1 = -\{K_{12}\} \Delta D_2 \quad 3.111$$

where the matrix $[K_{11}]$, already rearranged for the solution procedure in eq. 3.110 is also used in the subsequent equation, saving some computational effort in repeating the process.

The unknown factor $\Delta\alpha$ can then be obtained by equating 3.109, 3.110 and 3.111 as

$$\Delta\alpha = \frac{(K_{21}) \{ \Delta D_1 \}^1 - K_{22} \Delta D_2}{F_2 - (K_{21}) \{ \Delta D_1 \}^0} \quad 3.112$$

At this point, equilibrium of the system should be checked as observed for the Load Increment Method. The resisting load vector can be obtained from the current deformed state of the system and, if equilibrium is not achieved, further corrections in the displacement vector should be made. The process followed to this point is the first iteration of a step. For the second and subsequent iterations $\{\Delta D_2\} = 0$ and in its place there is a residual load vector $\{\Delta F_1\}$ and eq. 3.107 and 3.108 may be written as

$$[K_{11}] \{ \Delta D_1 \} = \Delta\alpha \{ F_1 \} + \{ \Delta F_1 \} \quad 3.113$$

and

$$(K_{21}) \{ \Delta D_1 \} = \Delta\alpha F_2 + \Delta F_2 \quad 3.114$$

The solution of the above equations, similar to that for eqs. 3.110 and 3.111, can be expressed as

$$[K_{11}] \{ \Delta D_1 \}^0 = \{ F_1 \} \quad 3.115$$

and

$$[K_{11}] \{ \Delta D_1 \}^1 = \{ \Delta F_1 \} \quad 3.116$$

where once more the same matrix $[K_{11}]$ is used. $[K_{11}]$ needs to be updated only at the beginning of a new incremental step, if any. Eq. 3.112 is now replaced by

$$\Delta\alpha = \frac{(K_{21}) \{ \Delta D_1 \}^1 - \Delta F_2}{F_2 - (K_{21}) \{ \Delta D_1 \}^0} \quad 3.117$$

For each iteration the current load vector is obtained as $(\Sigma\Delta\alpha)$ $\{F\}$, where the $\Delta\alpha$'s are to be added for all the previous iterations and steps. Until the residual load vector is sufficiently small when convergence is obtained, the iterations are to be continued.

3.9 Time-Dependent Response Analysis

Section 3.8 describes the procedures utilized for obtaining the instantaneous response of a general composite bridge beam. Concrete members, however, when loaded at different ages may respond quite differently due to the highly nonlinear time-dependent properties of the materials involved, such as creep, shrinkage and aging of concrete, and relaxation of prestressing steel.

Creep is defined as the time-dependent deformations of concrete which is the function of stress levels and the time at which the stresses are applied. Shrinkage represents the time-dependent deformation of concrete that is independent of stress levels and a function of time only. Relaxation is defined as the time-dependent stress decrements of steel under constant strain. The aging of concrete is reflected in the change of the stress-strain curve of the material with time. The stress-strain curve intrinsic shape is assumed to be the same but stresses at a same strain level will be a function of time, as outlined in Section 2.1.3.4.

Time-dependent response analysis may be obtained by subdividing the interval of time under consideration into several small time increments, within which the previously described instantaneous solution is used. In each time increment, or step, it is assumed that material properties and the response of each fiber of the beam follow the functions of time and stress level history up to the start of the time increment. The equilibrium position of the member can be found and is used as the basis for the analysis of the response in the next time step. Starting from the beginning of the time interval the whole range of the time-dependent response can be captured.

Time at which loads are applied is also considered. Loads may be applied any time after the erection time of the beam and they will be accumulated. Some portions of the cross-section of the member may be added later, i.e. the composite beam action is taken into account as described in the following section. External support restraints are generally independent of time and applied at the beginning of the solution. However, as seen in Chapter 5, some changes in the supporting conditions can be accommodated within the solution.

As previously mentioned, in determining the instantaneous response of a beam, the beam is subdivided into several elements connected end-to-end at nodal points. Each of the elements is further subdivided vertically into layers. A layer is able to carry strains, observed at their centroids, assumed constant throughout their length and cross-section. Loads and restraints are discretized and applied only at the nodal points.

For the time-dependent response analysis it is assumed that the strain in each layer consists of time-dependent strain parts in addition to instantaneous strain parts. Time dependent strains of concrete consist of shrinkage strains and creep strains, and those of prestressing steel are relaxation strains. Shrinkage strains are the function of time alone thus they can be found immediately at any given time increment, assuming the shrinkage function described in Section 3.1.3.3. Creep strains under constant stress may be represented by creep functions. For creep under variable stress, as in a beam, two methods of predicting creep strains under variable stresses may be used. The methods, outlined in Section 2.1.3.2, are the Rate of Creep Method and the Superposition Method. The Rate of Creep Method uses the strain at the beginning of the time increment as the basis for finding the creep increment strain. For the Superposition Method the stress history up to the current time step is used in the calculation. Relaxation strains are treated the same way as the creep strains. But, instead of determining the creep strains, relaxation stresses are calculated from the stress history and only a method similar to the rate of creep method is used. A method similar to the superposition method is invalid since relaxation is not a linear function of stress level.

The so obtained time-dependent strains at any incremental time step are then related to stresses and eventually transformed into nodal forces. The load vector is subsequently applied to the model and an age-corrected instantaneous solution is performed, seeking the current equilibrium position of the member as in the procedure detailed in Section 3.8.1. This process is repeatedly applied for each increment of time and the time-dependent response of the member is obtained.

3.10 Composite Beam Action

Bridge beams are usually constructed as composite beams (9,10,18,39,89,90) where the girders are of precast concrete or steel and the deck slab is cast-in-place on top of the girders at some later date as shown in Fig. 3.12. At the time of casting the deck slab the beams may be shored, i.e. the precast girders do not carry slab loads at the time of casting, or unshored, that is the precast girders carry slab and formwork loads at the time of casting of the slab. After the slab has gained sufficient strength, forming the composite beam, both act together under the additional loads.

For assuring perfect bond between the girders and the deck slab shear connectors are often provided at that interface (10,91). Experimental data show that adequate composite action is obtained when those connections are properly designed (11,92).

In this analysis the following technique is used for modeling the composite behavior at some specified age of the member. As described before, the stiffnesses of the elements are obtained by integrating the individual stiffnesses of the various layers that compose each element. When any new loading is applied, a companion variable ICOMP is assigned a value 0 or 1, indicating that the stiffness integration should be performed within the girder section or extended to the deck portion, respectively. In the early phases of the construction, before the deck is cast, the beam elements represent the behavior of the girders alone. Under the action of deck dead load the variable ICOMP may have its value set to 1 or 0 representing shored or unshored construction, respectively. After the deck has attained enough strength and

additional loading is applied, ICOMP remains equal to 1. Composite action is then obtained and the connection elements, if any, link the various spans.

3.11 Program Flow Diagram

With the procedures described in previous sections a method of analysis is developed for both instantaneous and time-dependent responses of a general composite bridge beam. The method can be summarized by the flow diagram in Fig. 3.13 using the subroutines shown in Fig. 3.14. The steps include reading and printing of the input data. A series of time increments is specified and it is assumed that loads and parts of the cross-section are added at different times but only at the beginning of a given time interval. For each time increment an equilibrium position of the member is estimated for the changes in time-dependent strains in each fiber. Additional loads are discretized as nodal point loads and a new equilibrium position of the beam is estimated under the new loading condition. Steps may be omitted if they are not applicable to the time increment being considered and solution output may be printed if needed. The process is repeated for all loading cases and time increments over the interval of interest.

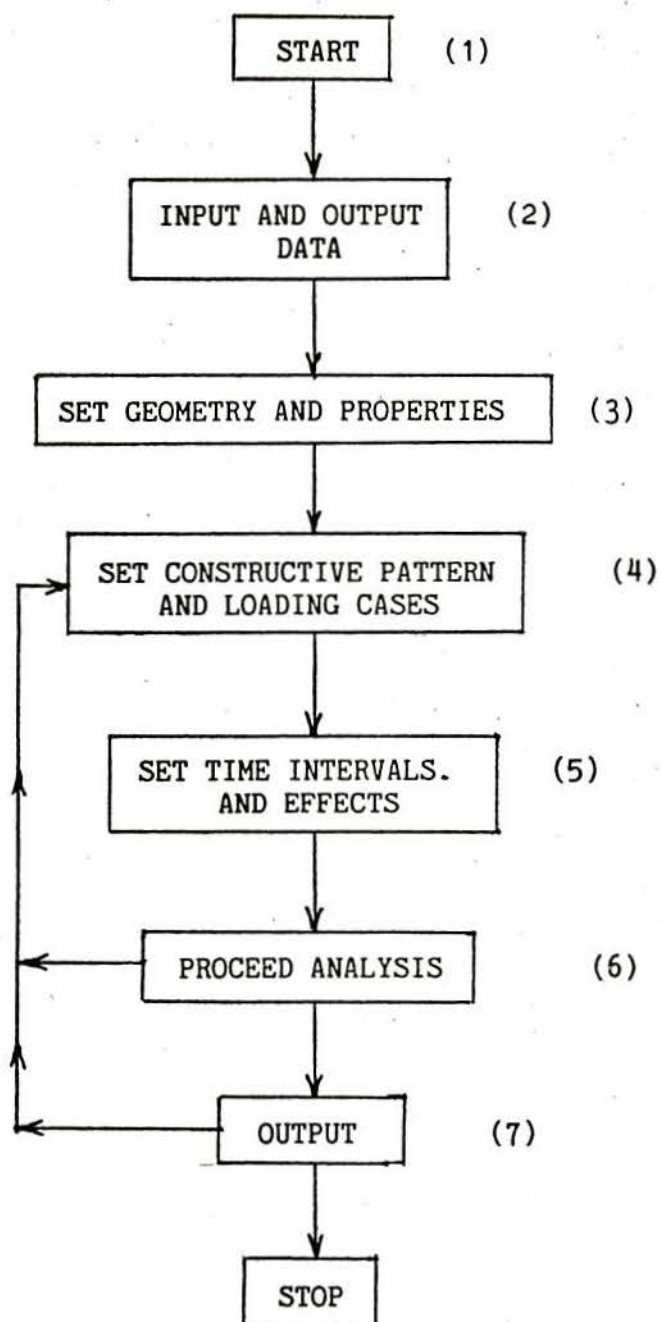


Fig. 3.13 Program's Flow Diagram

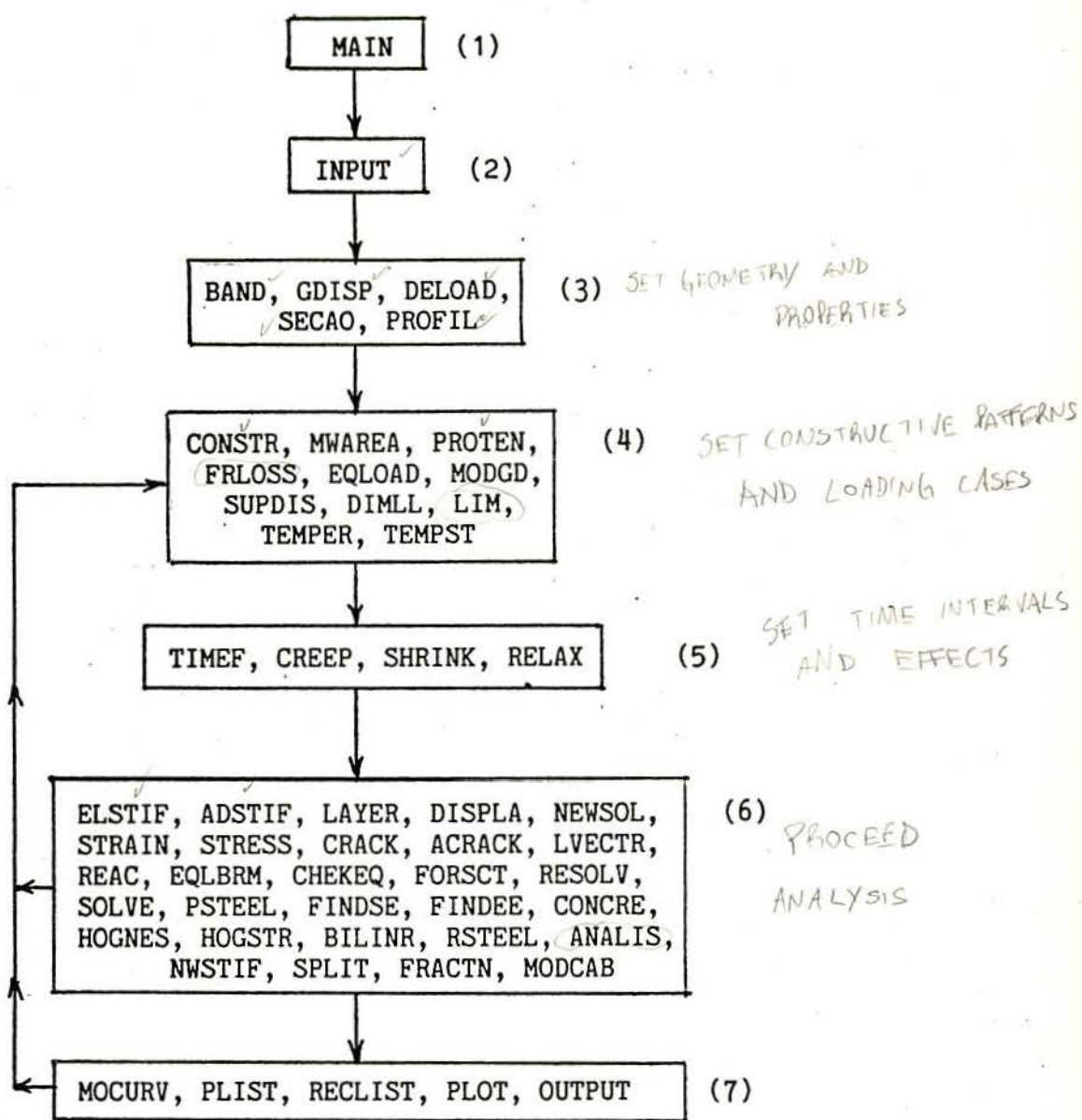


Fig. 3.14 Subroutines for phases in Fig. 3.13

4. VALIDATION OF THE ANALYTICAL MODEL

4.1 Introduction

The proposed program is intended for the analysis of instantaneous and time-dependent responses of non-composite or composite beams, built in steel, reinforced or prestressed concrete, and simple or continuous over two or more spans. Even though its main purpose is aimed at the analysis of beams with continuous deck slabs, as detailed in Chapters 1, 3 and 5, it is also applicable to the analyses of simple and fully-continuous beams. The purpose of this chapter is to validate the analytical model by studying a group of beam members for which analytical and experimental results are available in the literature.

In the following sections, eighteen different beams are analyzed and presented as ten separated problems. Problems 1 to 5, cover the instantaneous response and strength of non-composite and composite beams, in steel, reinforced and prestressed concrete. The remaining five problems cover the time-dependent response of similar beams. Material properties, i.e. stress-strain-time relationships, are based on the assumed models described in Chapter 2. Where actual material properties are known, characteristic constants for the models are adjusted to fit the actual data for each particular case.

4.2 Instantaneous Response and Strength of Non-Composite Beams

4.2.1 Steel I-Beam

A simply supported W18x50 steel I-beam, under a uniformly distributed load over a span of 15 ft, is analyzed for its response up

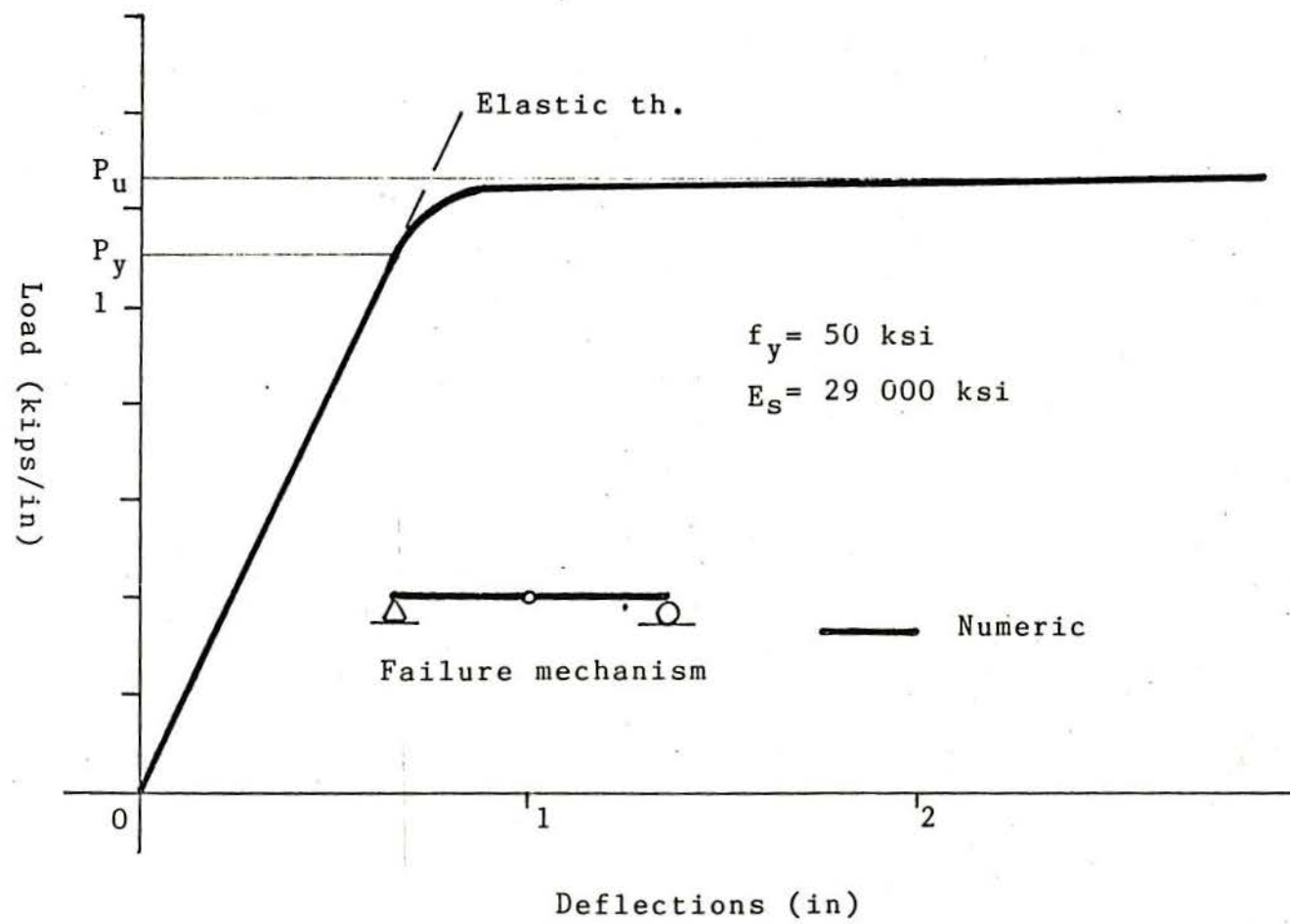
to the ultimate strength (93). One half of the beam is modeled by 9 beam elements, subdivided vertically into 30 horizontal layers. The load-deflection curve obtained by the use of the Displacement Increment Method with a specified displacement increment of 0.04 in. at the mid section is shown in Fig. 4.1 along with the assumed material properties. The curve compared very closely with analytical results obtained by the elastic theory and the plastic moment presented in Ref. (93).

The analytically obtained plastic moment is 5050 in-lb, whereas the numerically obtained is 5056 in-lb, for an ultimate deflection of 2.9 in, when a plastic hinge is formed at the mid-span.

4.2.2 Reinforced Concrete Rectangular Beam.

In a joint program carried out by the Instituto de Materiales y Modelos Estructurales (IMME) at the Universidad Central de Venezuela, Caracas, Venezuela and the Laboratory for Structural Models at MIT, a total of 132 beams at five geometric scales and two reinforcement ratios were tested. Included in the test program were four sets of reinforced concrete beams, having two scale factors with maximum aggregate size of 1 in. and 3/8 in., and eighteen sets of reinforced mortar beams, with five scale factors and maximum size of aggregate of 0.033 in., regardless of scale. From the test results presented by Litle and Paparont (94), and the numerical results by Lazaro and Richards (31), a set of six similar beams, M7.1 to M12.1, with the scale factor of one and reinforcement ratio of 1 % is selected for comparison with the predictions by the author's computer model.

Fig 4.1 - Load-deflection curve for beam Example 4.2.1.



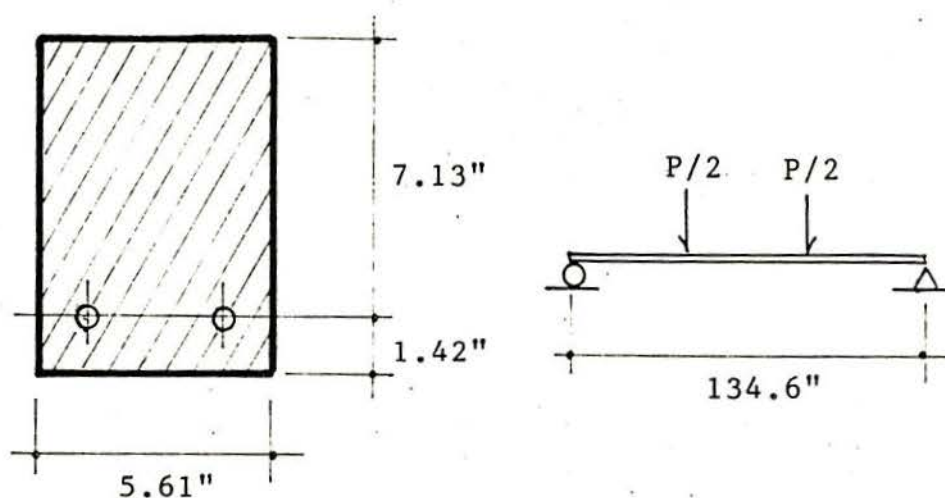
The beams were simply supported and loaded in their third points, and with the cross-section and material properties shown in Fig. 4.2. In the numerical analysis, which led to the load-deflection curves presented in Fig. 4.3, one half of the beam is modeled by 14 elements, subdivided into 30 layers, and the Displacement Increment Method is used, assuming both the Hognestad's and the bi-linear stress-strain relationships for concrete.

A comparison of the results obtained experimentally, analytically and numerically, is also presented in Fig. 4.2. In the post-cracking range the observed results indicate that the beam is stiffer than the numerically predicted behavior due to the absence of the tension stiffening effect in the analytical model. The ultimate mid-span deflection based on bi-linear stress-strain relationship is 33% more than that based on Hognestad stress-strain curve. No observed ultimate deflection is presented in the published results (94).

4.2.3 Prestressed Concrete I-Beam

Keyder (95), reported the testing of two simply supported non-composite pre-tensioned prestressed concrete beams, one of which was also numerically analyzed by Chang (36). The beam was 14 ft long and loaded symmetrically at the two points 4 ft 6 in from each support. It contained only five prestressed strands as reinforcement and the total initial pre-tensioning force was 70 Kips. (14 Kips./strand).

The cross-section of the beam and the material properties are shown in Fig. 4.4. In modeling the beam, one half of the span is analyzed by



Section and material properties

$$A_s = 0.394 \text{ in}^2 \quad \rho = 0.98\%$$

$$f'_c = 5070 \text{ psi} \quad f_y = 49 \text{ ksi}$$

Assumed concrete properties

$$E_{ci} = 57000 \sqrt{f'_c} = 4\,060\,000 \text{ psi}$$

$$f_t = 7.5 \sqrt{f'_c} = 534 \text{ psi}$$

Observed and proposed results

	P_{cr}	P_y	P_u	M_u
Observed	---	---	6050	132000
ACI'S	1808	5510	5803	130000
Num.biln.	1740	5550	5820	131000
Num.Hogn.	1716	5490	5730	129000
	(1b)	(1b)	(1b)	(1b/in)

Fig 4.2 - Properties and results for beam Example 4.2.2.

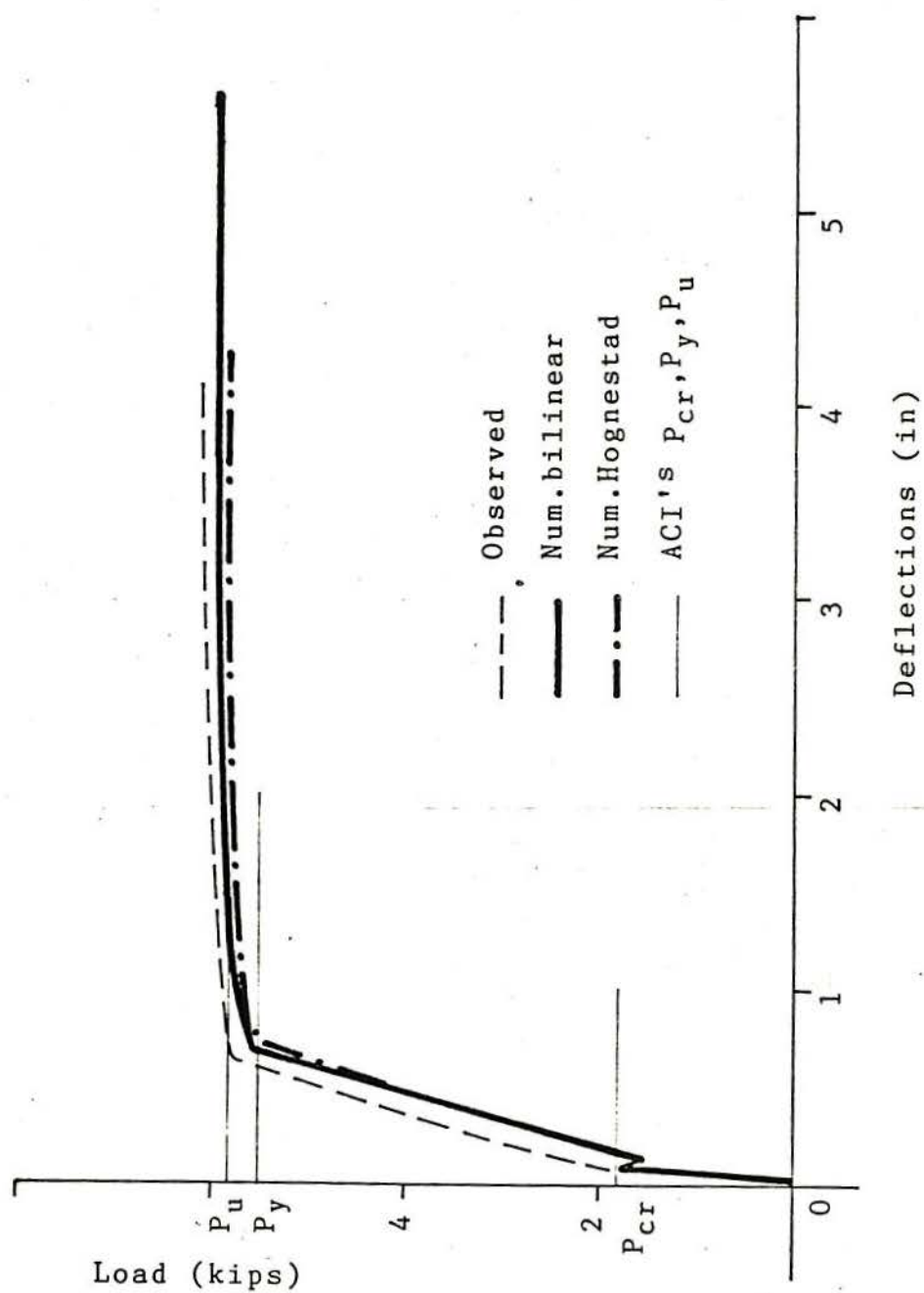
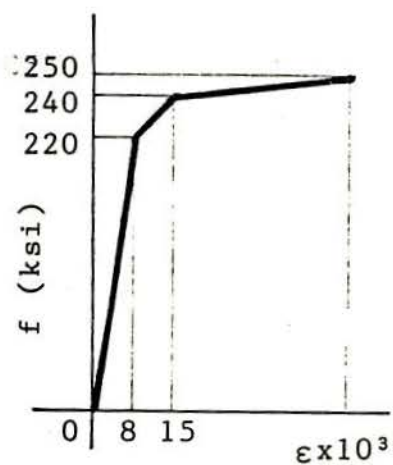
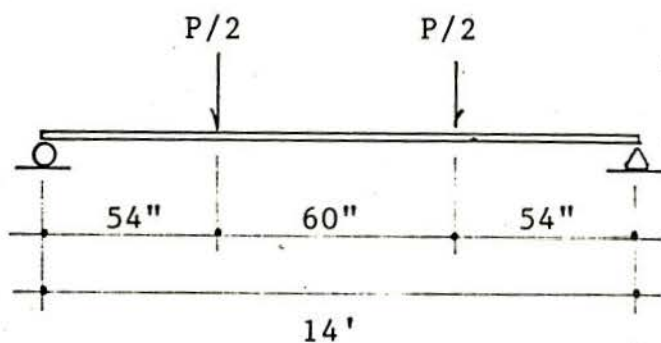
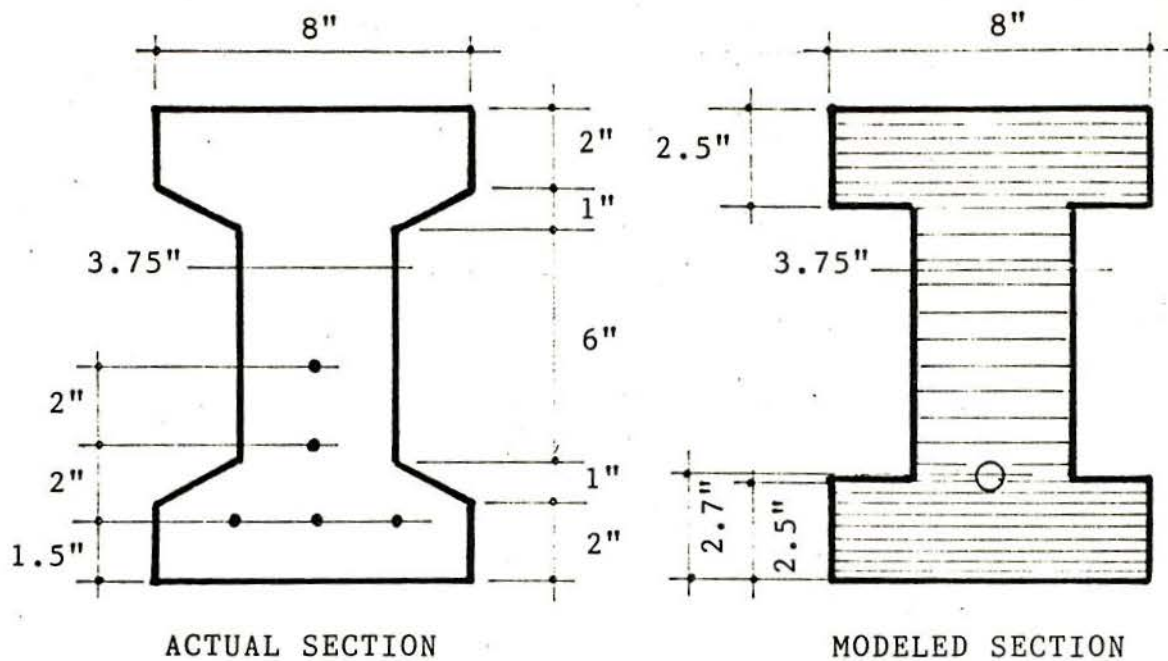


Fig 4.3 - Load-deflection curve for beam Example 4.2.2.



PRESTRESSING STEEL

$$\begin{aligned} f'_c &= 6750 \text{ psi} \\ E_{ci} &= 3300 \text{ ksi} \\ f_t &= 616 \text{ psi} \\ A_{ps} &= .4 \text{ in}^2 (5 \times \phi 3/8") \\ \epsilon_{si} &= .00622 \\ F_{si} &= 70 \text{ ksi} \end{aligned}$$

Fig 4.4 - Pre-tensioned beam for Example 4.2.3.

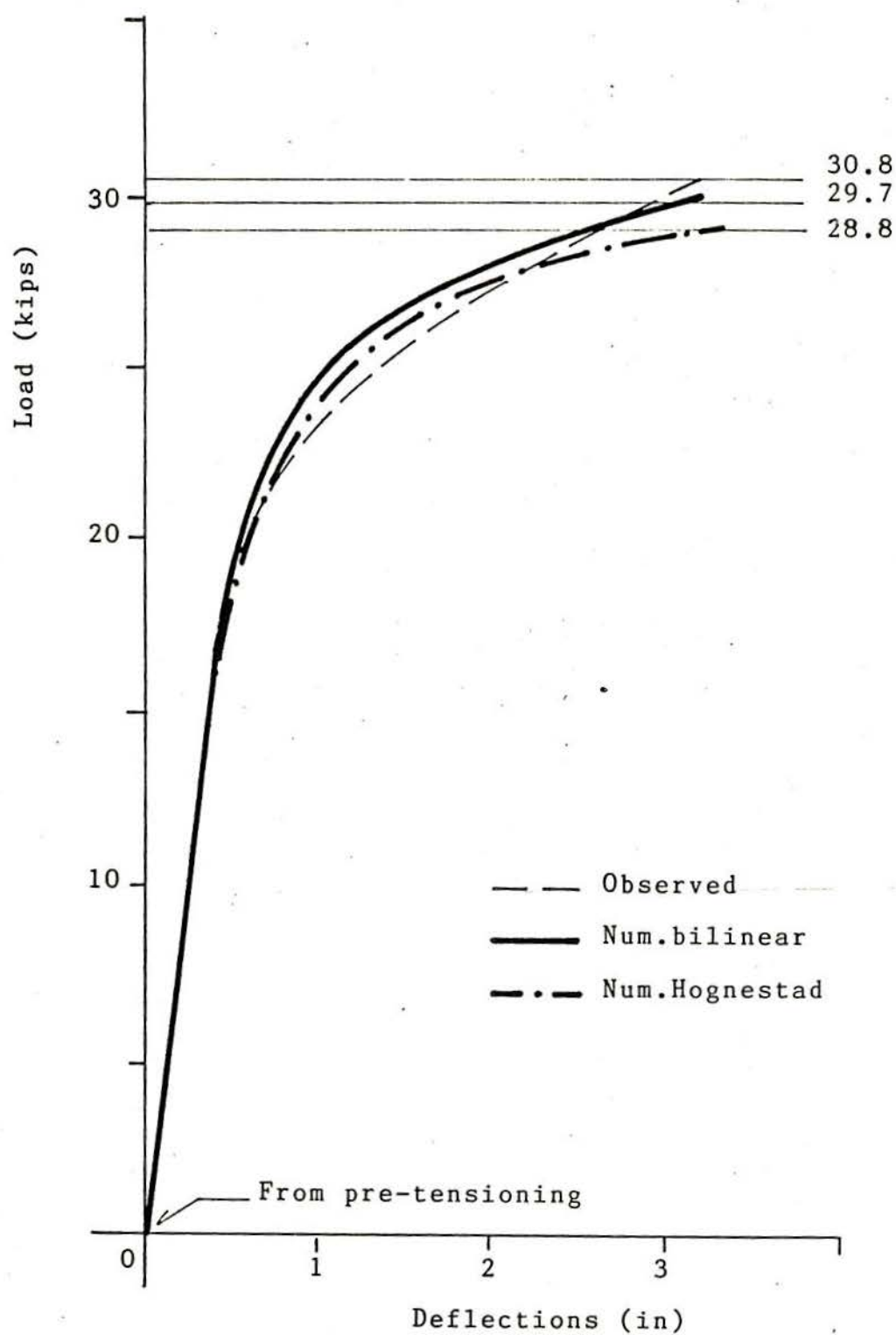


Fig 4.5 - Load-deflection curve for beam Example 4.2.3.

using 11 elements, subdivided into 24 layers. The Displacement Increment Method is used for live load using both the Hognestad and bi-linear stress-strain relationships. The load-deflection curves are shown in Fig. 4.5.

The ultimate loads obtained numerically, by using the two different stress-strain relationships, are respectively 3.6 and 6.5 percent lower than the 30.8 kips. reported by Keyder. In the post-cracking range, the beam appears to be stiffer as predicted by the computer model, which is believed to be due mainly to the sharp tri-linear modeling of the stress-strain relationship for the prestressing steel.

4.3 Instantaneous Response and Strength of Composite Beams

4.3.1 Prestressed Concrete Double Tee Beam

A standard double tee section taken from the PCI Design Handbook (18), with a simple span of 36 ft was selected to test the ability of the program in analyzing the composite beam action. This section was also analyzed by Lo (37), using a modified form of the program developed by Chang (36), as well as by the elastic theory, the effective modulus method and the ACI method for ultimate moment. Since no measurement of the actual behavior of the beam is available, Lo's results will be used to compare with the results obtained from the computer analysis.

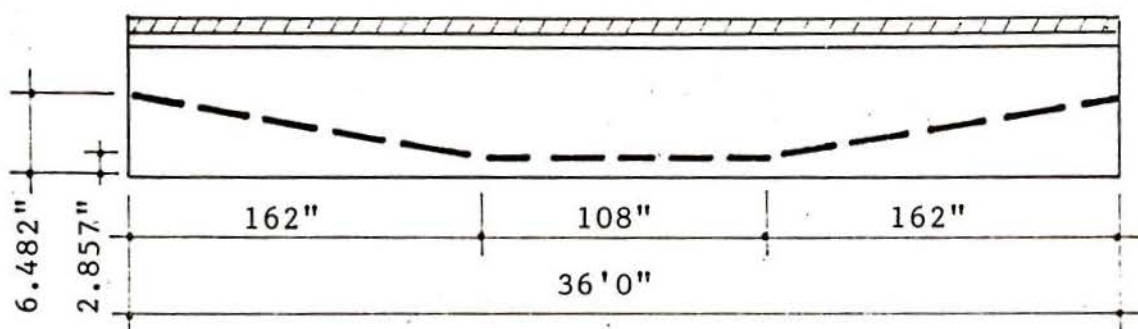
The beam is pre-tensioned by two 7-wire strands, 270 K grade, with initial prestressing stress fsi of 189 ksi. At transfer the prestressing stress is assumed to be 0.9 fsi and equal to 170 ksi. Details of the draped cable profile, the cross-section and material

properties assumed in the analysis are given in Fig. 4.6. The beam is assumed to be pre-tensioned before the topping is cast. When the topping is cast, its weight is supported by the beam alone. Live load is uniformly distributed over the top surface and applied after the composite action is obtained.

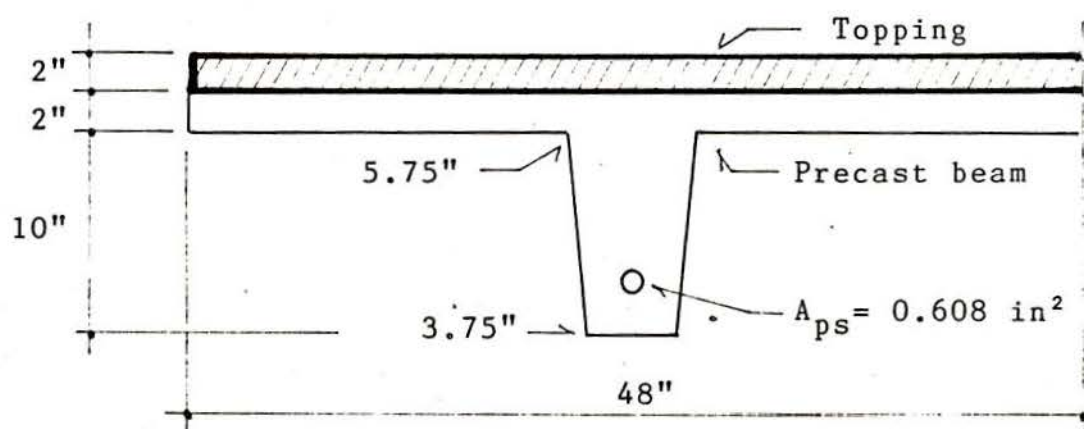
In the proposed analysis a symmetric quadrant of the beam is modeled by 18 beam elements, subdivided into 20 and 5 layers for the beam and topping, respectively. Prestressing and dead loads are applied by using the Load Increment Method, and live load by the Displacement Increment Method, with specified displacement increments of 0.01 in. Both the Hognestad and bi-linear stress-strain relationships for concrete are assumed, and the results are presented in Fig. 4.7.

The load-deflection responses from the computer analysis and from the elastic theory are in fairly good agreement up to the cracking load of the beam. A stiffer beam is predicted by Lo's analysis before the composite action is formed. However, no change in the stiffness of the section is indicated by Lo's results after the development of composite action. Evidently, he has shown the camber for a stiffer section and thus his curve begins with less initial upward deflection prior to downward load application. A slightly higher cracking load is predicted by the computer analysis, as compared to Lo's results and that of the elastic theory, which is probably due to approximation in modeling the section.

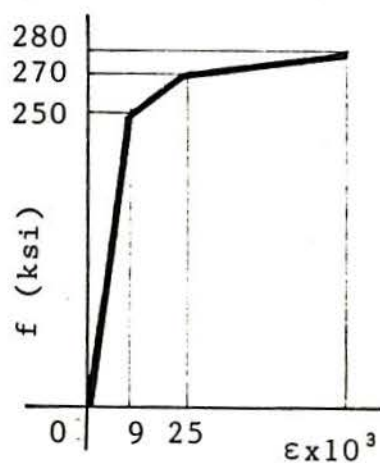
The responses to applied load after the composite action is developed, as represented by both analyses are in good agreement. However, the Effective Modulus of Inertia Method predicts a much less



TENDON PROFILE



CROSS-SECTION

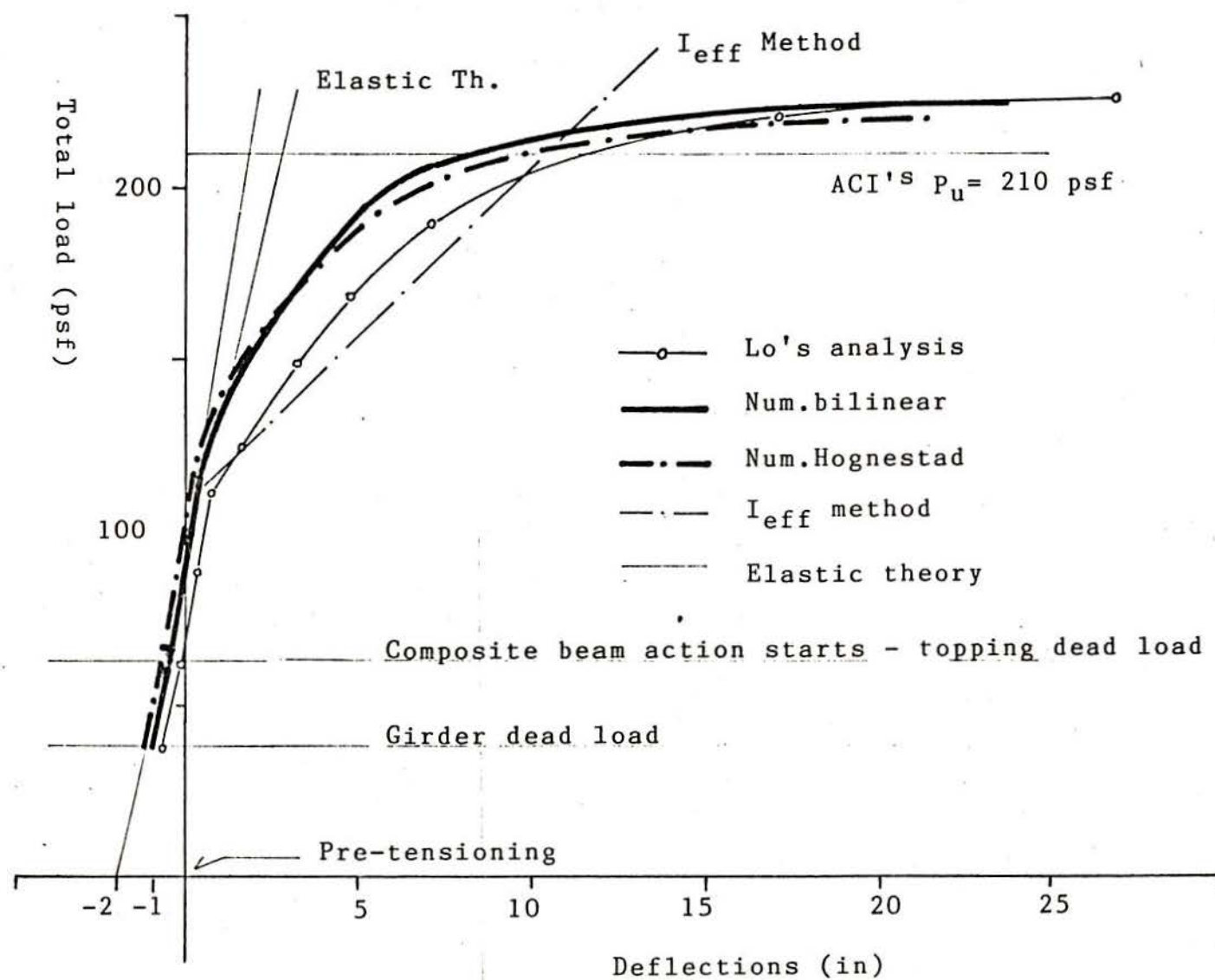


PRESTRESSING STEEL

$f'_c = 5000 \text{ psi}$ (girder)
 $E_{ci} = 4290 \text{ ksi}$ (")
 $f'_c = 3000 \text{ psi}$ (topping)
 $E_{ci} = 3320 \text{ ksi}$ (")
 $f_{si} = 189 \text{ ksi}$
 (before transfer)
 $E_{ps} = 27800 \text{ ksi}$

Fig 4.6 - Pre-tensioned composite beam for Example 4.3.1.

Fig 4.7 - Load-deflection curve for beam Example 4.3.1.



stiff beam after cracking and does not show the ductility of the beam in the range where the prestressing steel yields. The ultimate loads as presented by the different methods are: 227 psf. by Lo's analysis, 225 and 221 psf. by the computed analyses, using a bi-linear and Hognestad's stress-strain relationships, respectively, and 210 psf. by the ACI Method, which are within about 8 percent of one another.

4.3.2 Two-Span Prestressed Concrete I-Beam

From the group of three pre-tensioned composite and continuous beams tested by Wong (38), Beam BS-3 is chosen for validation of the author's program in modeling prestressed continuous beams. The beam was also analyzed previously by Chang (36).

The beam, as shown in Fig. 4.8, was composed of two standard I-girders, each 15 ft long, and connected by a cast-in-place deck slab with a rectangular diaphragm, positioned over the intermediate support. The girders were pre-tensioned, after that the deck and diaphragm were cast making a continuous beam for live load. Both deck and girders were reinforced with steel bars with yield strength of 60 and 85 ksi. respectively.

The assumed material properties are shown in Fig. 4.8. The computer analysis was performed by modeling one of the spans with 17 beam elements, subdivided into 20 and 10 layers for the beam and deck, respectively. Loading was applied as two concentrated loads, at the center of each span, and the analysis was carried out by the Displacement Increment Method, with specified displacement increments of

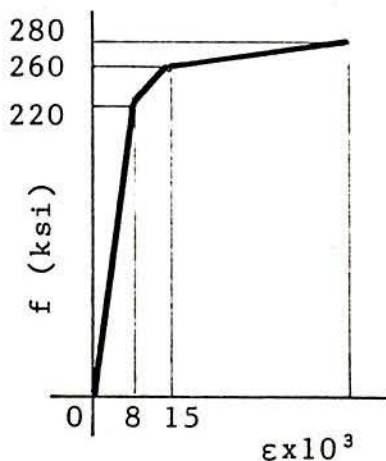
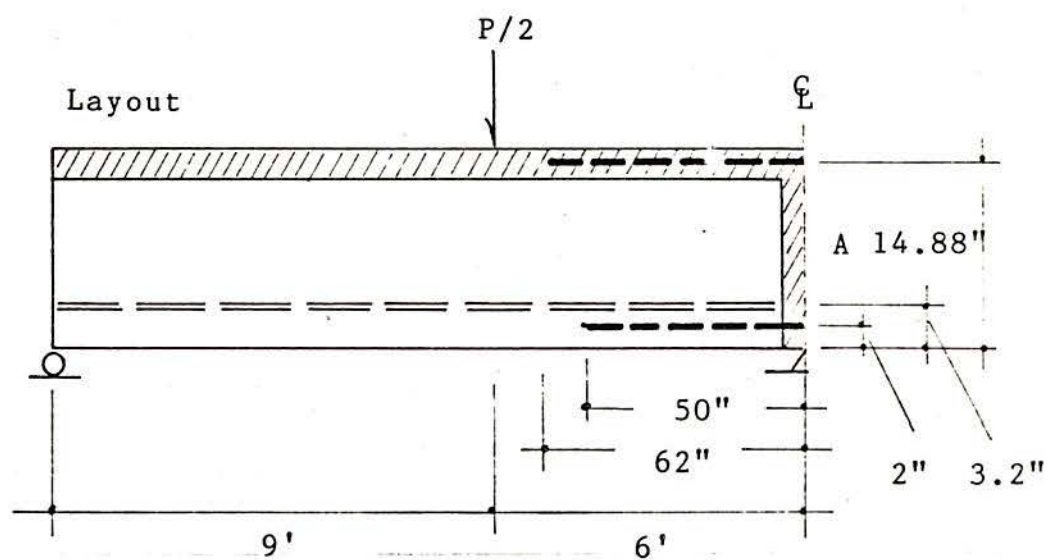
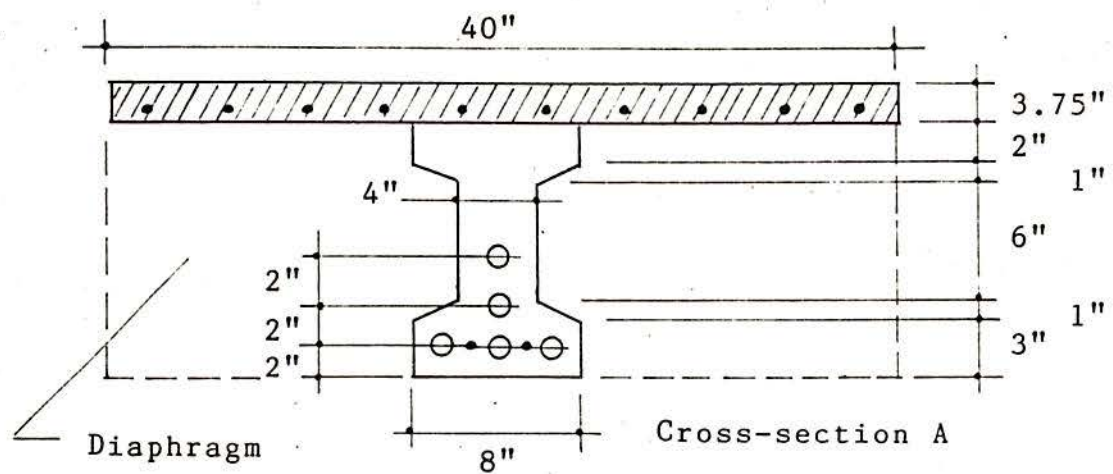
0.01 in. Analysis for the effect of prestressing, however, was obtained by using the Load Increment Method.

The general shape of the load-deflection curve, shown in Fig. 4.9 for the mid-span deflection, is in good agreement with the observed results, although the beam seems to be somewhat stiffer up to near the ultimate range based on the computed results. This stiffer response may be attributed to the early occurrence of cracking in the deck slab near the intermediate support. This cracking is not evidenced in the analytical curve by the sudden drops characteristic of cracking development. Flexural cracks due to positive moment, evidenced in the analytical curve by the first drop at a load level of 54 kips., are however in good agreement with the observed results. The ultimate loads obtained by using a bi-linear and Hognestad stress-strain relationships are 117 and 115 kips. respectively, which are within 7 percent of the observed ultimate load of 123.5 kips.

4.4 Time-Dependent Response of Non-Composite Beams

4.4.1 Reinforced Concrete Rectangular Beam

Bakoss, et al (28) have reported the testing for time-dependent effects of four reinforced concrete beams, performed at the N.S.W. Institute of Technology, Sidney, Australia. Two similar one-span beams, designated 1B1 and 1B2, cast with one of the two concrete mixes used, Mix A, are selected for checking the time-dependent response analysis by the author's method. The beams were singly reinforced with two 12 mm bars, at a reinforcement ratio of 0.017, as shown on Fig. 4.10. They were cast and moist cured for 14 days, remaining in a climate-controlled



PRESTRESSING STEEL

$f'_c = 6720$ psi (girder)
 $E_{ci} = 3300$ ksi (")
 $f'_c = 4410$ psi (deck)
 $E_{ci} = 2700$ ksi (")
 $A_s = 0.88$ in²
 $A'_s = 1.80$ in²
 $A_{ps} = 0.40$ in²
 $\epsilon_{si} = 0.00622$

Fig 4.8 - Pre-tensioned composite two-span continuous beam for Example 4.3.2.

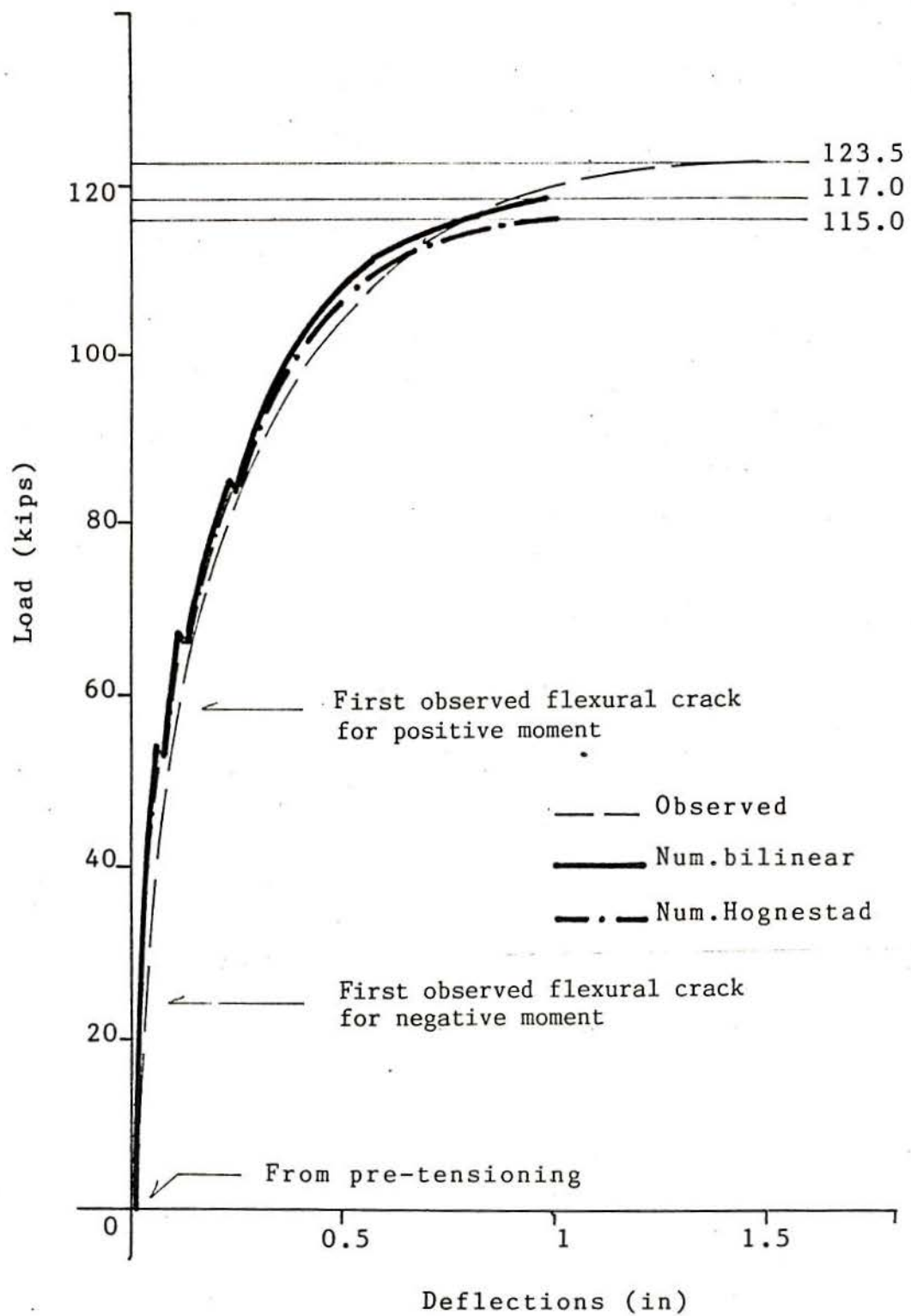


Fig 4.9 - Load-deflection curve for beam Example 4.3.2.

environment for the next 14 days, when they were tested under load at 28 days.

As shown in Fig. 4.10, the beams were loaded in their third points, by two concentrated loads of 2.6 KN (585 lb), 45 percent greater than their cracking load capacity. The resulting mid-span bending moment was 62 percent of the calculated moment capacity of the sections. From that time on, the beams were observed for their post-cracking time-dependent deflection up to 500 days.

The effects of creep and shrinkage were observed in a companion beam, with the same cracking pattern as the one under test, but free of loading. The ultimate coefficients for creep and shrinkage, as obtained according to four different codes, vary from 1.4 to 2.8 and 0.0002 to 0.0007, at ages of 600 and 800 days, respectively. The coefficients obtained by following the ACI specifications ⁽⁵⁶⁾ were 1.5 and 0.0007, which were also used in the numerical analysis.

The beam was modeled by using 9 elements, subdivided into 12 layers, and the time-dependent response under the effects of creep, shrinkage and aging of the concrete was obtained by following the procedure outlined in Section 3.9. Fig. 4.10 shows the comparison of the time-dependent responses obtained experimentally and numerically, by using both assumed stress-strain relationships for concrete. Very good agreement is found concerning the general shape of the response up to an age of 500 days.

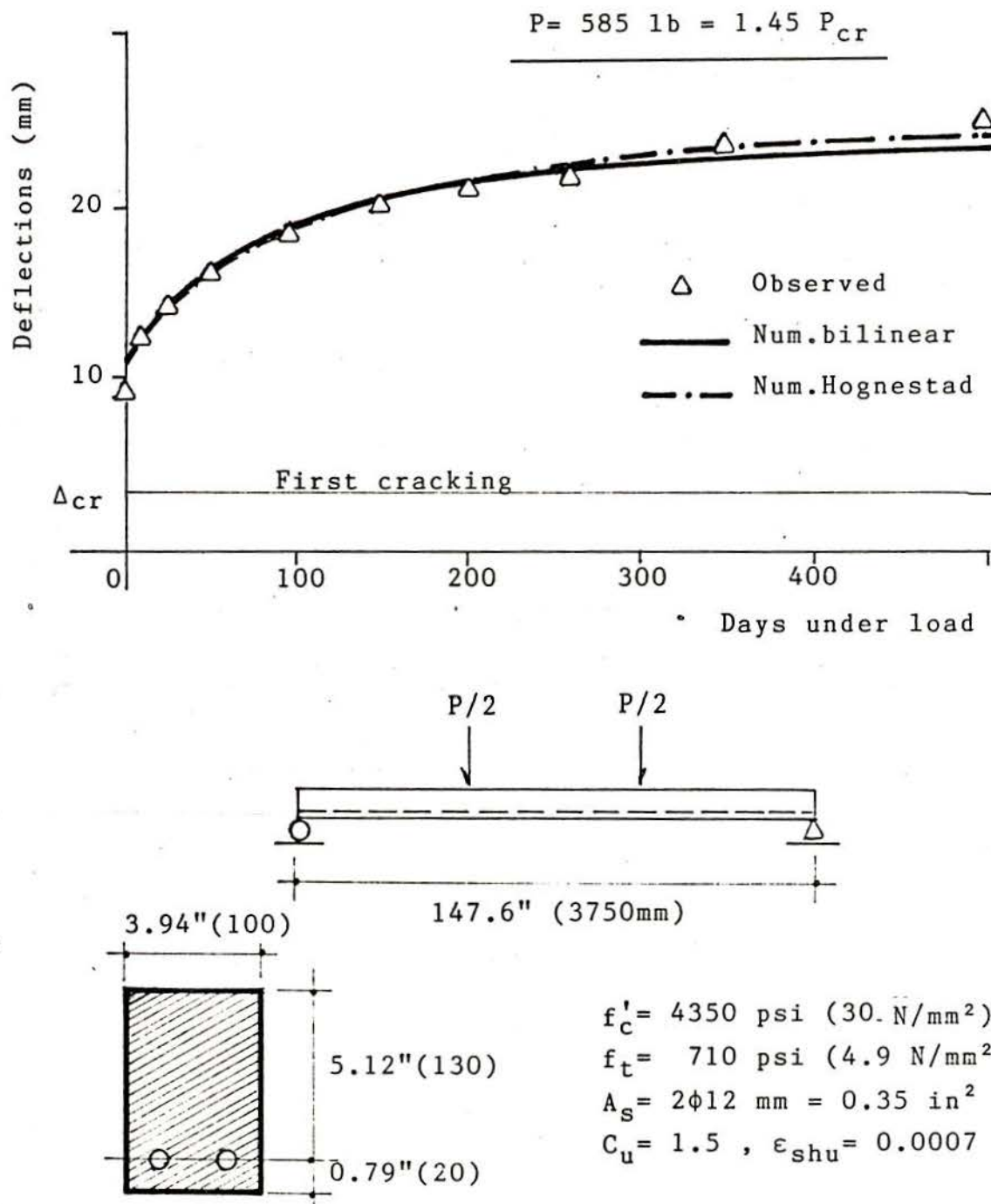


Fig 4.10 - Time-deflection curve, loading arrangement, and cross-section and material properties for beam Example 4.4.1.

4.4.2 Two-Span Reinforced Concrete Rectangular Beam

In the same work by Bakoss, et al (28), two two-span continuous beams were also tested for their time-dependent response under concentrated sustained loads. These beams had similar characteristics as the ones discussed above although they were cast with a different concrete mix, Mix B, and reinforced for both positive and negative moments as shown in Fig. 4.11. Two concentrated loads of 6 KN (1350 lb) were applied at the center of each span and the resulting maximum negative moment was 63 percent of the calculated moment capacity of the section, or 47 percent greater than the cracking moment capacity.

The assumed material properties, as listed in Fig. 4.11, were used for the analysis of the post-cracking time-dependent response of the beam, modeled by 12 elements, subdivided into 12 layers, for one span. The observed and computed responses are in good agreement, as seen in Fig. 4.11.

4.4.3 Prestressed Concrete Rectangular Beams

An investigation of the time-dependent responses of non-composite, simply supported and pre-tensioned concrete beams, prior to cracking, was conducted by Zundeleovich, et al (65) at the University of Hawaii, in conjunction with the State of Hawaii Department of Transportation, Highway Division. The beams were made of normal and lightweight concretes manufactured with Hawaiian aggregates. Three sets of specimens, made from basalt, cinderlite, and vulcanite aggregates, were used. Each set contained seven beams, three for studying camber, three

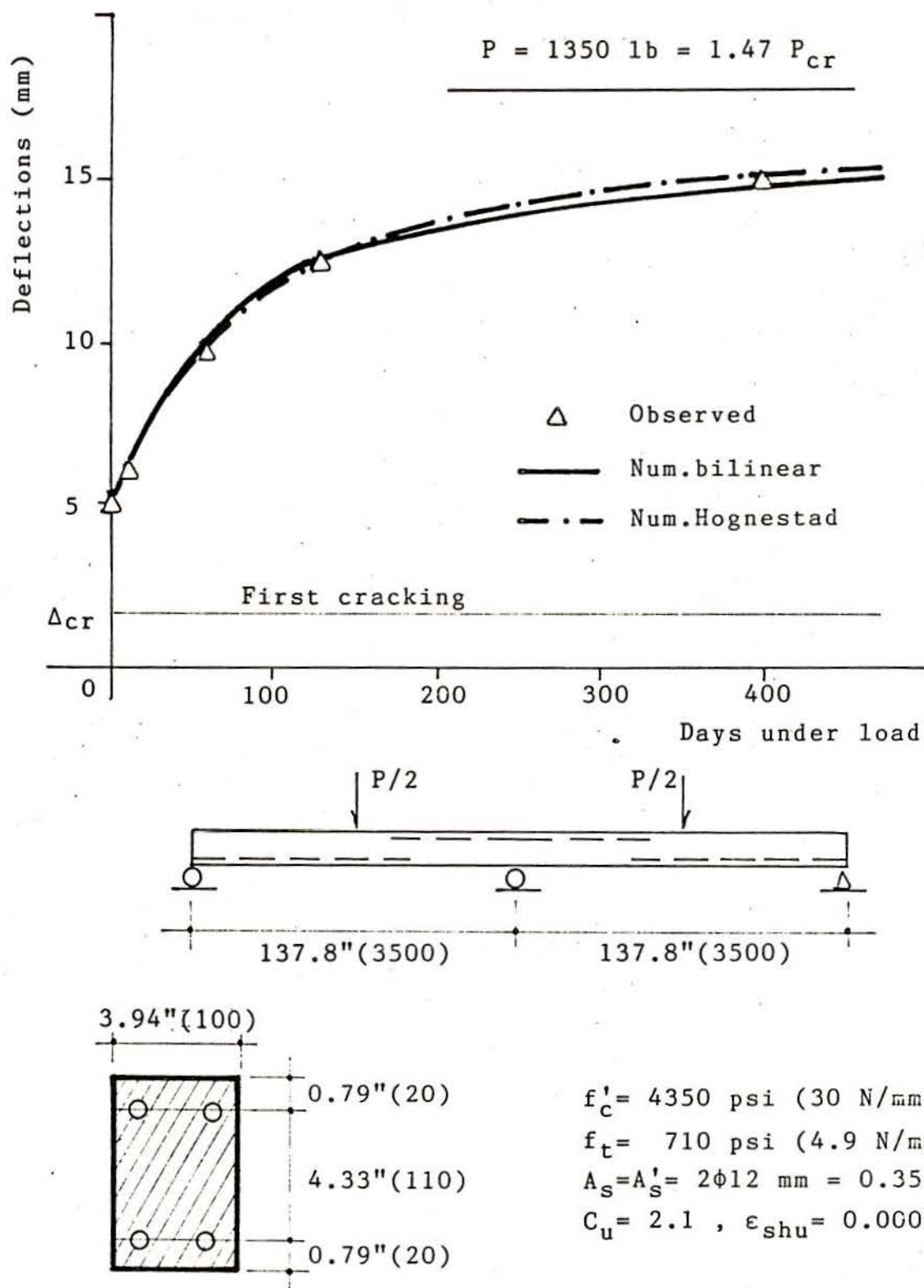
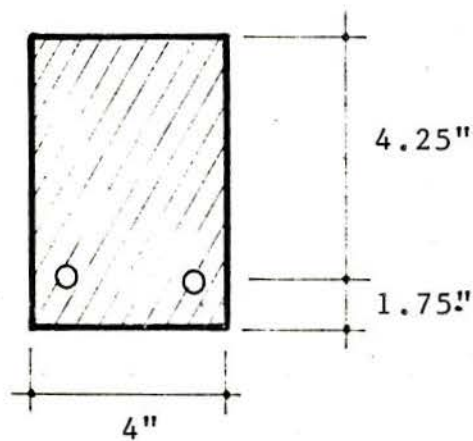
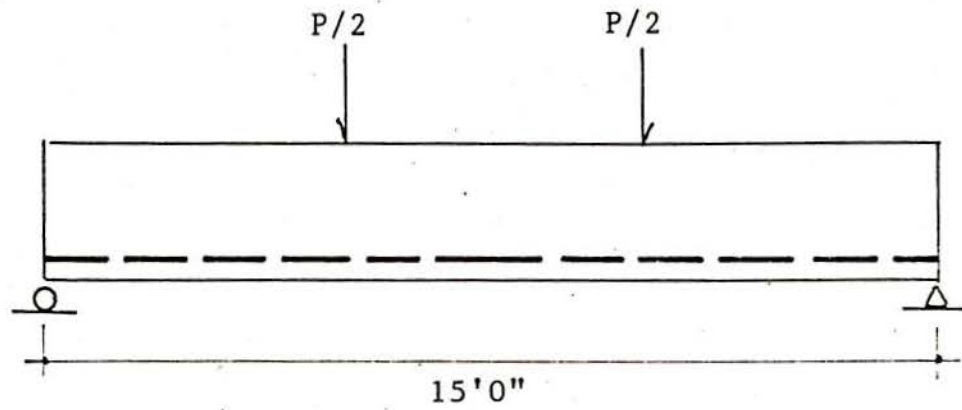


Fig 4.11 - Time-deflection curve, loading arrangement, and cross-section and material properties for beam Example 4.4.2.

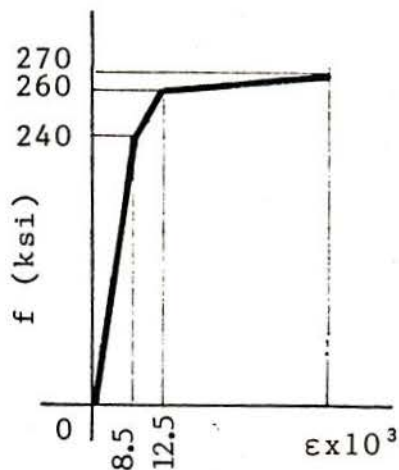


$$A_{ps} = 2 \phi 3/8"$$

$$= 0.17 \text{ in}^2$$

$$F_{si} = 15 \text{ kips/str.}$$

PRESTRESSING STEEL



$$f'_c = 5900 \text{ psi}$$

$$E_{ci} = 4400 \text{ ksi}$$

$$E_{ps} = 28\,000 \text{ ksi}$$

$$f_{su} = 270\,000 \text{ psi}$$

$$C_u = 3.3$$

$$\epsilon_{shu} = 0.00105$$

Fig 4.12 - Pre-tensioned beam for Example 4.4.3.

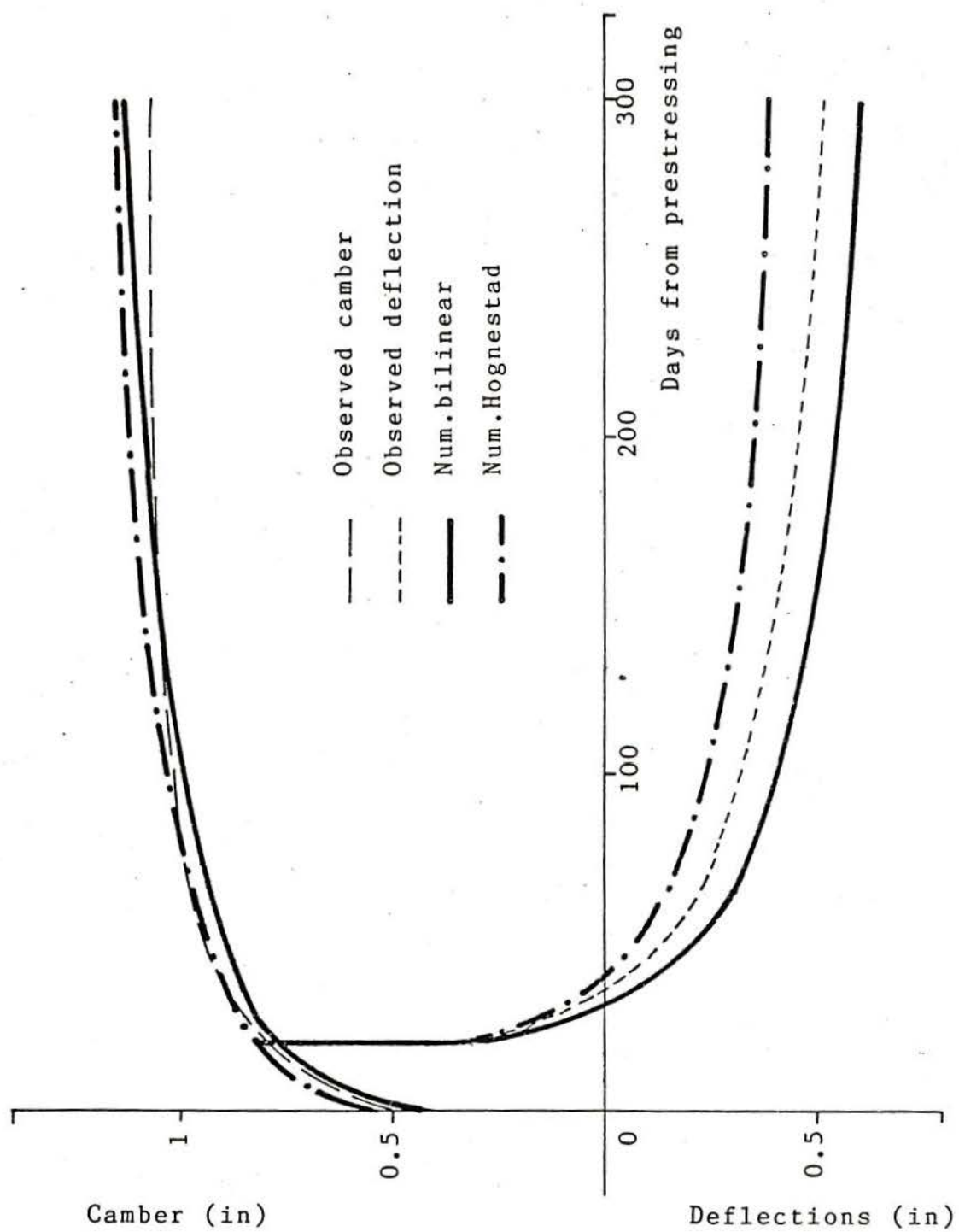


Fig 4.13 - Camber and deflection-time curves for beam Example 4.4.3.

for studying deflection and the other as a shrinkage specimen. The basalt specimens, designated as BEAM1 series, are selected for analysis by the computer program in handling creep recovery under partial unloading of a beam.

The beams were 4 in. by 6 in. in cross-section, and simply supported over their 15 ft span. They were prestressed at the age of seven days by two straight 7-wire strands at an eccentricity of 1.25 in.. The details of the beam and material properties are shown in Fig. 4.12. The camber specimens were observed for camber growth with the beams carrying only their own weight. For the deflection specimens, the beams were loaded at their third points by two 750 lb loads per beam at 21 days after prestressing.

For the computer analysis, one half of the beam was modeled by 9 elements, subdivided into 12 layers. The pre-tensioning effect is obtained by the Load Increment Method, live load application obtained by the Displacement Increment Method and the time-dependent responses by using the Rate of Creep Method and the Superposition Method, as explained in Chapters 2 and 3.

The camber and deflection obtained by assuming both the Hognestad and bi-linear stress-strain relationships for concrete are compared with the observed results in Fig. 4.13. The calculated instantaneous deflections, either for prestressing or for live load, are in good agreement with the observed results. So are the general shapes of the time-dependent responses. Using the Hognestad stress-strain relationship seems to overestimate the camber growth and underestimate the deflection under a creep recovery process. The bi-linear stress-strain relationship

gives errors in the opposite sense for deflection, but seems to predict closely the observed camber growth due to prestressing.

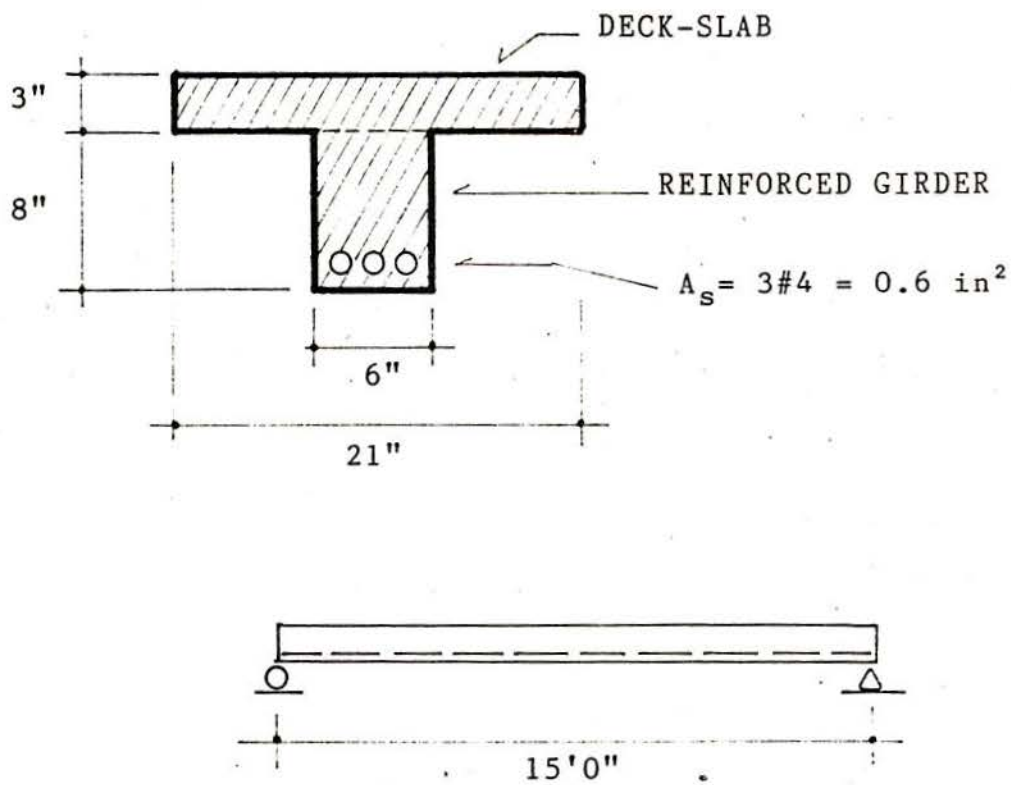
4.5 Time-Dependent Response of Composite Beams

4.5.1 Reinforced Concrete Rectangular Beams

Kripanarayanan and Branson (96) reported studies on the time-dependent behavior of composite reinforced concrete beams, resulted from the age differential between the casting of the beams and the casting of the deck slab. Three simply supported beams, as shown in Fig. 4.14, were cast and tested under the influence of dead load only. One of the beams was non-composite and served as the control specimen for the other two, of which their decks were cast at the age of one and seven weeks respectively after positioning of the beams.

The beams were made of sand-lightweight concrete with a 28-day cylinder strength of 3950 psi, and the decks of normal weight concrete with a 28-day cylinder strength of 4225 psi. All beams were singly reinforced with three #4 bars, having a reinforcement ratio of 0.01667, the deck slabs were not reinforced. The assumed ultimate creep and shrinkage coefficients were 4.0 and 0.0006 for the beams, and 4.0 and 0.0004 for the slabs, respectively.

The beams are modeled for half span by 6 beam elements, subdivided into 12 and 6 layers, for the web and flange respectively. Dead load is applied by the Load Increment Method and the time-dependent response obtained by using the Rate of Creep and Superposition Methods.



$$\begin{aligned}
 f'_c &= 3950 \text{ psi (beam-sand lightweight concrete)} \\
 E_{ci} &= 3000 \text{ ksi} \\
 f'_c &= 4225 \text{ psi (deck-normal concrete)} \\
 E_{ci} &= 3700 \text{ ksi} \\
 f_y &= 50 \text{ ksi} \\
 C_u &= 4.0 \quad (\text{beam and deck}) \\
 \epsilon_{shu} &= 0.0006 \quad (\text{beam}) \\
 \epsilon_{shu} &= 0.0004 \quad (\text{deck})
 \end{aligned}$$

Fig 4.14 - Composite beams for Example 4.5.1.

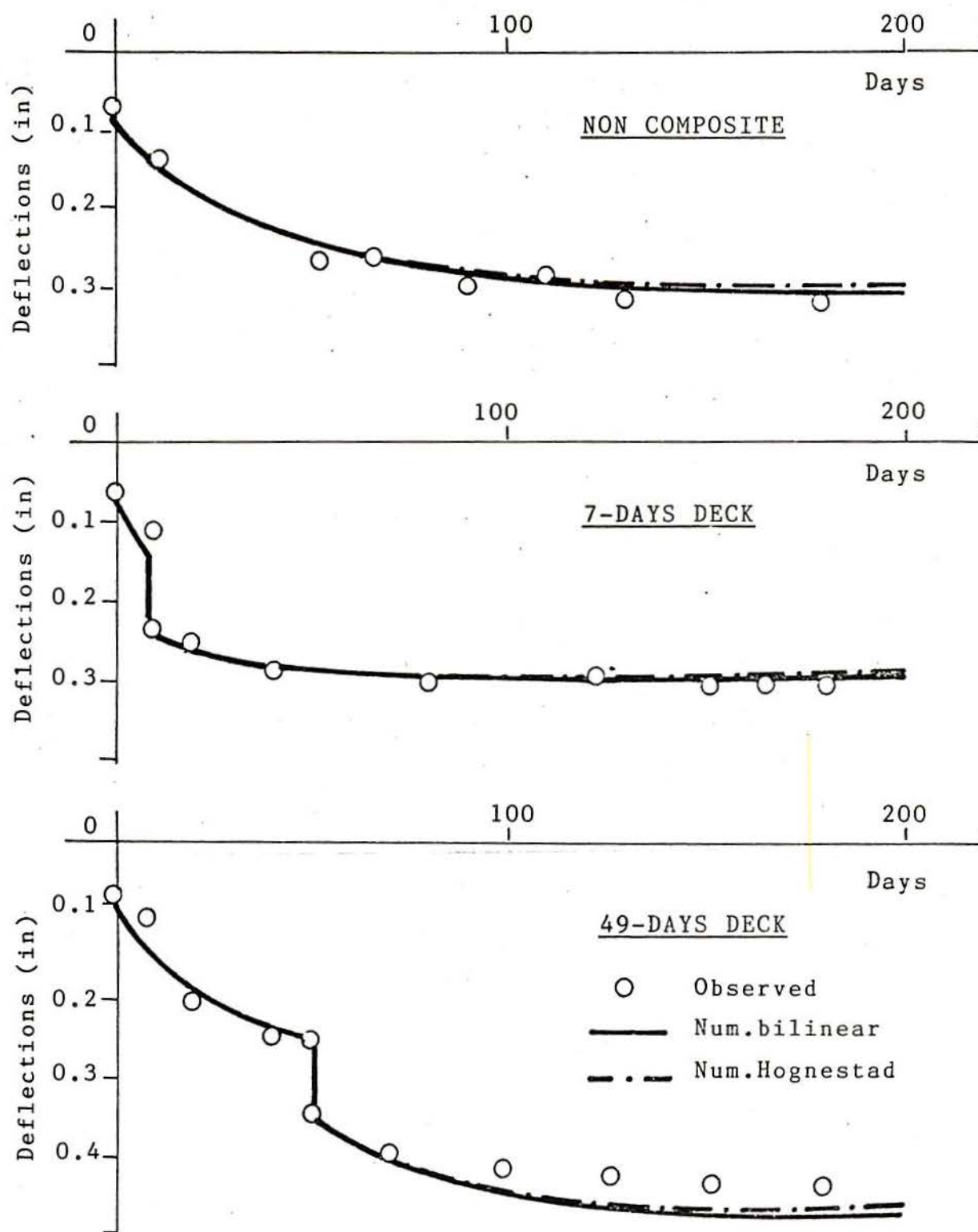


Fig 4.15 - Time-deflection curves for beams Example 4.5.1.

Shown in Fig. 4.15 are the time-dependent responses for the three beams, as obtained from the analysis and compared with the observed data. A very close agreement is obtained by the Hognestad and a bi-linear stress-strain relationships. In addition, close agreement is obtained also between calculated and experimental results. For the third beam, however, the one with the deck cast at seven weeks, the calculated results seem to overestimate the deflection response after about 20 days from the casting of the slab, predicting a final deflection some 10 percent greater than the measured value.

4.5.2 Prestressed Concrete Rectangular Beams

In studying the time-dependent response of composite prestressed concrete beams, Rao and Dilger ⁽²¹⁾ reported the testing of six one-span simply supported beams, having different reinforcement arrangements and subjected to superimposed sustained live loads.

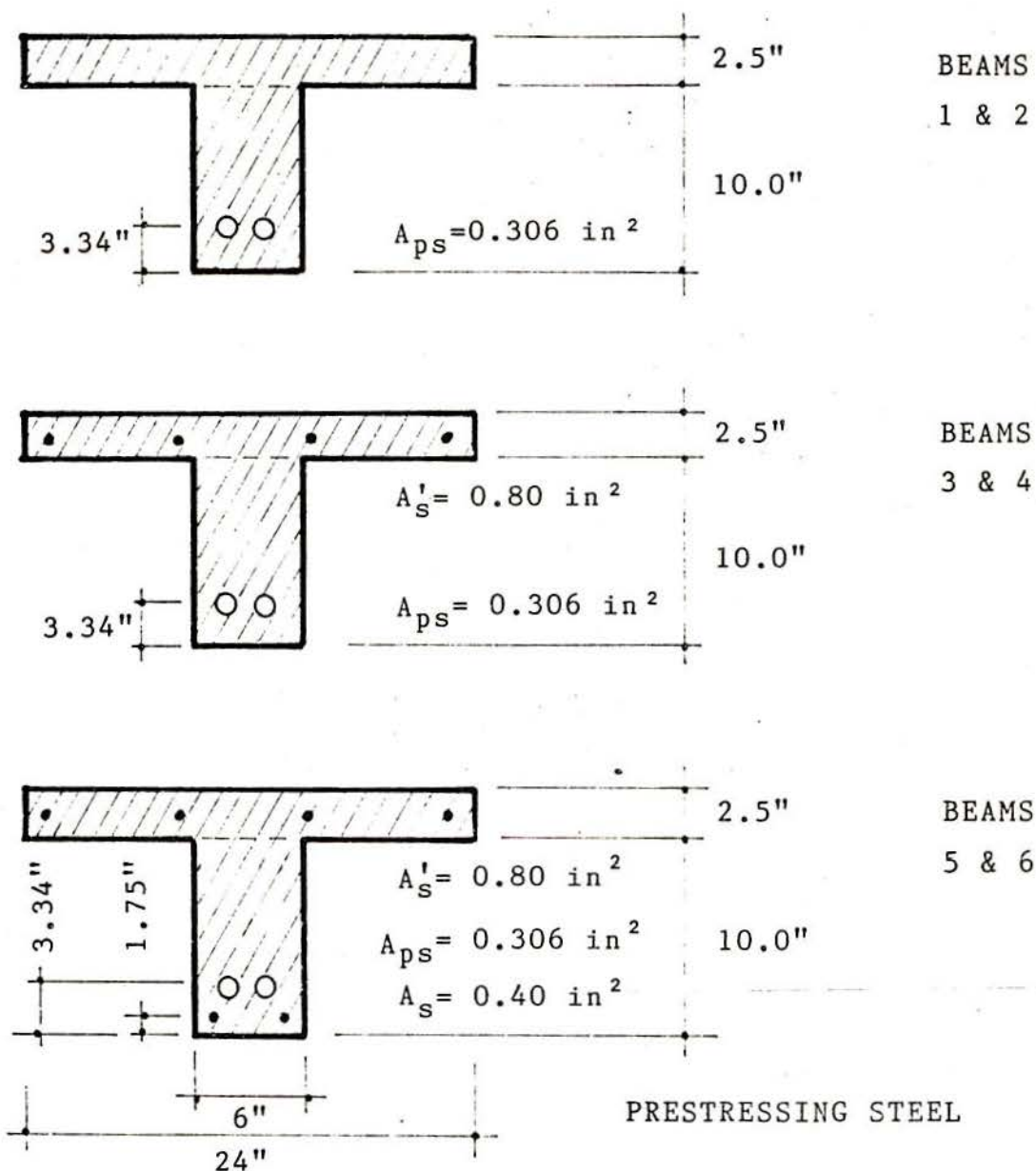
The beams, with the cross-sections shown in Fig 4.16, were numbered 1 to 6. Beams 1 and 2 were pre-tensioned but did not have any mild steel reinforcement. Beams 3 and 4 had an additional deck reinforcement, and beams 5 and 6 also had additional reinforcement in the web. All six beams were 12 ft. long and pre-tensioned by two straight 7-wire strands with an initial total prestressing force of 65.8 kips. The prestressing force was transferred to the concrete seven days after casting. The deck was cast forty one days after the casting of the beam, by using shored construction. Live load was applied on the composite member twelve days after the deck was cast. Two 5.8 kips. concentrated loads were applied at the third points of beams 2, 4 and 6.

The beams are modeled by 12 beam elements, for one half span, subdivided into 12 and 5 layers for the web and top flange, respectively. Prestressing force, dead and live loads are applied by using the Load Increment Method. The assumed material properties are shown in Fig. 4.16.

Since the strands were stressed eight days prior to transferring of the forces to the beams, the initial prestressing force used in the analysis is reduced from the initial force of 65.8 kips to account for the effects of relaxation. The assumed initial prestressing force, obtained by using the recommended PCI equations for loss due to relaxation in stress-relieved steel, given in Section 2.3.2, is 60.5 kips, 8 percent smaller than the previous value.

From the time of prestressing to one hundred and forty days after casting of the beam section, measurements were taken in the six beams for camber, deflection and curvature of the mid-span section. Figs. 4.17 to 4.20, show a comparison of the observed and calculated results, for curvature in beams 1 and 2, and camber and deflection for beams 1 to 6, respectively.

The use of the Hognestad stress-strain relationship for the web and deck concrete, shows a consistent overestimate of camber and accordingly underestimate of deflections, as compared to similar results by using the bi-linear stress-strain relationship. The particular shape of the camber- and deflection-time curves for each of the three sets of beams, vary slightly depending on the amount and position of the mild steel reinforcement. The general trend of the time-dependent responses for all sets of beams are, however, in agreement with the measured results.



	BEAM	SLAB
f'_c	6200	4210 psi
E_{ci}	4610	3640 ksi
C_u	1.60	2.48
ϵ_{shu}	.000685	.000900

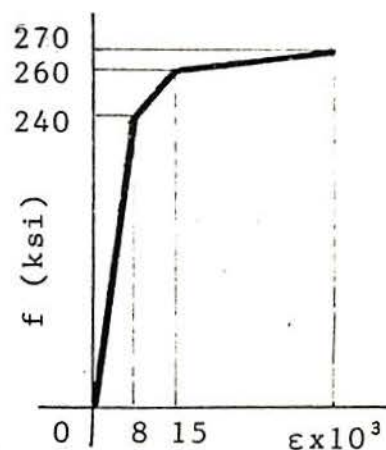


Fig 4.16 - Pre-tensioned beam for Example 4.5.2.

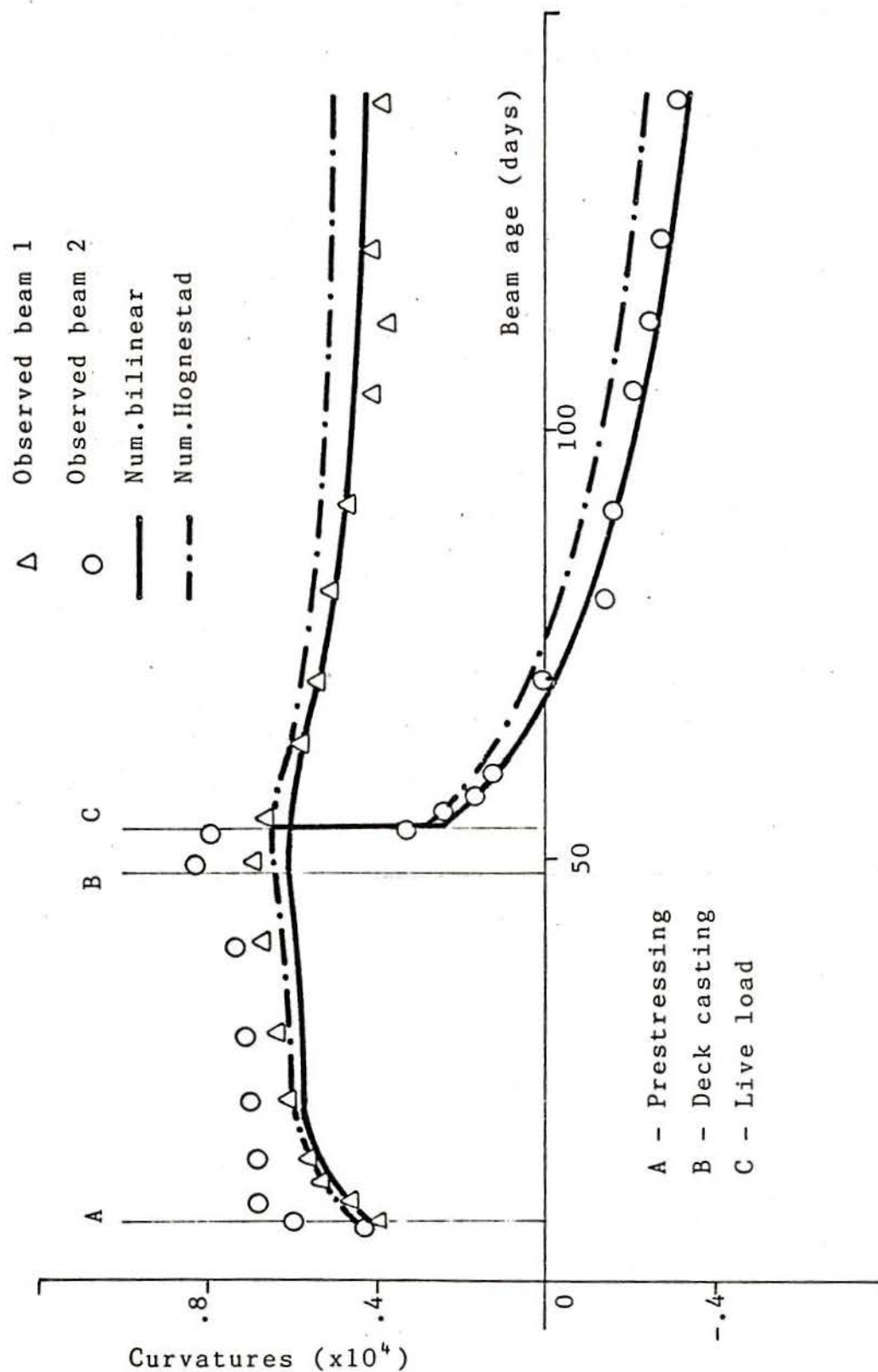
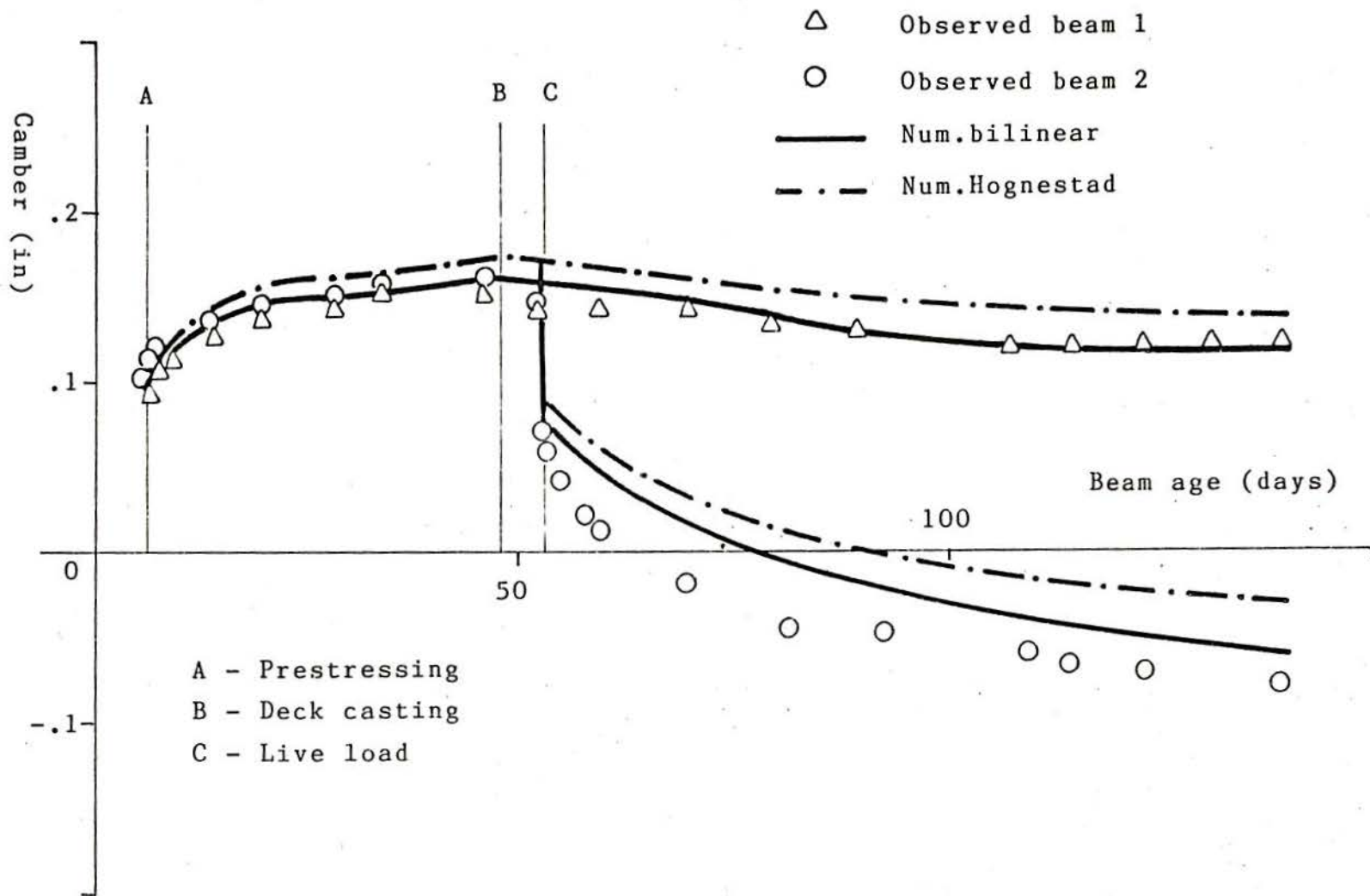


Fig 4.17 - Time-curvature curves for beams 1&2, Example 4.5.2.

Fig 4.18 - Time-deflection curves for beams 1&2, Example 4.5.2.



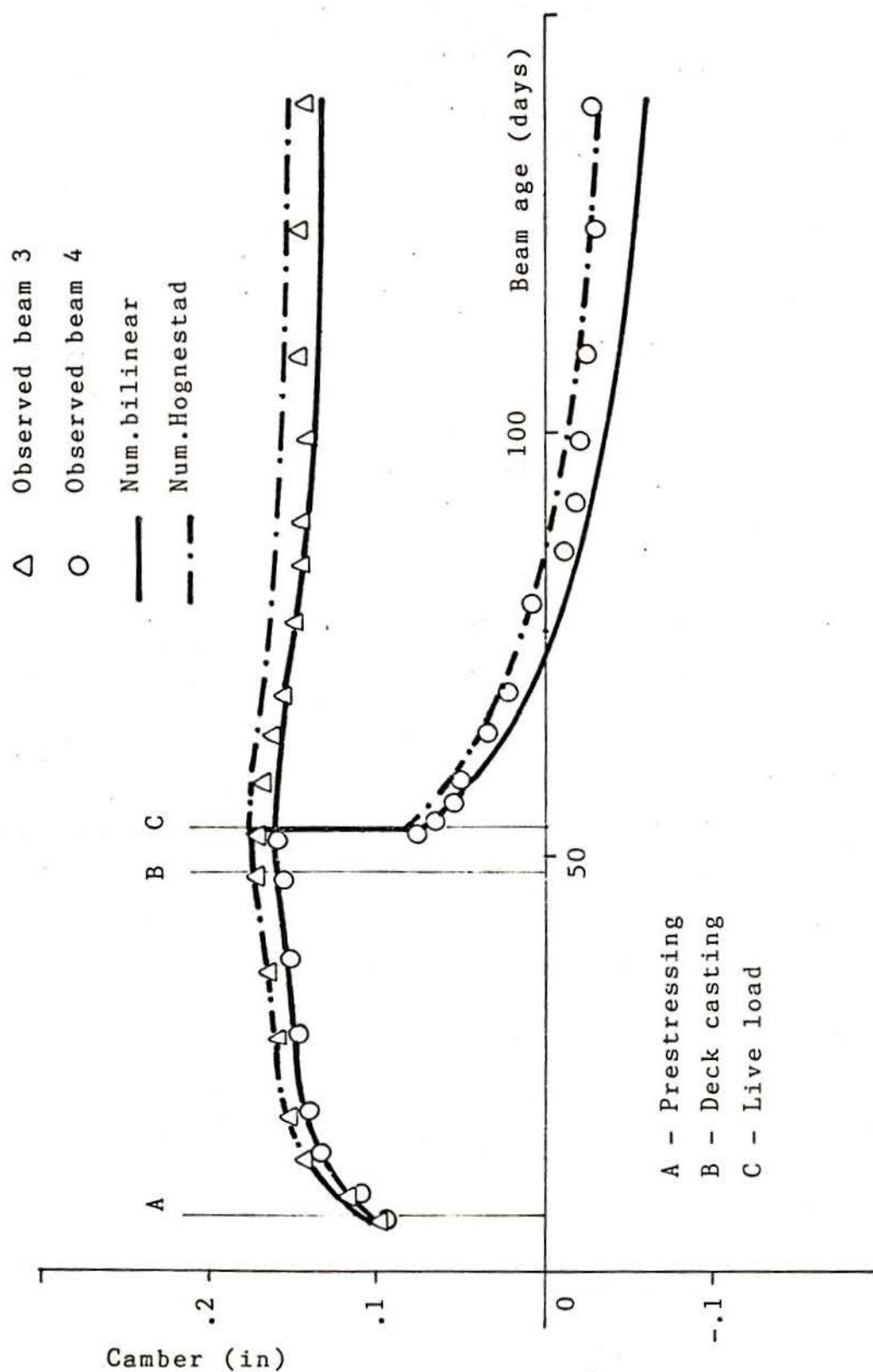
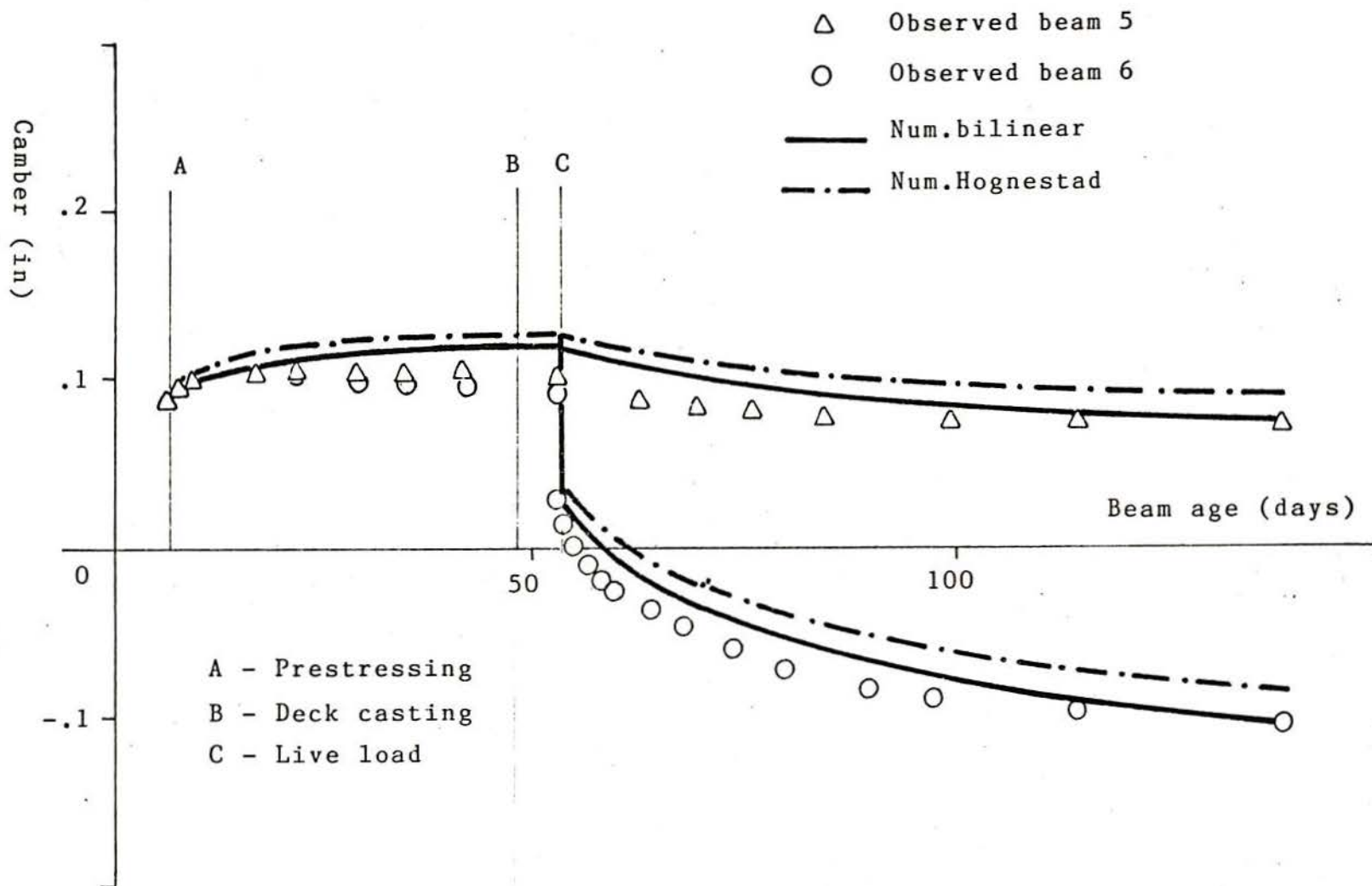


Fig 4.19 - Time-deflection curves for beams 3&4, Example 4.5.2.

Fig 4.20 - Time-deflection curves for beams 5&6, Example 4.5.2.



5. APPLICATION OF THE ANALYTICAL MODEL TO JOINTLESS BRIDGE BEAMS

5.1 Introduction

Jointless bridge beams may be considered as a solution for the persistent problems caused by the insertion of joints in multi-span bridges. The elimination of joints may be achieved in several ways:

- (a) By using a fully-continuous beam, for deck and girders, (FCB).
- (b) By casting a continuous deck and a connecting segment or diaphragm between two simple beams over each intermediate support, to develop continuity for carrying live load, (FCLL).
- (c) By casting a fully-continuous deck slab over the simple span non-continuous girders, (FCD).

Fully-continuous beam has generally established an excellent performance record. However, it is not as widely used as beams of simple span. Beams made continuous for live load have proven suitable for precast concrete construction and show remarkable performance as far as continuity is concerned when compared to fully-continuous beams. Nevertheless, they may not be adequate for the case of steel girders which are usually constructed as simple span beams with joints being formed at the deck.

A simpler and thus more economical option is to connect simply supported girders through a fully-continuous deck (FCD), with no continuity between the adjacent girders. Being also suitable for precast construction and complying with the join-free idea, they appear

to be an alternative solution to one of the severe bridge maintenance problems. Beams with continuous deck provide a simple and efficient solution not only for the construction of new bridges but also for the rehabilitation of old ones, by re-decking the still serviceable simply supported girders.

For beams in which continuity is obtained only through the deck, conventional analytical techniques are inadequate since they are based on the concept of full continuity of the beams. The numerical solution developed in this study, nevertheless, can adequately handle such unconventional cases and, due to its versatility, investigate all the different situations described previously.

In the following sections, two commonly used structures for mid-size span bridges over highway intersections will be analyzed, and comparisons will be made for different situations of loading, continuity and supporting conditions. In Section 5.2, a 100 ft two-span bridge with steel girders will be considered and in Section 5.3, a 264 ft four-span bridge with prestressed girders of equal and unequal spans will be analyzed.

5.2 Analysis of a Jointless-Deck on Two-span Beam With Steel Girders

5.2.1 General Behavior

Shown in Fig. 5.1 is a two-span bridge with two fifty feet W33x118 steel girders supporting a 7 ft by 7 in reinforced concrete deck slab (93). Three different construction details are given in Fig. 5.2, namely: fully-continuous, deck-continuous and non-continuous. The

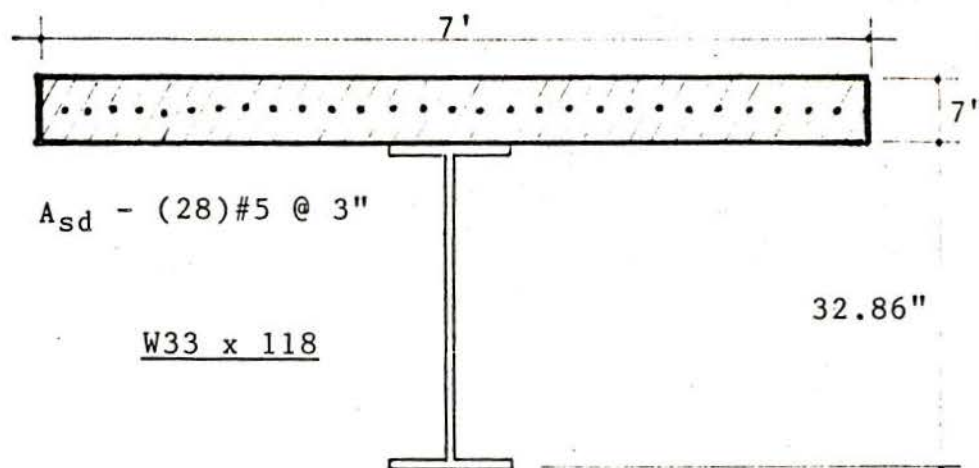


Fig 5.1 - Cross-section.

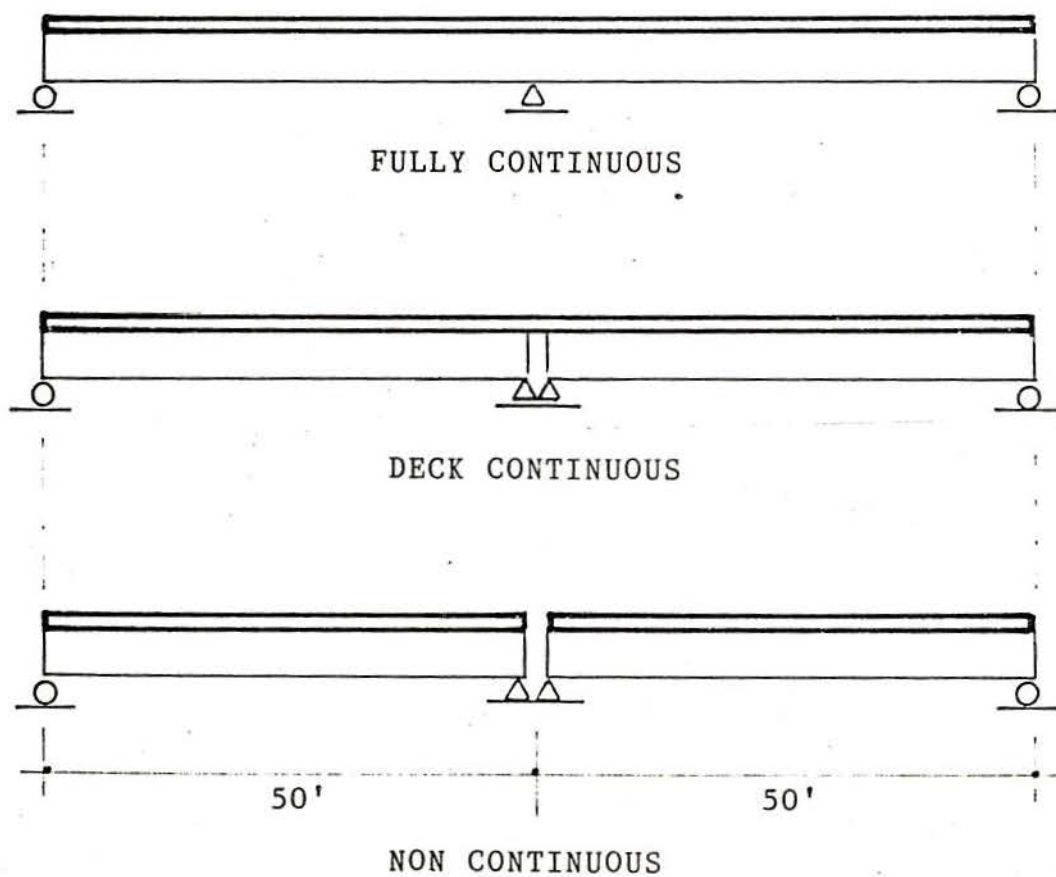


Fig 5.2 - Two-span composite beam with steel girders.

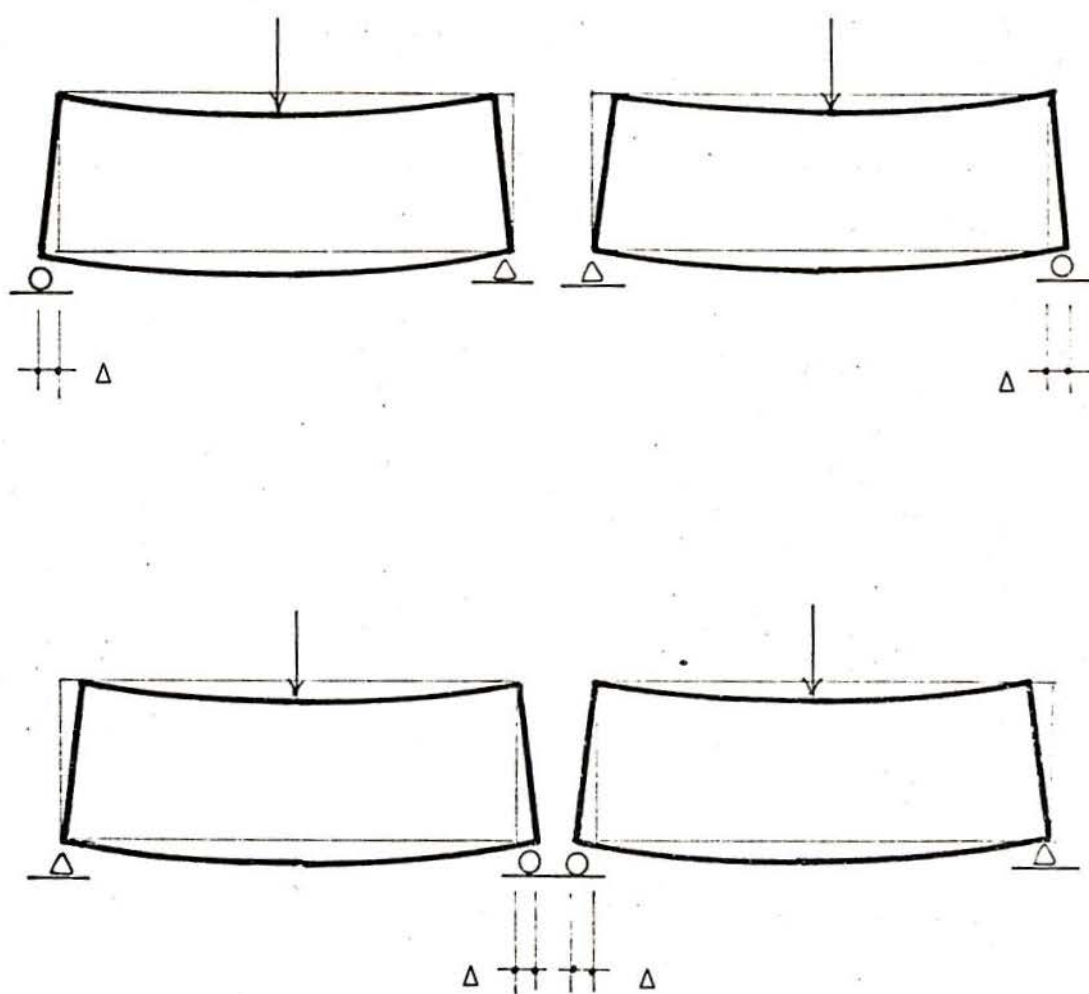


Fig 5.3 - Horizontal movements for different supporting conditions.

performance of these three types of design will be analyzed and compared.

The steel girders are placed into position over the supports, and the concrete deck is cast, either by shored or unshored construction. Supports are provided at the bottom flange of the respective girders, and assumed as hinges, preventing any horizontal movement, or as bearing pads, allowing for some horizontal displacements. Bearing pads are designed according to the procedures outlined in Section 2.4.

When hinges are used, it is assumed that free horizontal movement of the supports is possible only under the action of girder dead load. Horizontal movement of the supports is considered to be restricted for all other superimposed loads on the girders. This supporting condition allows for a more realistic modeling of the structure, since horizontal reactions at the hinges, if any, only appear under the action of live load, or any loading condition following the setting of the hinged supports. The existence of horizontal reactions in the restrictive supports, as well as the force built-up in the deck connection are taken into consideration in the analysis. Should the supports be located at the centroidal plane of the sections, as commonly assumed in basic structural analysis no restricting forces would be generated even if the horizontal movements are prevented.

The deck connection over the intermediate supports is, under any applied loading, subjected to bending and axial force. As shown in Fig. 5.3, depending on the type and arrangement of the supporting conditions, tension or compression may occur at the deck connection, producing a different behavior of the whole structure for each supporting condition.

A numerical analysis is performed by using the Load Increment Method for girders subjected to its own dead load and deck dead load. After composite action is established the beams are analyzed for an increasing uniformly distributed live load up to failure, by using the Displacement Increment Method. Both spans are divided into 12 equal elements, subdivided into 18 and 12 layers for the girders and deck respectively. A connection element is provided when there is deck continuity.

Figure 5.4 shows the load-deflection responses for the deck-continuous beam under different support arrangements, and comparison is made with the extreme cases of a fully-continuous beam and a non-continuous beam. It is assumed that the beams are unshored during the deck construction, and bearing pads are provided at all non-hinged supports. It is interesting to observe that the different beams present a remarkably different behavior, depending on the boundary conditions. Nevertheless, all cases fall within the upper and lower bounds, i.e. fully-continuous and non-continuous cases. The beams in cases 3, 4 and 5, for which a tensile force occurs in the deck connection, behave quite similarly to a non-continuous beam but with slightly less deflections and much less ductility. The maximum load capacity would be governed by yield of the reinforcing steel (assumed at a limiting strain of 1%) in the deck connection.

A compressive force is encountered at the deck connection for the beam in case 2, which yields a much lower moment carrying capacity and ductility, allowing failure to occur by crushing of concrete at the bottom face of the deck. Under loading on one span only, however, as shown in Fig. 5.5, a tensile force is transmitted through the

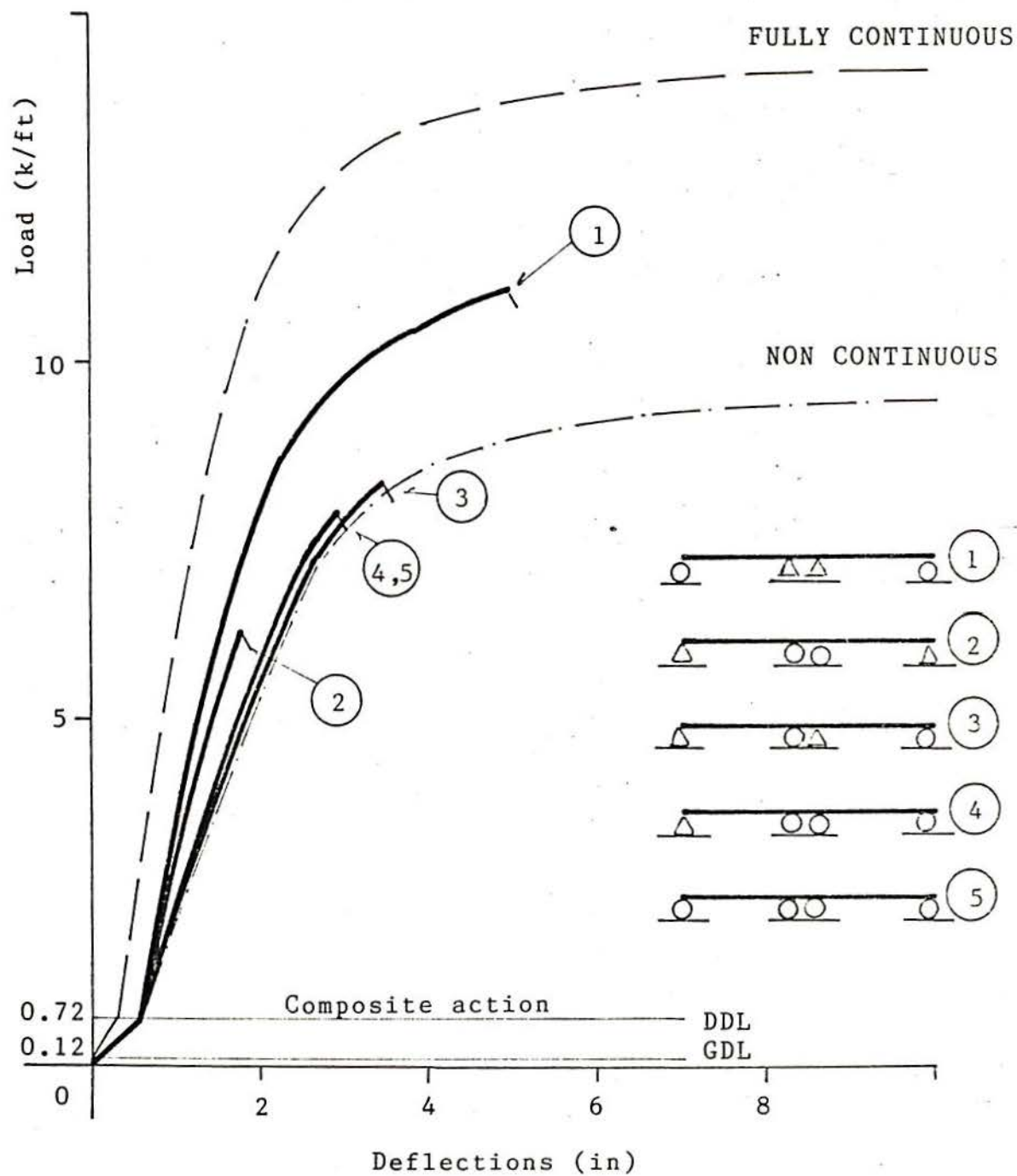


Fig 5.4 - Load-deflection responses under full span loading for various support arrangements. Unshored deck construction.

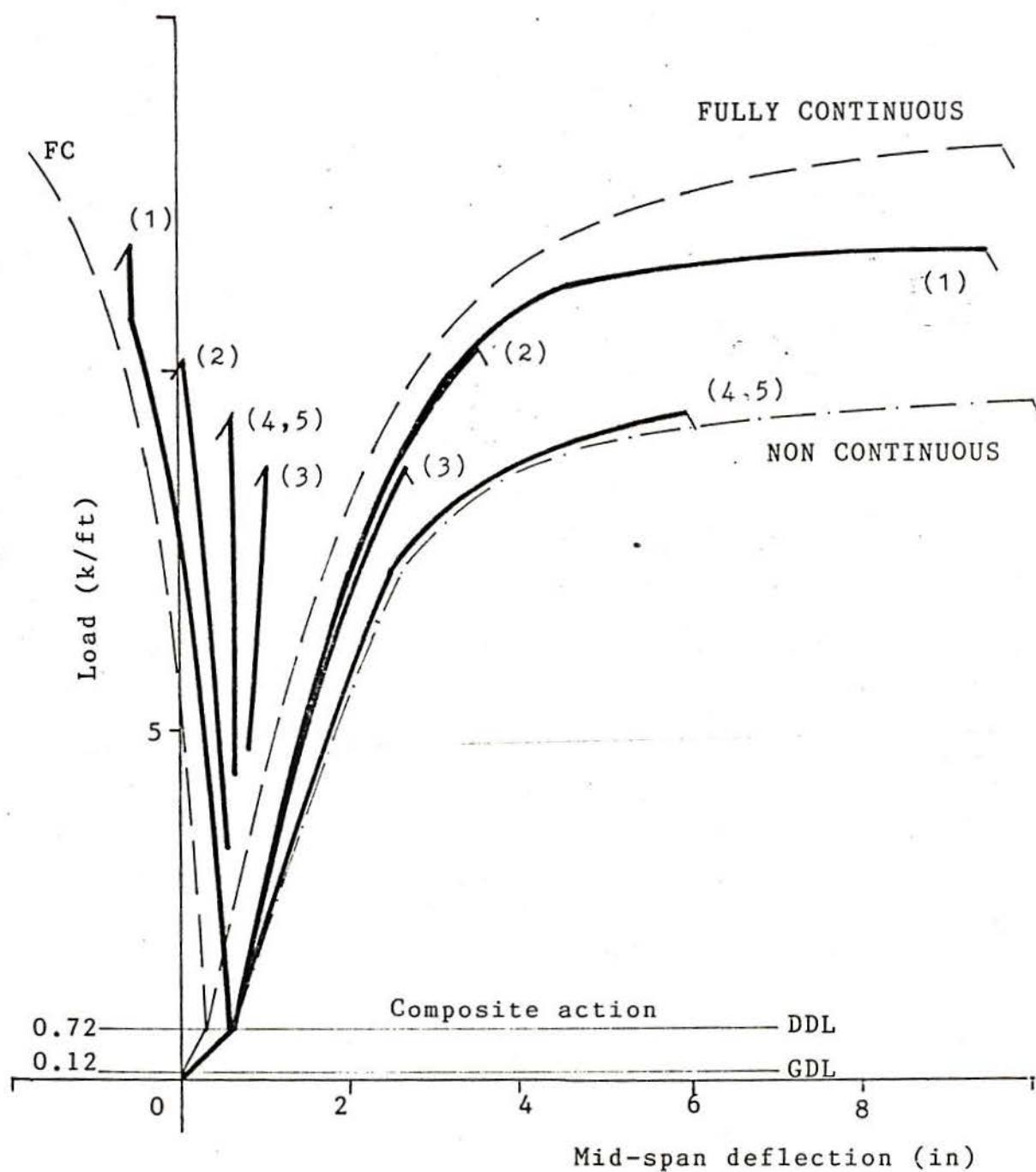


Fig 5.5 - Load-deflection responses under one-span loading. Deflections of both spans for all cases in Fig 5.4.

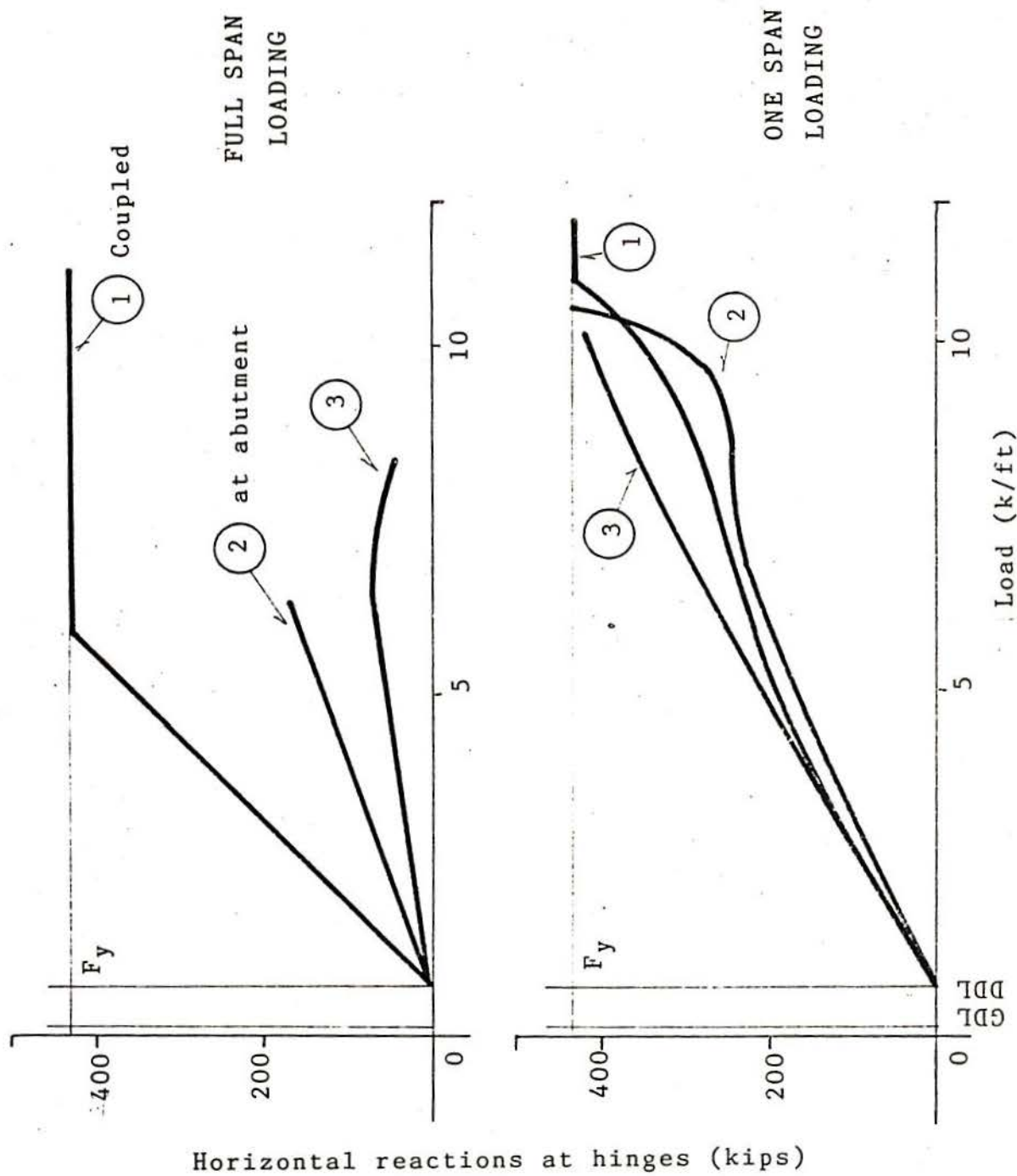


Fig 5.6 - Horizontal reaction build-up for cases in Figs 5.4 and 5.5.

connection, thus enhancing its performance in deflections and strength.

The beam Case 1, having hinges at the intermediate supports, which assure a thorough tensile behavior of the deck connection, performs remarkably better than the beams of all other cases, under either symmetric or unsymmetric loading. Deflections at the service load range are comparable to the case of full continuity, as seen in Figs. 5.4 and 5.5. It is also true for the case of shored construction as shown in Fig. 5.8. Failure is obtained by extensive yielding of the reinforcing steel, at the connection, and its ultimate load capacity is well above that of a non-continuous beam.

The horizontal reactions supported by the hinges for the situation of full span loading in Case 1 are well above those for the remaining cases, as shown in Fig. 5.6, but comparable to the other cases for one span loading. However the reactions are coupled over one single support, thus allowing for the use of some local resisting device. For the beams in Cases 2 and 3, even though the reactions are of smaller magnitude they must be supported by the end abutments or by a single intermediate hinge.

From the observations made to this point, it is concluded that:

a) Cases 4 and 5 appear to be a good alternative for the case of non continuity. Their service load range behavior is better, as far as deflections are concerned and, more importantly, they do eliminate the undesirable joint. No horizontal reactions are created at the supports. After yielding of the deck connection reinforcement steel, the beams will behave as if a joint were provided at that location, thus gaining

all the ductility capacity provided by the non-continuous beams.

b) If hinges are used they should be placed in pairs over the intermediate supports as in Case 1. The behavior of the beams is enhanced remarkably in deflections, strength and ductility. It constitutes a valid, more economical alternative for a fully continuous structure.

5.2.2 Deck-Continuity Over Hinged Supports

Among the different beams analyzed previously the beam supported as in Case 1, with deck-continuity over hinged supports, presented an interesting behavior. Its response under uniformly distributed load is the closest to the response of a fully-continuous beam under the same loading conditions. Further analyses are made to compare the responses of both FCB and FCD under this and other situations of loading. Some conclusions are described next.

(a) Linear Response

From Figs. 5.7 and 5.8 it is observed that both beams present a very similar stiffness within service load range. Linearity extends up to a load level approximately eight times the total dead load, for either shored or unshored construction.

(b) First Cracking

First cracking of the deck slab occurs at a load level about four times the total dead load. Cracking is first developed in a region near the internal supports, as shown by point 2 in Fig. 5.7. Cracking of the

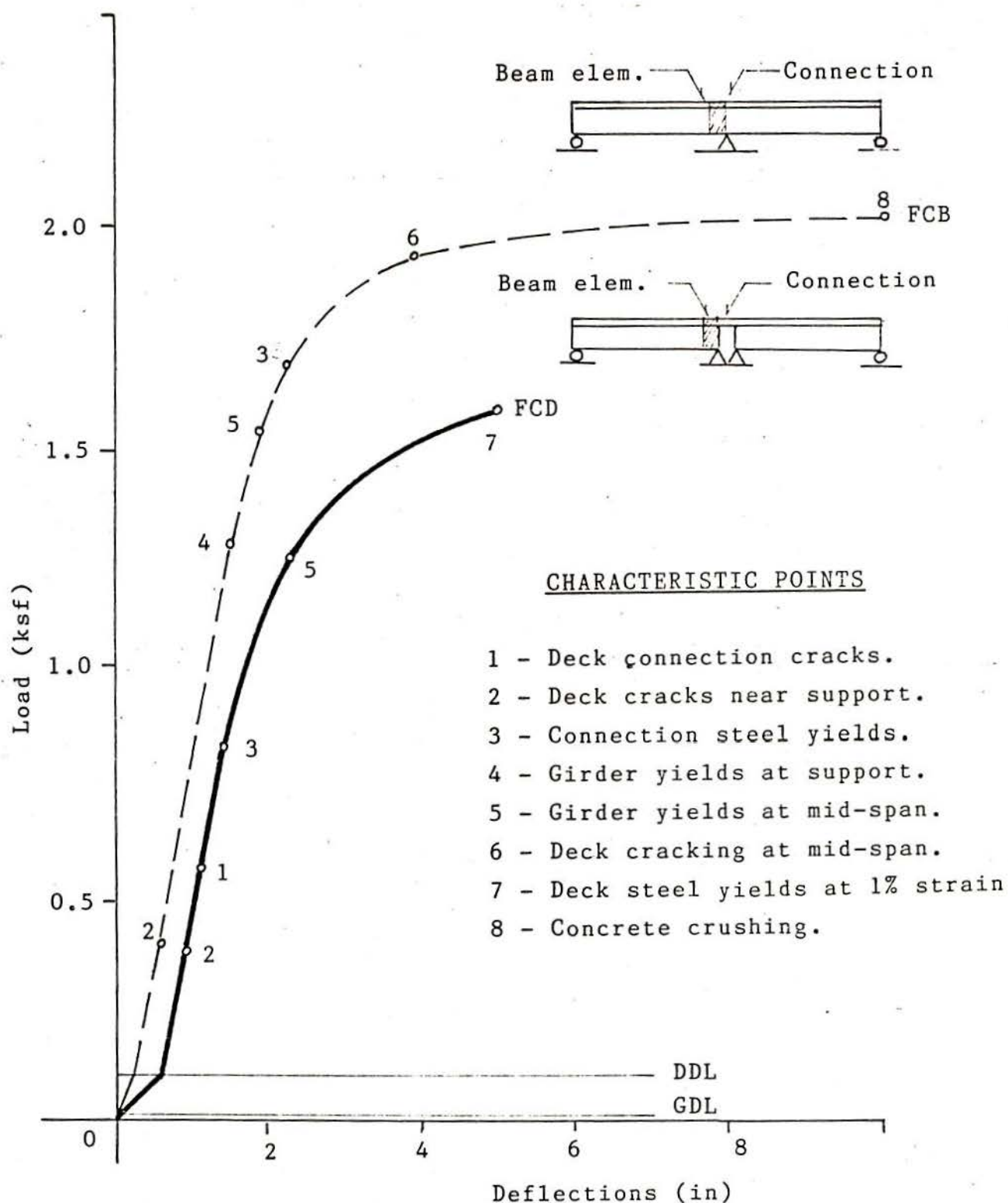


Fig 5.7 - Load-deflection responses for the FCB and FCD beams, both under unshored deck construction and loaded at both spans.

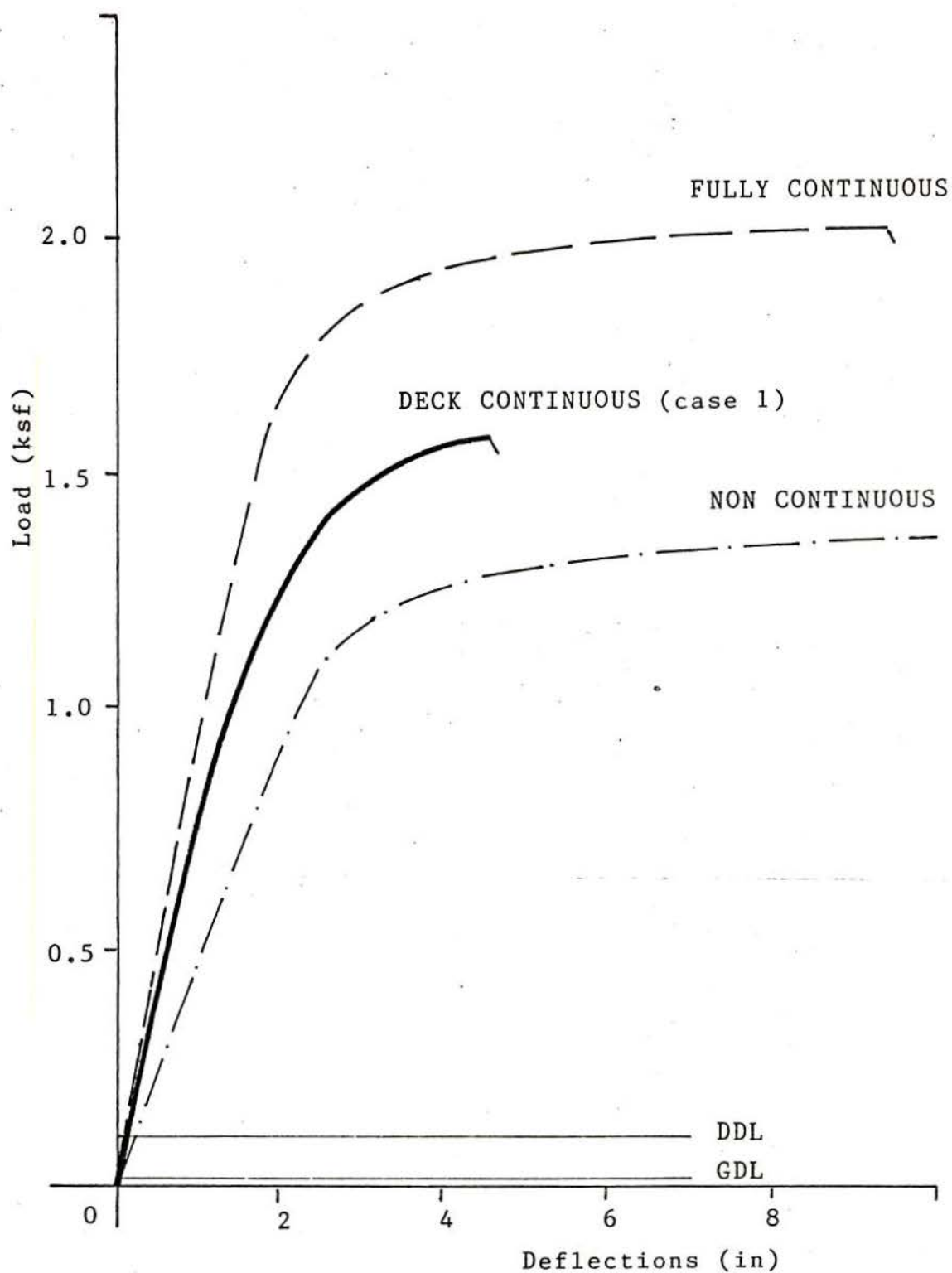


Fig 5.8 - Load-deflection responses for beams under full span loading and with shored deck construction.

deck connection in the FCD beam follows closely, at five times the total dead load (point 1).

(c) Yielding of the Deck Reinforcement

Yielding of the deck reinforcement in the FCD beam (point 3) occurs at a load level eight times the total dead load, when the beam response becomes nonlinear. However, in the FCB deck reinforcement yield happens at a much higher load, after yielding of the steel girders (points 4 and 5).

Force build-up in the deck connection of the FCD beam is virtually linear before yielding of the reinforcement. After that a constant force is maintained until failure, see Fig. 5.9. The development of stresses in the deck reinforcing steel of both beams is shown in Fig. 5.10. It can be observed that under service load conditions, when cracks are expected to be controlled, steel stresses remain in the elastic range therefore allowing cracks to close under unloading of the structure.

(d) Load Capacity

Failure of the FCD beam occurs by extensive yielding of the deck reinforcement whereas in the FCB crushing of the deck concrete is observed after a considerable mid-span deflection, and at a higher load as shown in Fig. 5.7. However, the load capacity of a deck-continuous beam may be enhanced by increasing the amount of deck reinforcement at the connection. Fig. 5.11 shows a comparison of their responses for different reinforcement ratios of 1.5, 2.0, 2.5 and 3.0 percent respectively. The same amount of deck reinforcement is maintained for

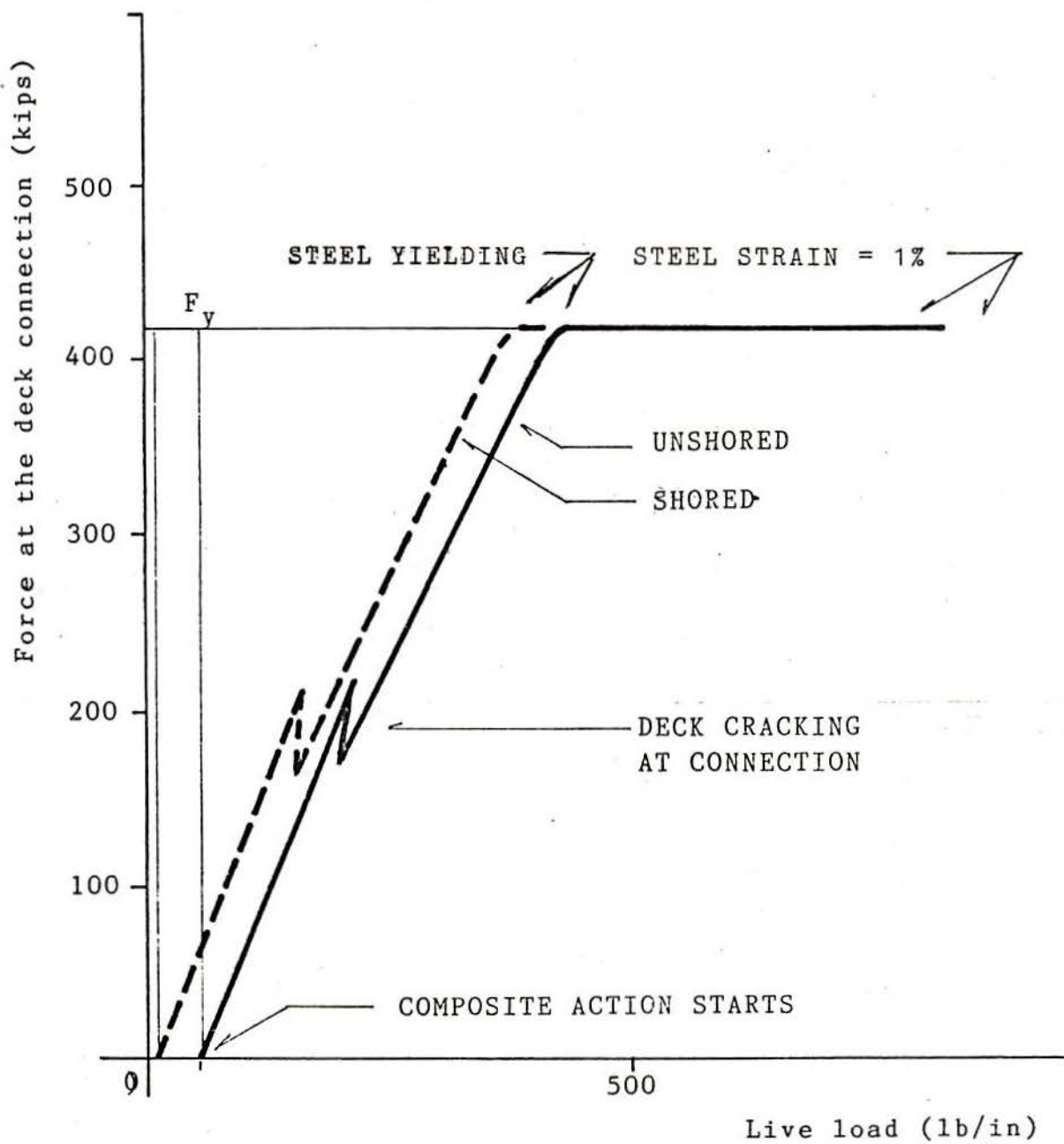
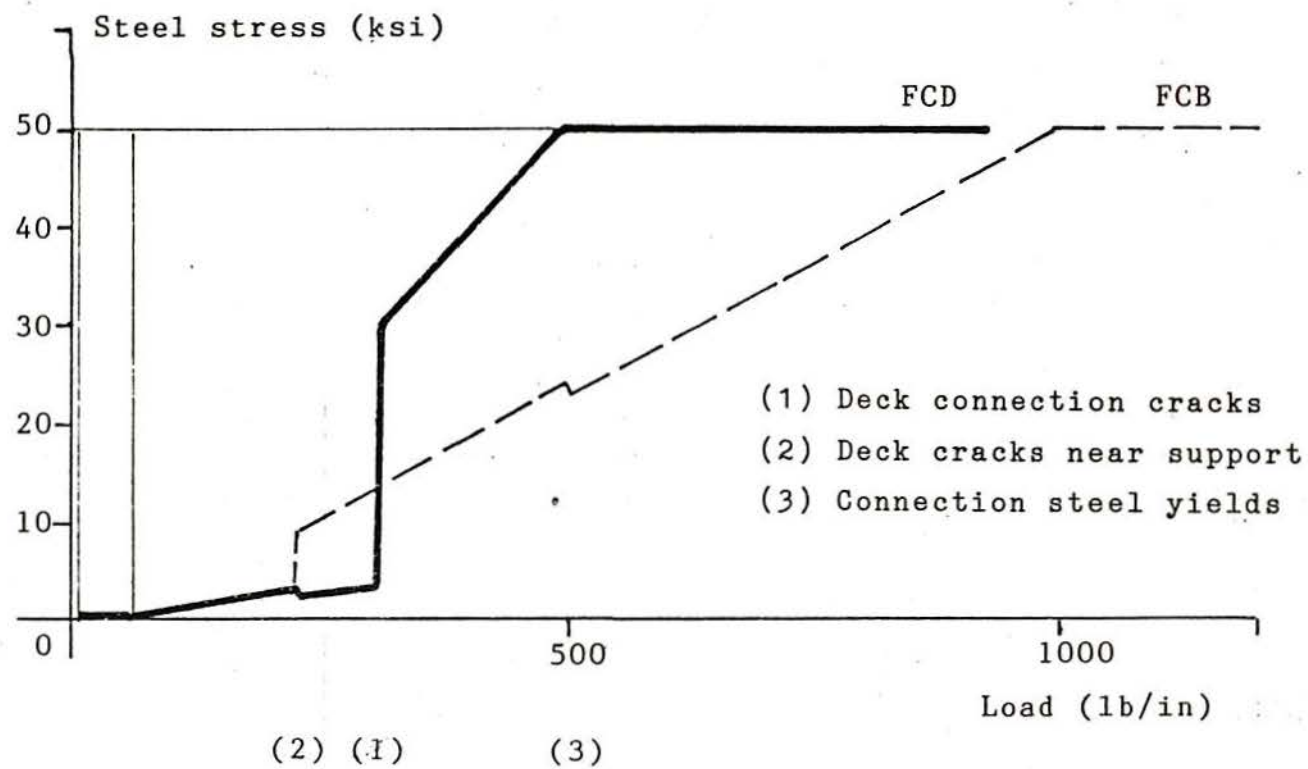


Fig 5.9 - Force build-up at the deck connection.
 Beam case 1: Full span loading, shored
 and unshored deck construction.

Fig 5.10 - Stresses in the deck reinforcing steel for full span loading and unshored construction.
Refer to Fig. 5.7.



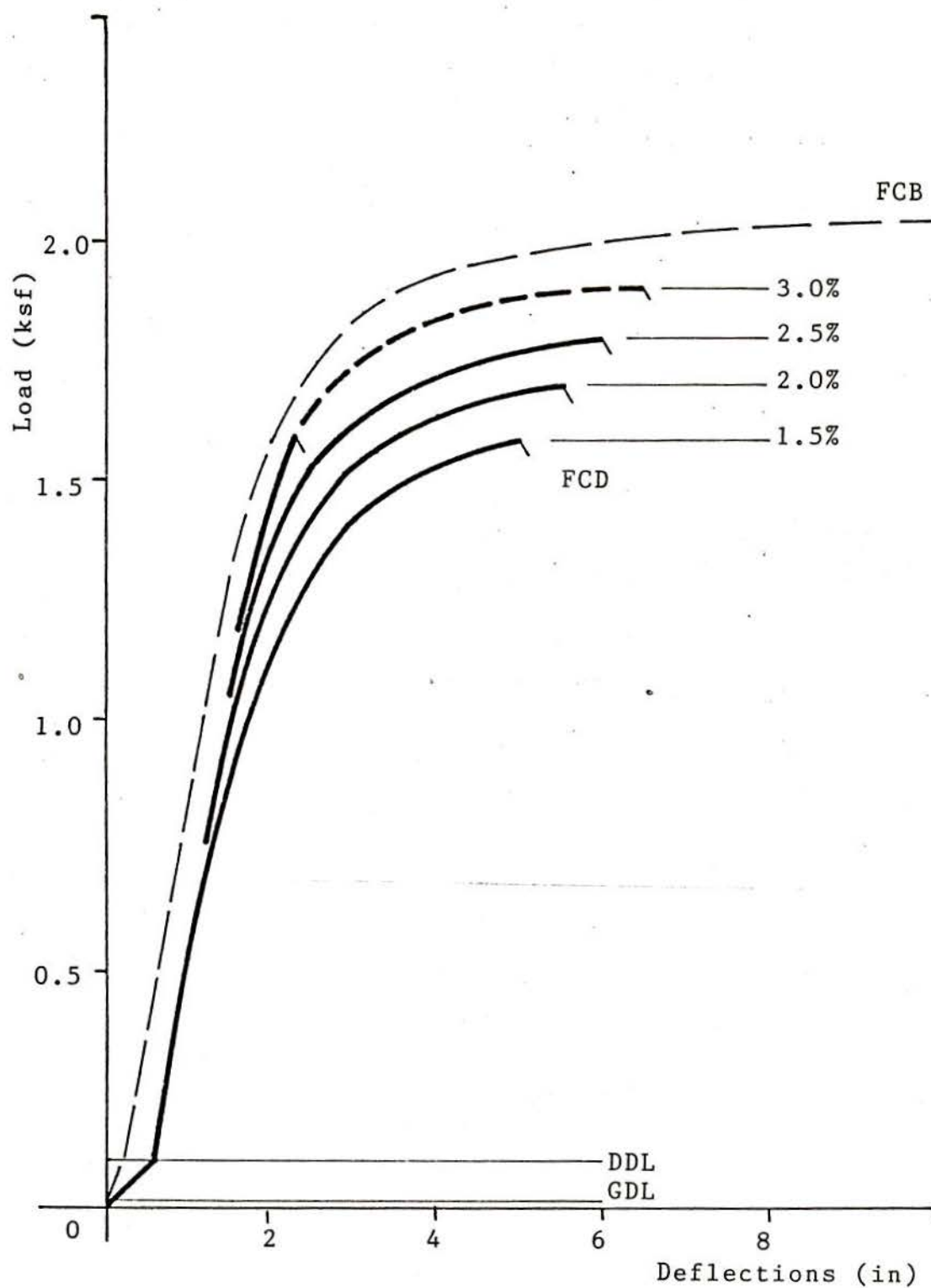


Fig 5.11 - Load-deflection responses for continuous deck beams, Case 1, with different reinforcement ratios at the connection. Unshored construction and full span loading.

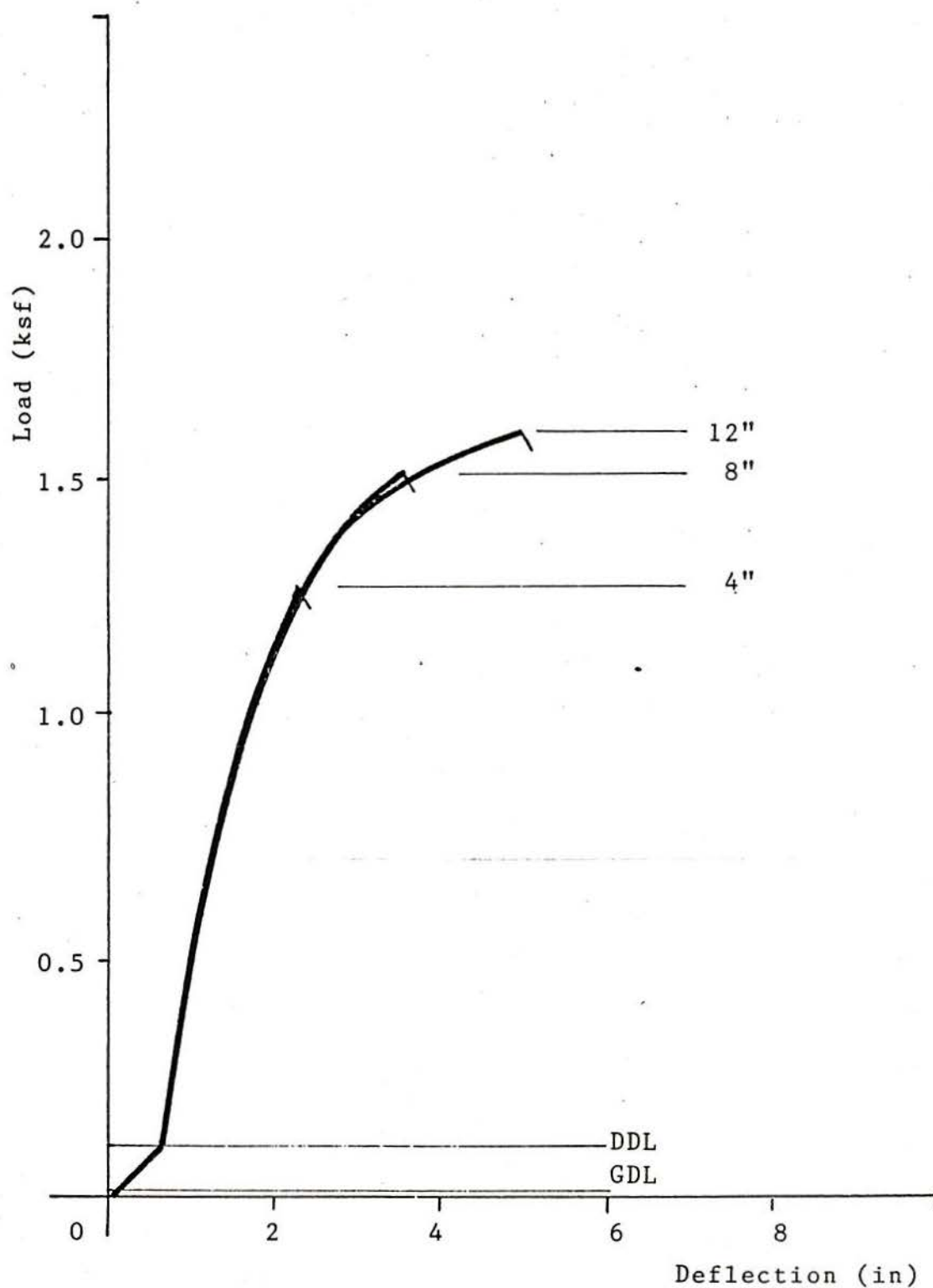


Fig 5.12 - Responses of a deck-continuous beam with different widths of the deck connection. Unshored deck construction and full span loading.

the spans. It is observed that the beam response comes closer and closer to the response of the FCB. But for reinforcement ratios of 3.0 percent and more the deck becomes over-reinforced causing failure to occur by crushing of concrete with much less ductility.

(e) Ductility Capacity

Ductility and strength of a FCD beam are associated with the width of the concrete deck connection. The shorter is the gap between adjacent girders the higher is the strain associated with the same amount of rotation of the end faces of the girders, thus allowing failure to occur prematurely. However, their responses under service loads are not differentiated by this variable, as shown in Fig. 5.12.

A wider deck connection could be achieved by separating the end faces of the adjacent girders, but a more robust support would be required. Yet, another solution could be to provide some small region near the gap to be unbonded, i.e. the deck-girder interface at both sides of the end faces of the girders could be left unbonded when casting the deck slab. The analytical model developed herein is not able to handle such a situation. However, should the unbonded length be kept small it is expected that the results of this analysis may be adequate.

(f) Sustained Loading

The development of mid-span deflections over a period of two years under a sustained live load is shown in Fig. 5.13. During this period, shrinkage and creep of the deck concrete are expected to cause the initial deflections to increase. It is once more observed that a FCD

beam behaves similarly to a FCB, unlike the non-continuous one. A non-continuous beam has a 70 percent increase in deflection whereas the other two beams present an initial increment of about 50 percent, in a six months period, decreasing to a steady 30 percent after two years. It is worth noting that such responses correspond to a post-cracking behavior of the decks, as seen in Fig. 5.7.

(g) Temperature Effect

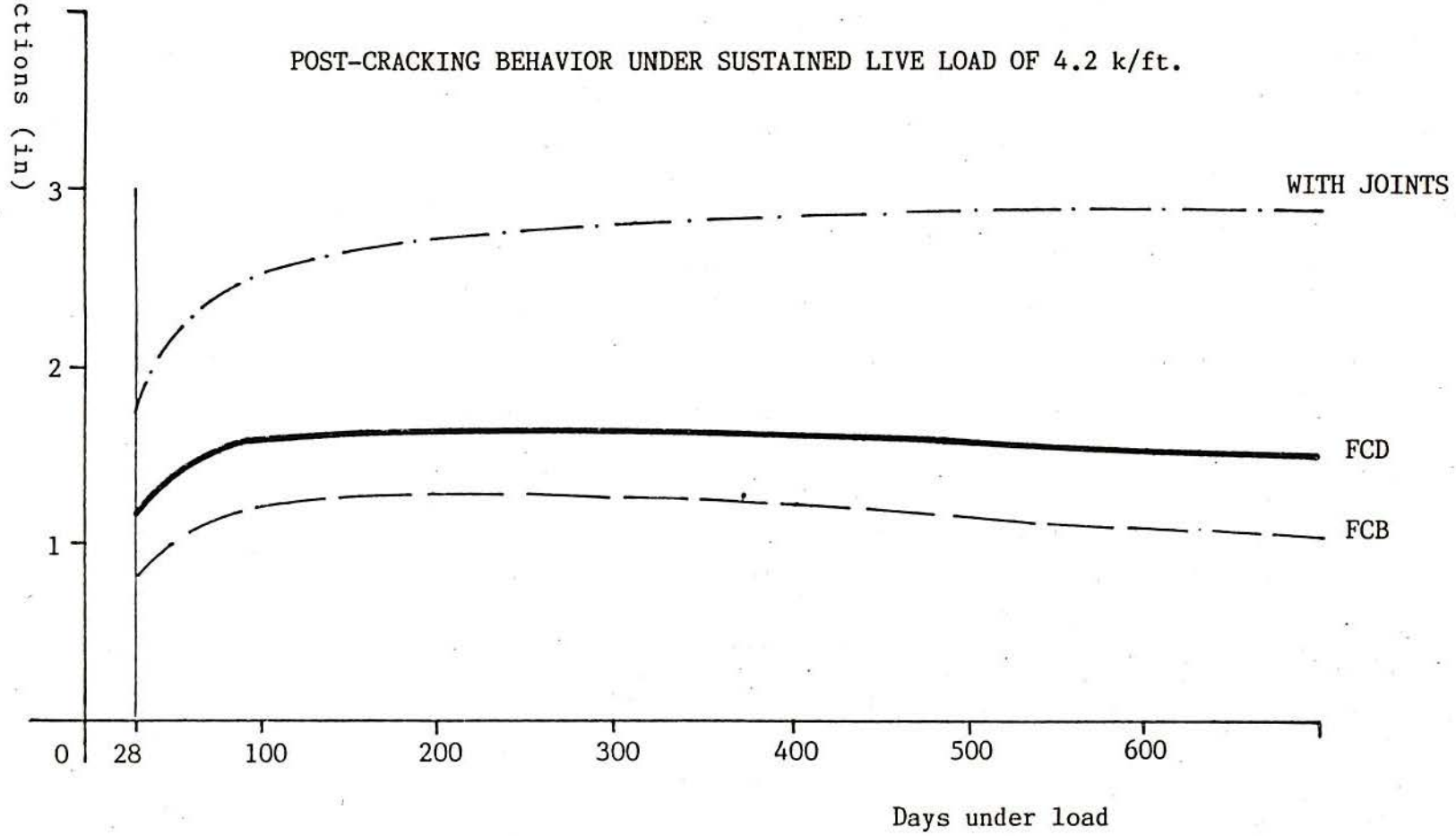
Under the action of the same service live load the beams are also analyzed for the effects of two temperature variation gradients. A constant temperature variation through the cross-sections is assumed to model a seasonal temperature change. For a daily oscillation of temperature a linearly decreasing gradient is used, as seen in Fig. 5.14. No significant changes in deflections nor in cracking development are noted for any of the beams analyzed.

(h) Compressive Effect

An amazingly similar response is presented by the three beams when all supports are hinged, i.e. when no horizontal movement is permitted after dead load is applied. In this situation horizontal reactions are created at the hinges. The compressive effect provided by these reactions overwhelmingly dictates a tremendously stiff response of the beams. Their load capacity are nearly doubled and their load-deflection responses become barely distinguishable, as shown in Fig. 5.15.

In this situation it is undoubtedly clear the superiority of a FCD beam over the other two beams. Such constructional scheme will avoid the use of expansion joints and yet permit the use of precast elements

Fig 5.13 - Development of mid-span deflections with time.
(Refer to Fig 5.4)



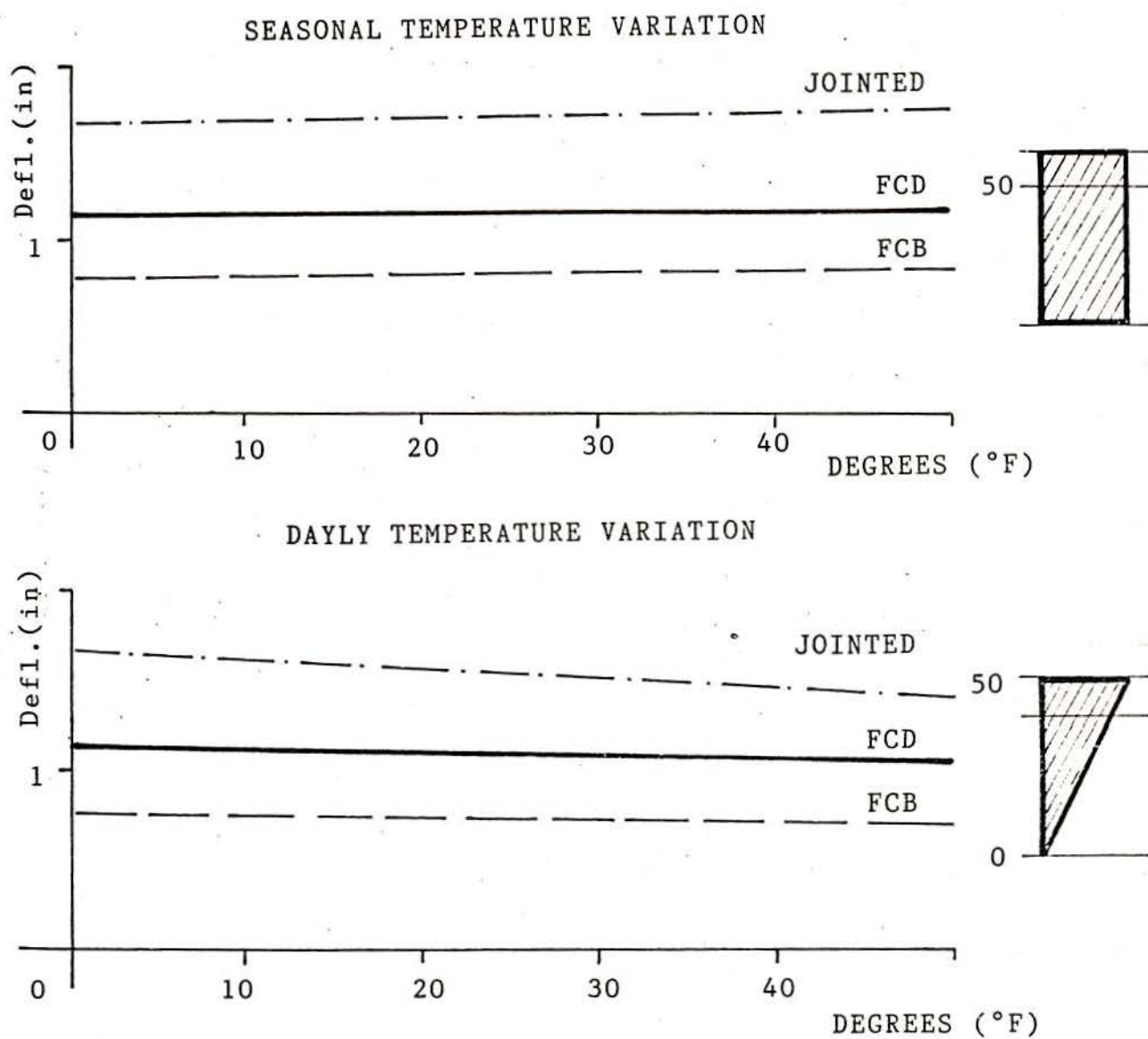


Fig 5.14 - Development of mid-span deflections for temperature variation. (Refer to Fig 5.4)

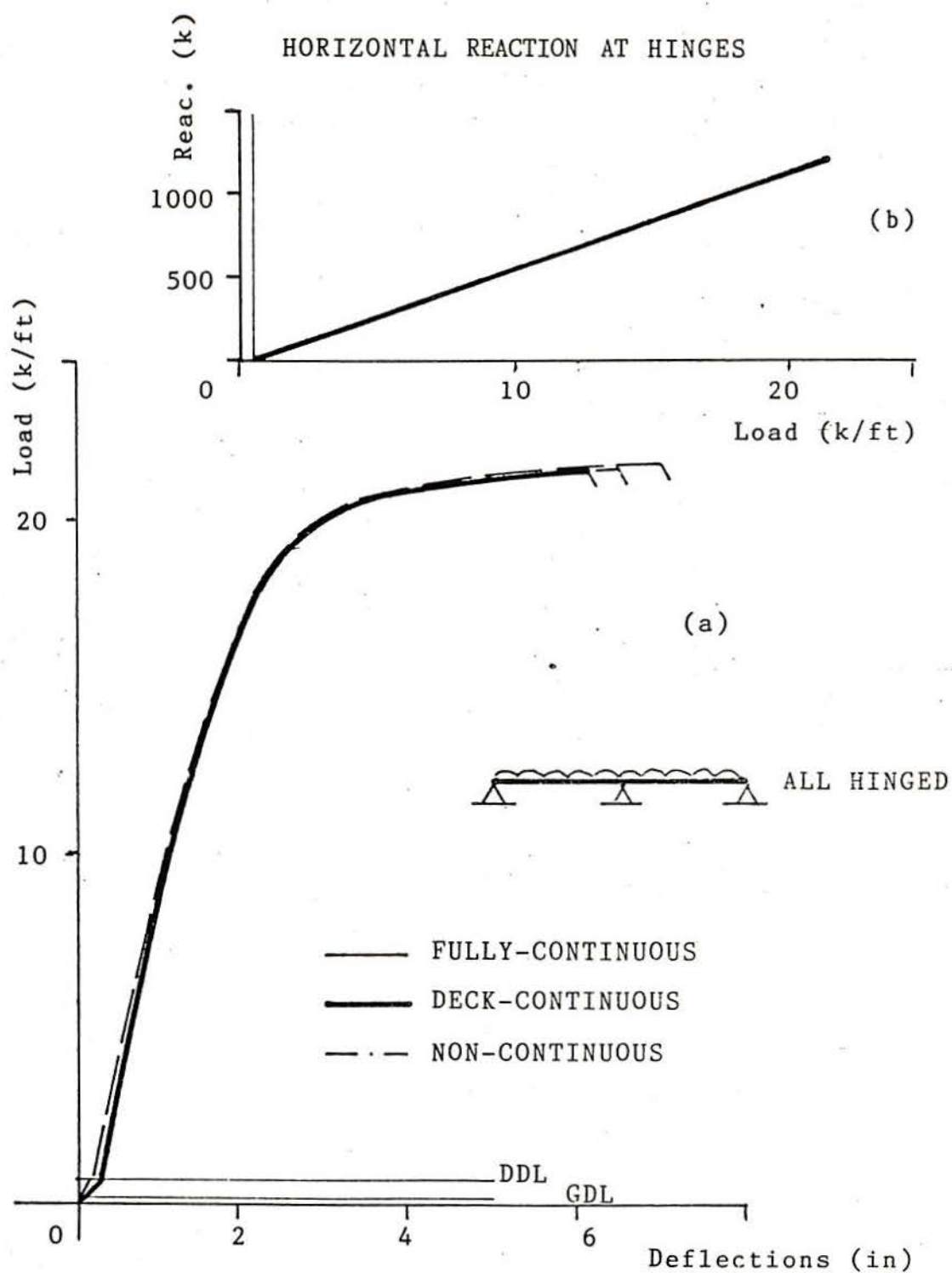


Fig 5.15 - Load-deflection response for beams loaded on full span and hinged at all supports (a). Horizontal reactions at the exterior hinges (b).

therefore lowering the cost associated with construction and maintenance.

The results presented up to this point predict the behavior of a particular two-span beam composed of steel girders and a reinforced concrete deck slab. A good performance is observed by the deck-continuous beam as compared to the upper and lower bound cases of full and no continuity. It is expected that similar conclusions may be extended to beams with more than two spans.

5.3 Analysis of a Jointless-Deck on Four-Span Beam With Precast Prestressed Concrete Girders.

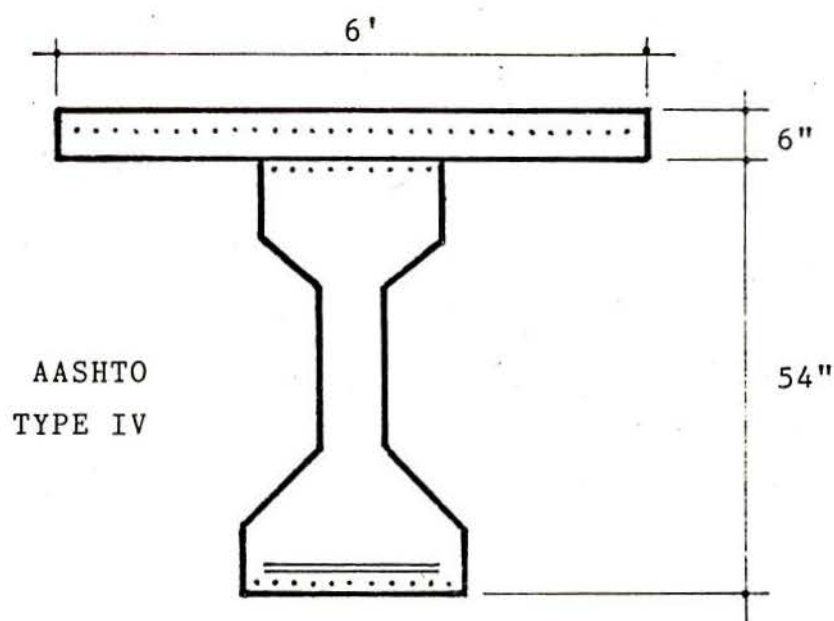
5.3.1 Properties

A four-span bridge beam, composed of four pre-tensioned concrete girders and a 6 ft by 6 in reinforced concrete deck slab, is analyzed to study the performance of a joint-free fully-continuous deck system. Comparison is made to beams with no continuity and full continuity for live load only. Layout, cross-sections and material properties are shown in Figs. 5.16, 5.17 and 5.18. Two situations are considered:

(a) The beams have four equal spans, each with a 66 ft precast pre-tensioned AASHTO TYPE IV girder.

(b) The beams have four unequal spans, with two exterior spans of a 24 ft precast pre-tensioned AASHTO TYPE II girder and two interior spans being the same as in case (a).

All girders are pre-tensioned by straight 7-wire strands 270 K grade

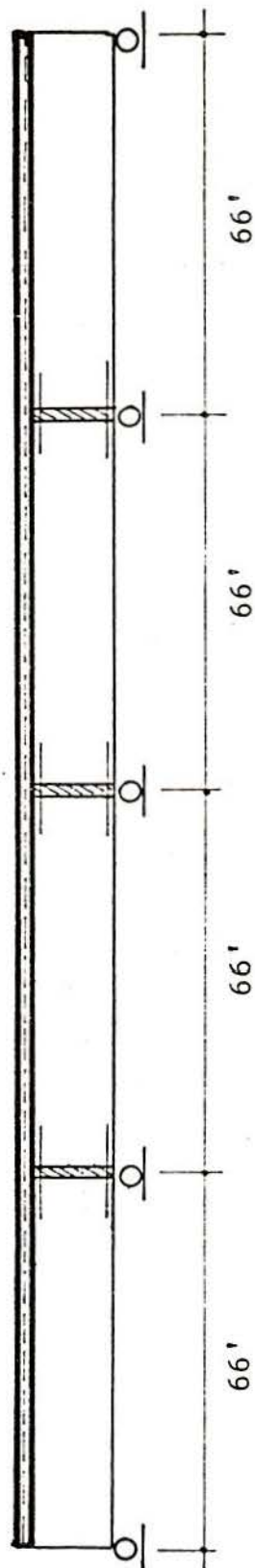


CROSS-SECTION AT FOUR SPANS

<u>Girders</u>		<u>Deck</u>	
$A_c = 789 \text{ in}^2$		$A_s = 432 \text{ in}^2$	
$I_c = 260741 \text{ in}^4$		$W_t = 450 \text{ plf}$	
$W_t = 822 \text{ plf}$		$E_c = 3.5 \cdot 10^6 \text{ psi}$	
$E_c = 4.5 \cdot 10^6 \text{ psi}$		$f_c = 3500 \text{ psi}$	
$f_c = 6000 \text{ psi}$			
<u>Reinforcement</u>		<u>Prestressing</u>	
	span		(32) 7 wire strands
			$f_{pu} = 270 \text{ ksi}$
deck	1.5%		$f_{pi} = 0.7 f_{pu}$
			$A_{ps} = 2.72 \text{ in}^2$
girders			$e = 21.73 \text{ in}$
	supports		
	2.6%		
	$A_s = 2 \text{ in}^2$		
	$A_s = 2 \text{ in}^2$		

Fig 5.16 - Cross-section and material properties
for the beam with four equal spans.

264 ft - FOUR EQUAL SPANS BEAM



180 ft - FOUR UNEQUAL SPANS BEAM

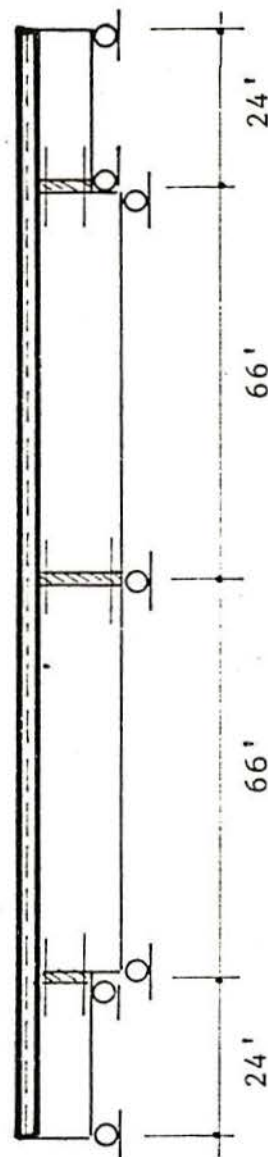
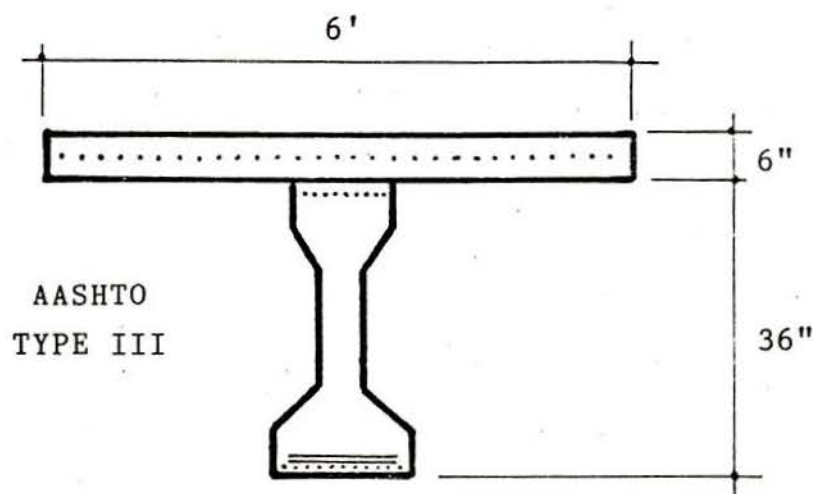


Fig 5.17 - Layout and reinforcement arrangement for both prestressed concrete composite beams.



CROSS-SECTION AT SHORTER SPANS

$$A_g = 369 \text{ in}^2$$

$$I_g = 50797 \text{ in}^4$$

$$W_t = 384 \text{ plf}$$

	<u>Reinforcement</u>		<u>Prestressing</u>
	spans	supports	(14) 7 wire strands
deck	1.5%	2.6%	$f_{pu} = 270 \text{ ksi}$
			$f_{pi} = 0.7 f_{pu}$
girders		$A'_S = 1.2 \text{ in}^2$	$A_{ps} = 1.19 \text{ in}^2$
		$A_S = 1.2 \text{ in}^2$	$e = 12 \text{ in}$

Fig 5.18.-- Cross-section and material properties for the two shorter spans.

low-relaxation steel at an initial stress $f_i = 0.7$ fpu. Prestressing is designed for zero stress at top girders under dead load. Reinforcement of 1.5% is also provided in the deck for the entire span. Additional deck reinforcement of 1.1% is also provided over the intermediate support. For the beams with full continuity for live load additional girder reinforcement is provided for negative and positive moments at the supports and the gap between adjacent girders is filled with concrete to assure perfect girder continuity. Unshored construction is assumed and bearing pads are provided for all supports. If hinges are used, they are effective only after dead load is applied.

5.3.2 Modeling

The analysis is performed by modeling the beams by 12 and 11 elements for the short and long spans respectively. All elements are subdivided into 20 layers for the girders and 10 for the deck. For the deck-continuous beams three connection elements are provided, one at the junction of each two adjacent girders. Prestressing and dead loads are applied by using the Load Increment Method and the Displacement Increment Method is used for applying live load up to failure. Various situations of loading, supports, temperature and time effects are studied and the results lead the observations that follow.

5.3.3 Results

(a) Equal Spans and Loading

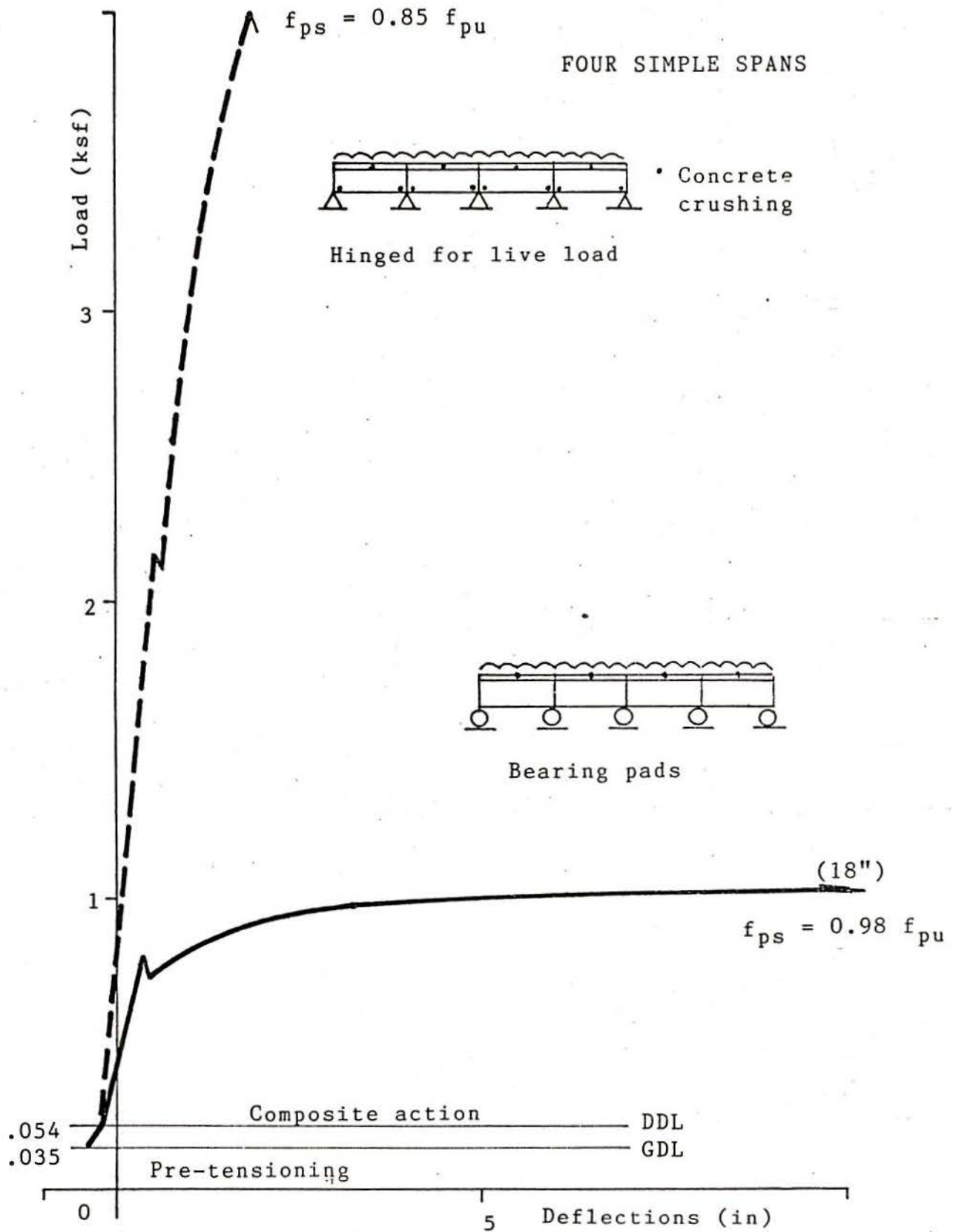


Fig 5.19 - Load-deflection responses under full span loading.

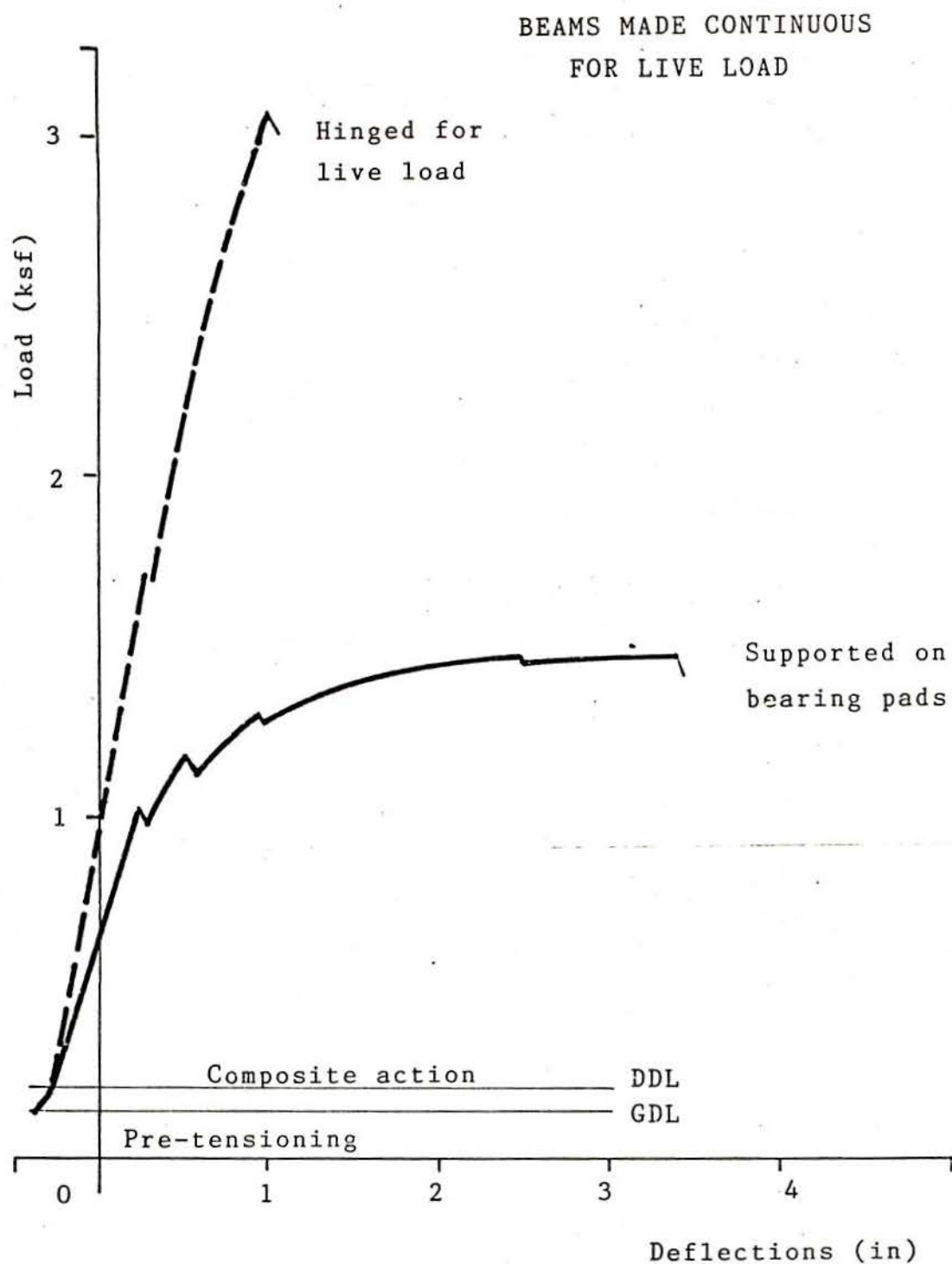


Fig 5.20 - Load-deflection responses under full span loading for the beams made continuous for live load.

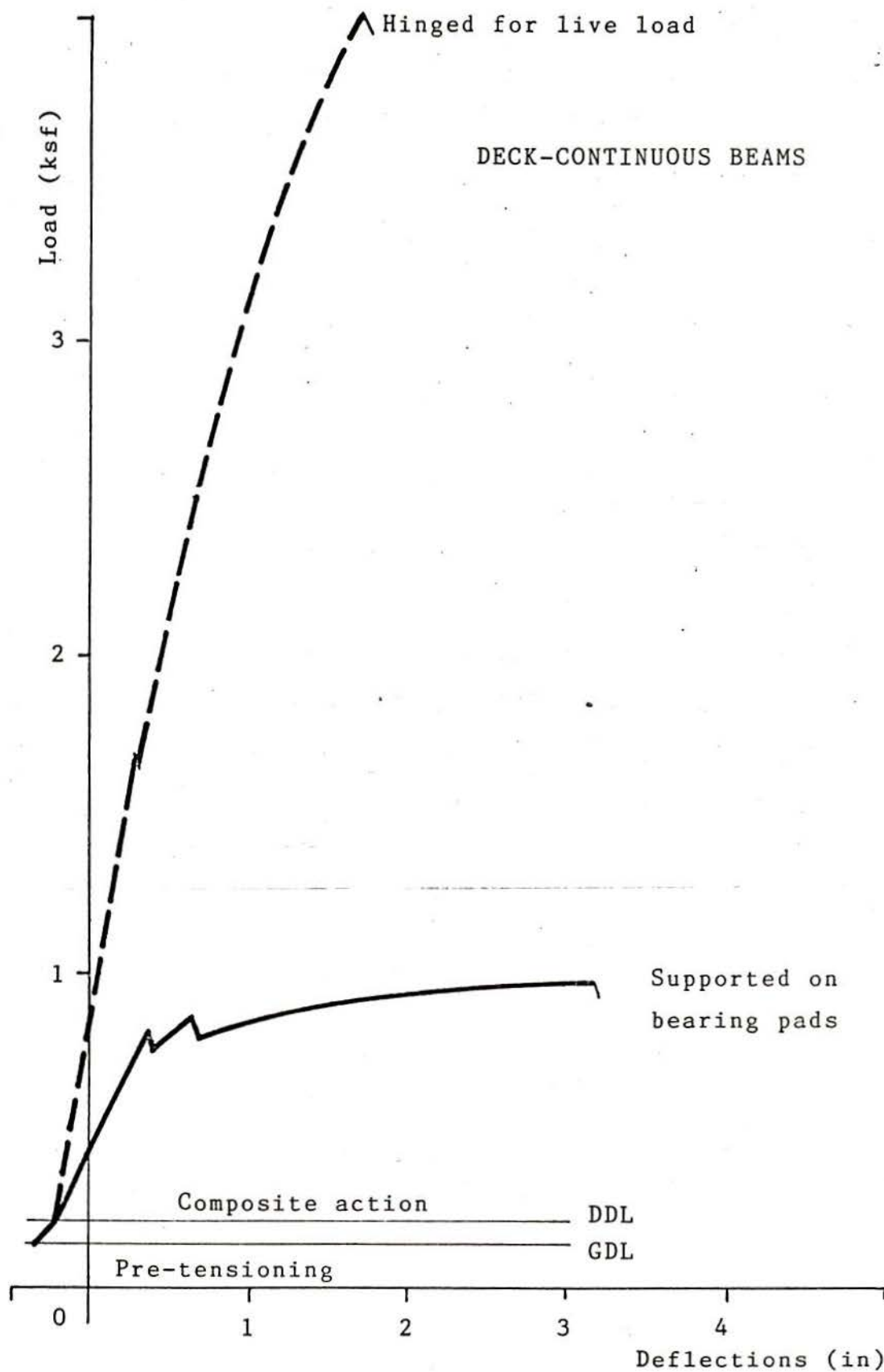


Fig 5.21 - Load-deflection responses under full span loading.

Figures 5.19, 5.20 and 5.21 show the load-deflection responses for the three cases of non continuity, full continuity for live load and deck continuity only, respectively. Beams are loaded on the entire span and two situations of supports are considered: bearing pads and hinges for live load. Deflections are measured at center of the exterior spans for all beams.

When supported by bearing pads, the beams show a rather ductile behavior, especially for the non-continuous cases failing by crushing of concrete at mid-span. Their stiffnesses are greatly increased when hinges are considered but failure is sudden, by concrete crushing at the hinges with no ductility plateau whatsoever.

(b) Equal Spans and Unequal Loading

Comparison is shown for the three continuity cases, in Figs. 5.22, 5.23 and 5.24, where beams are supported by bearing pads and loaded at different spans: fully-loaded, exterior and interior, respectively. The most critical loading condition appears to be the case where all spans are fully loaded. Other conditions of loading, not shown, seem to have less effect in deflections. The same applies to the hinged beams shown in Figs. 5.25, 5.26 and 5.27.

From the observed results conclusions that can be drawn are not much different from the ones outlined in Section 5.2 for steel girders. The deck-continuous beam behaves quite similarly to a non-continuous beam, even though slightly improved when supported by bearing pads. When hinges are used, its behavior becomes comparable to the behavior of a fully-continuous beam.

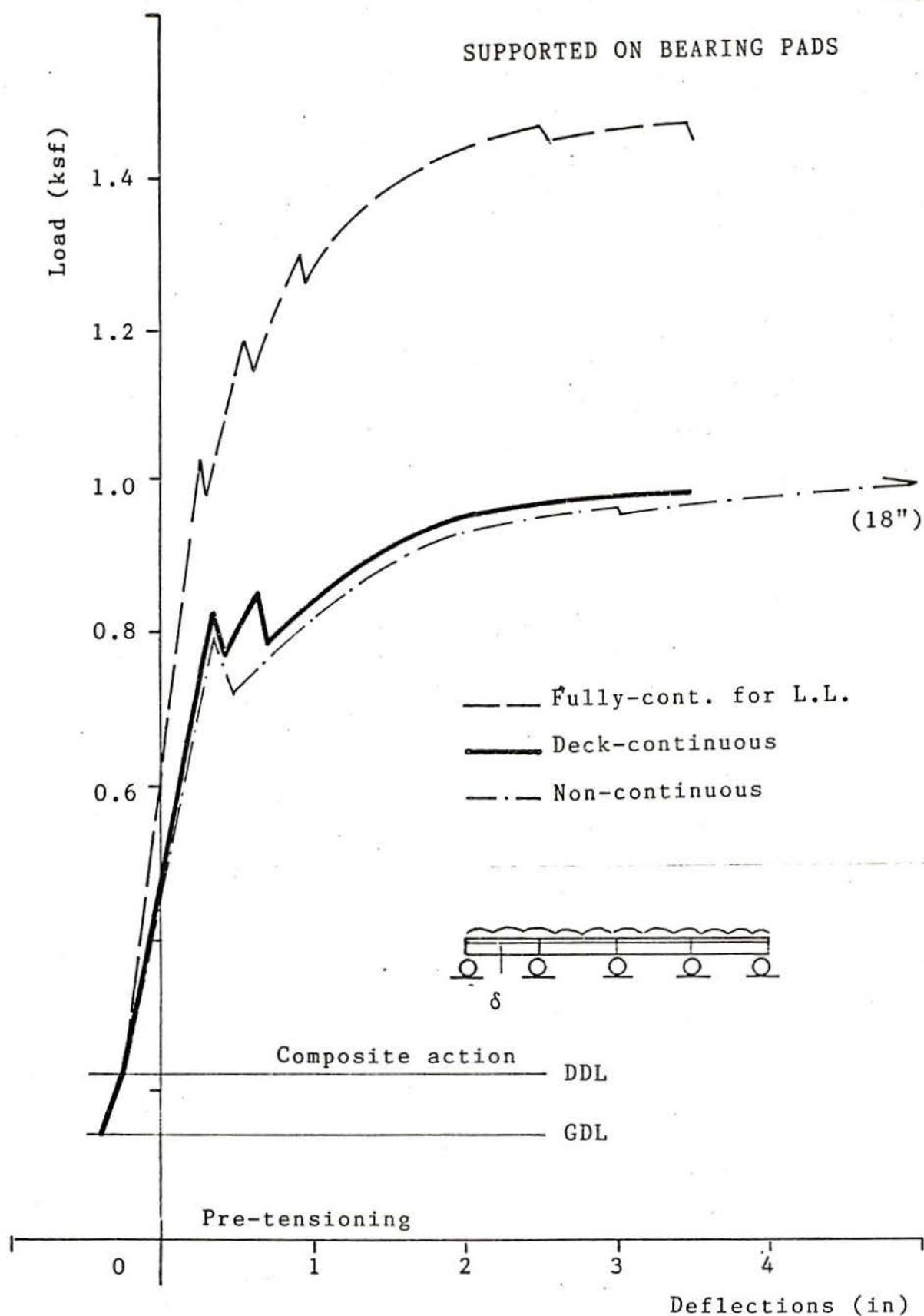


Fig 5.22 - Load-deflection responses under full span loading.

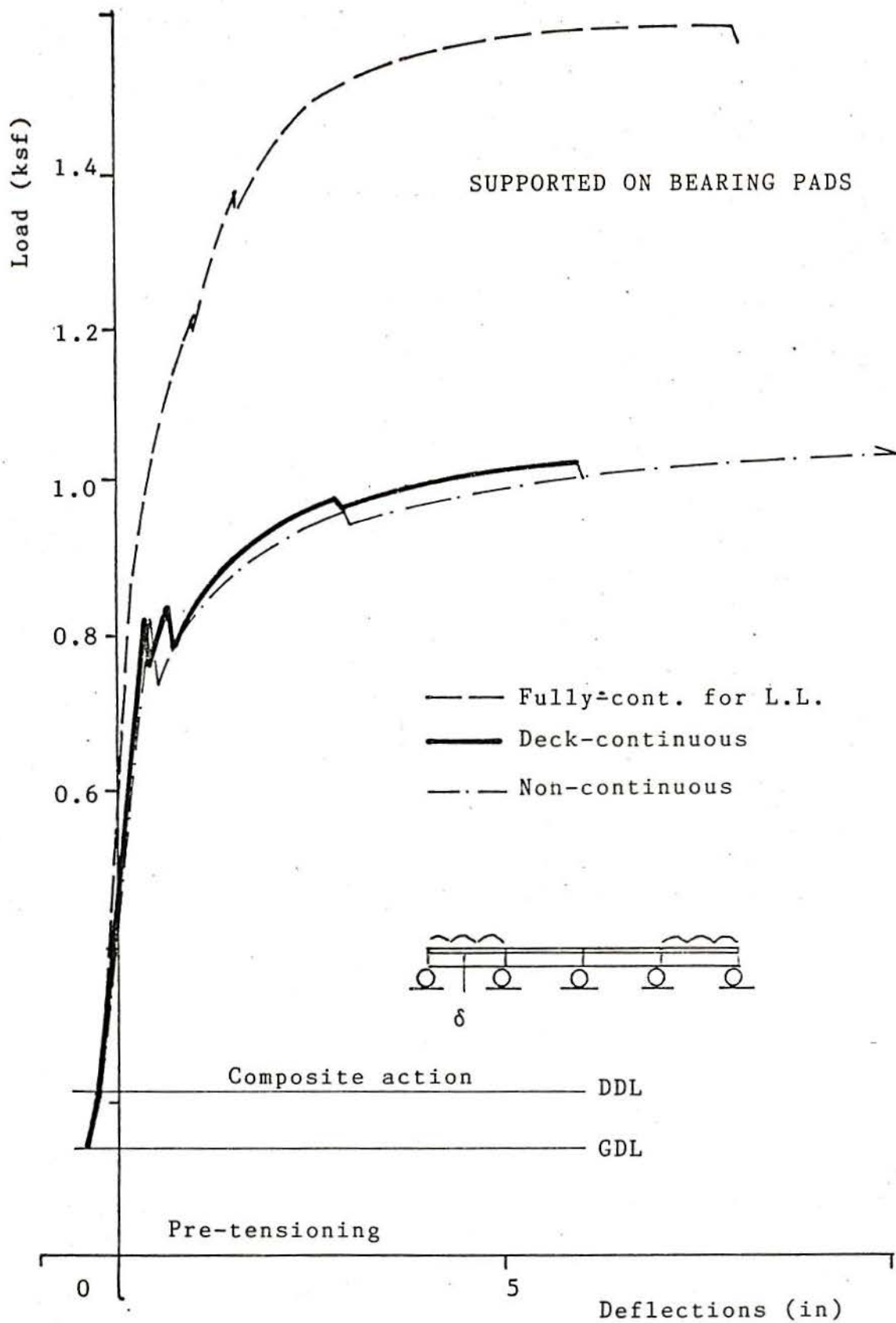


Fig 5.23 - Load-deflection responses for exterior spans loading.

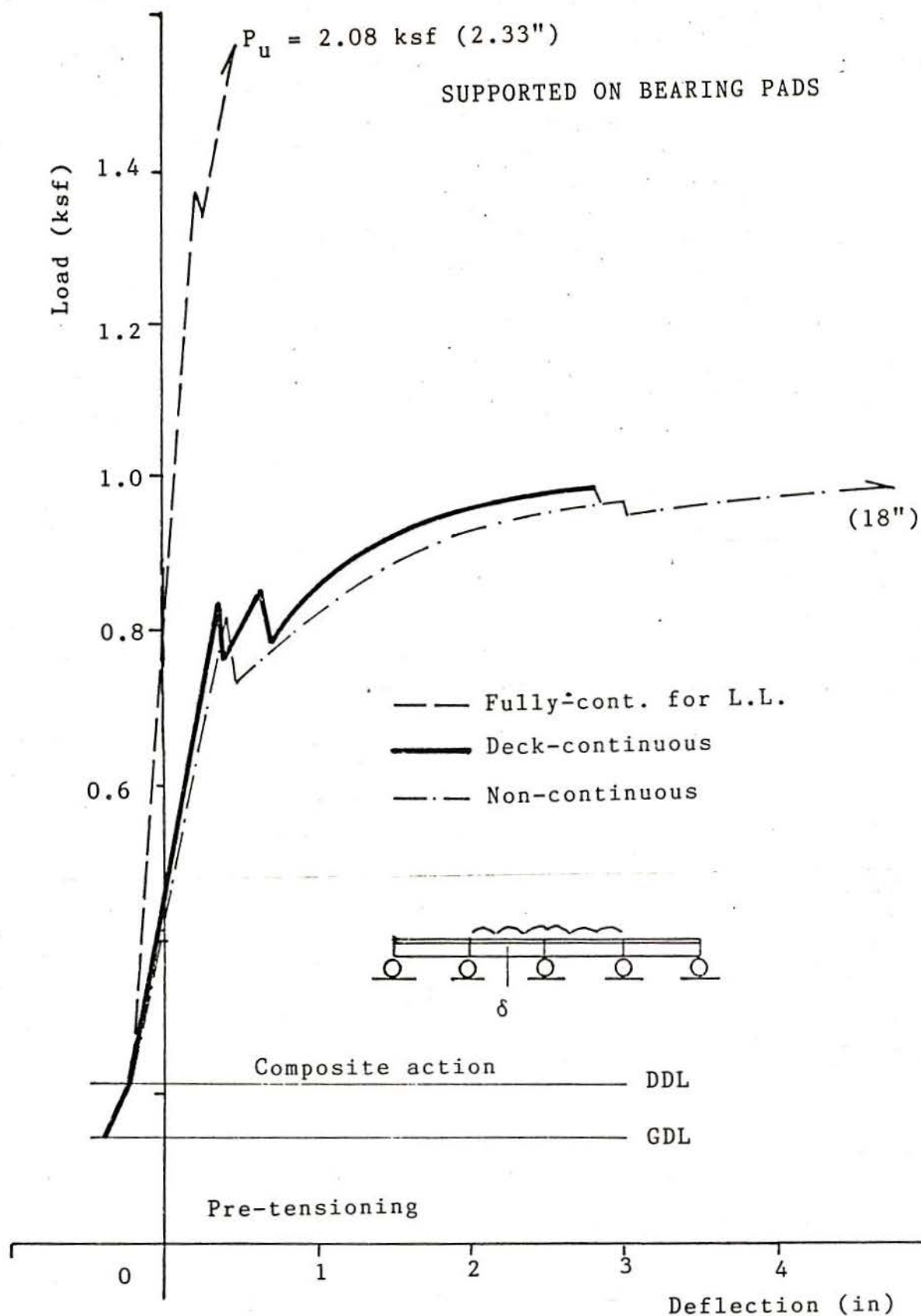


Fig 5.24 - Load-deflection responses for interior spans loading.

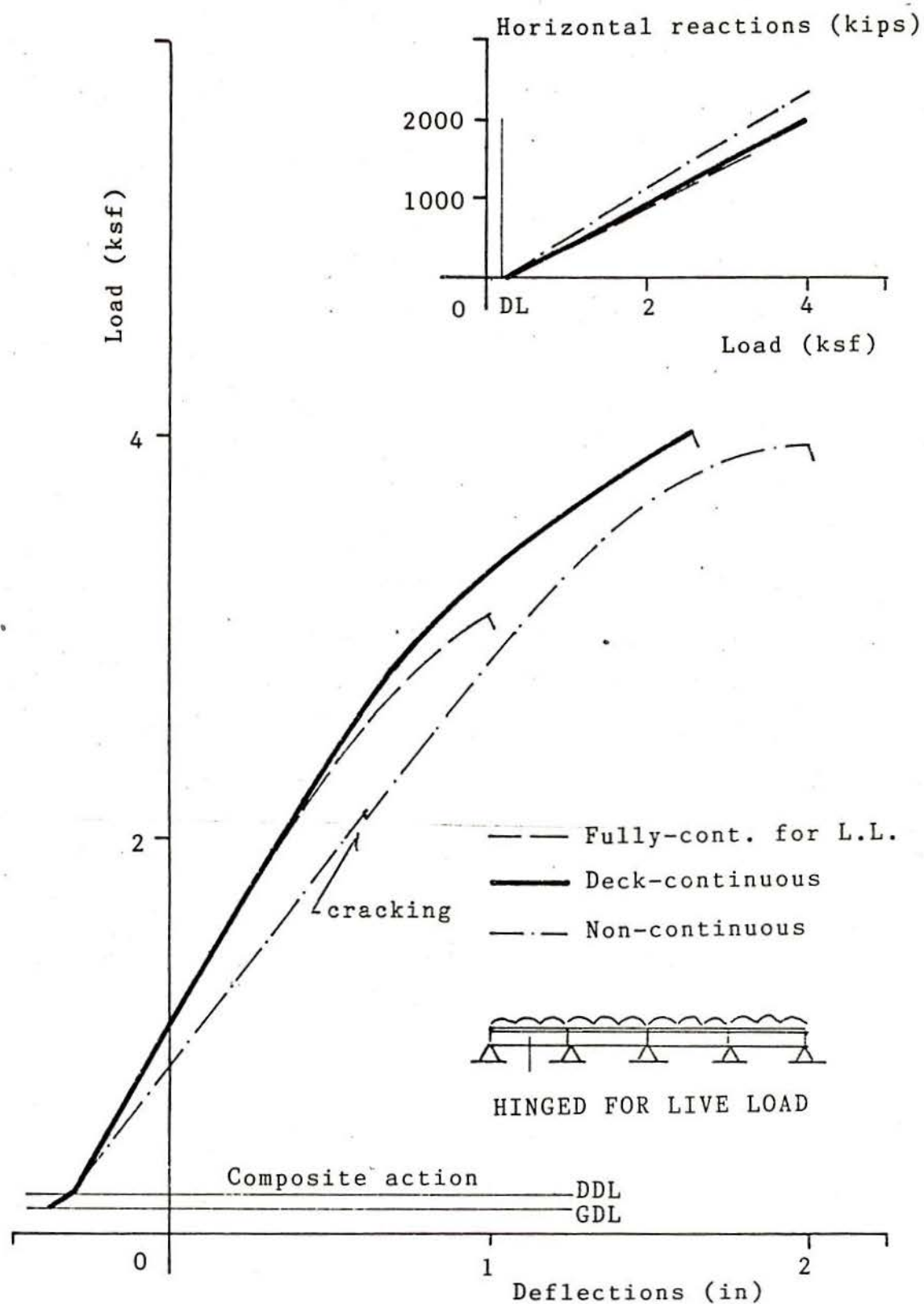


Fig 5.25 - Load-deflection responses under full span loading.

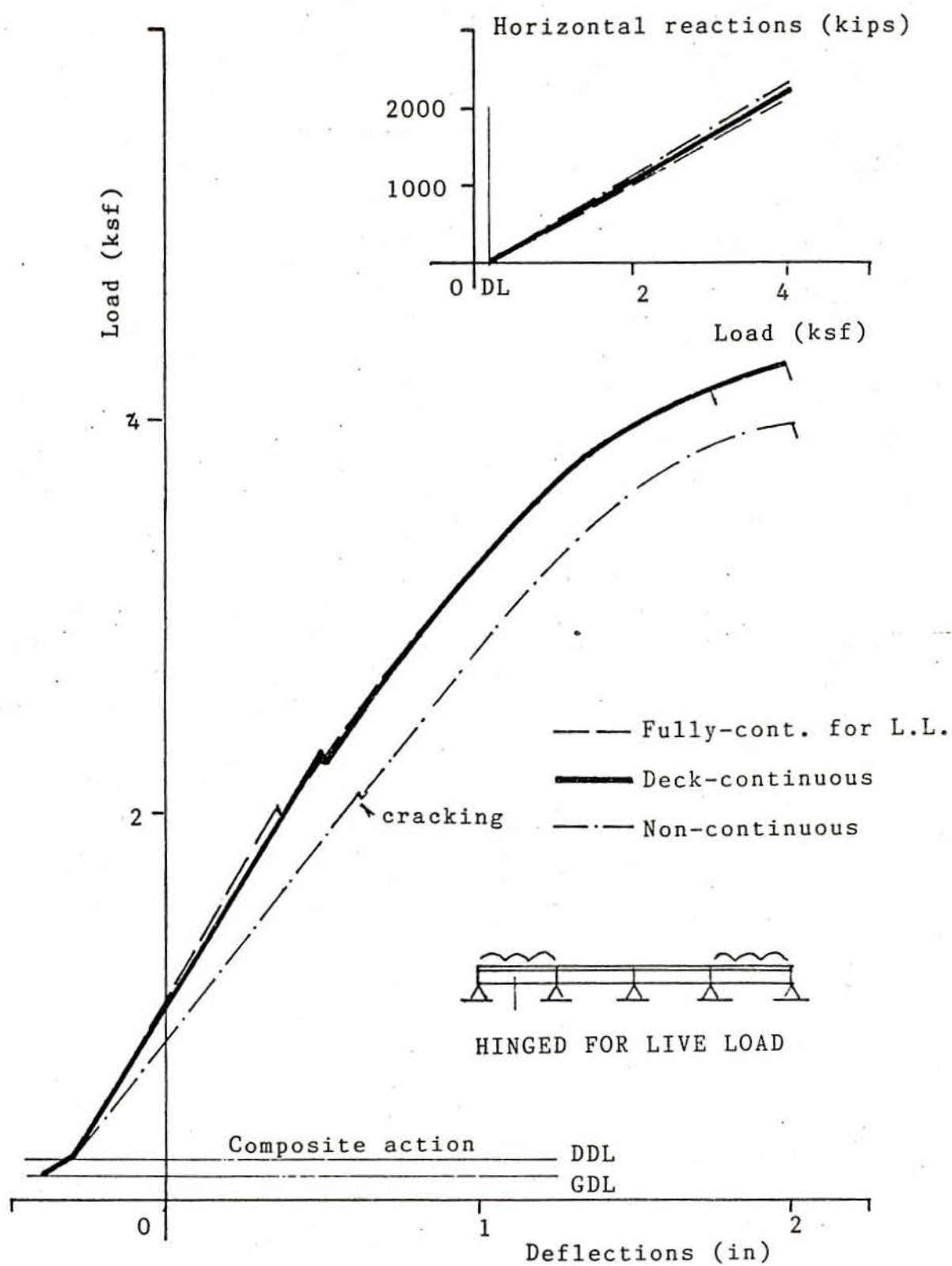


Fig 5.26 - Load-deflection responses for exterior spans loading.

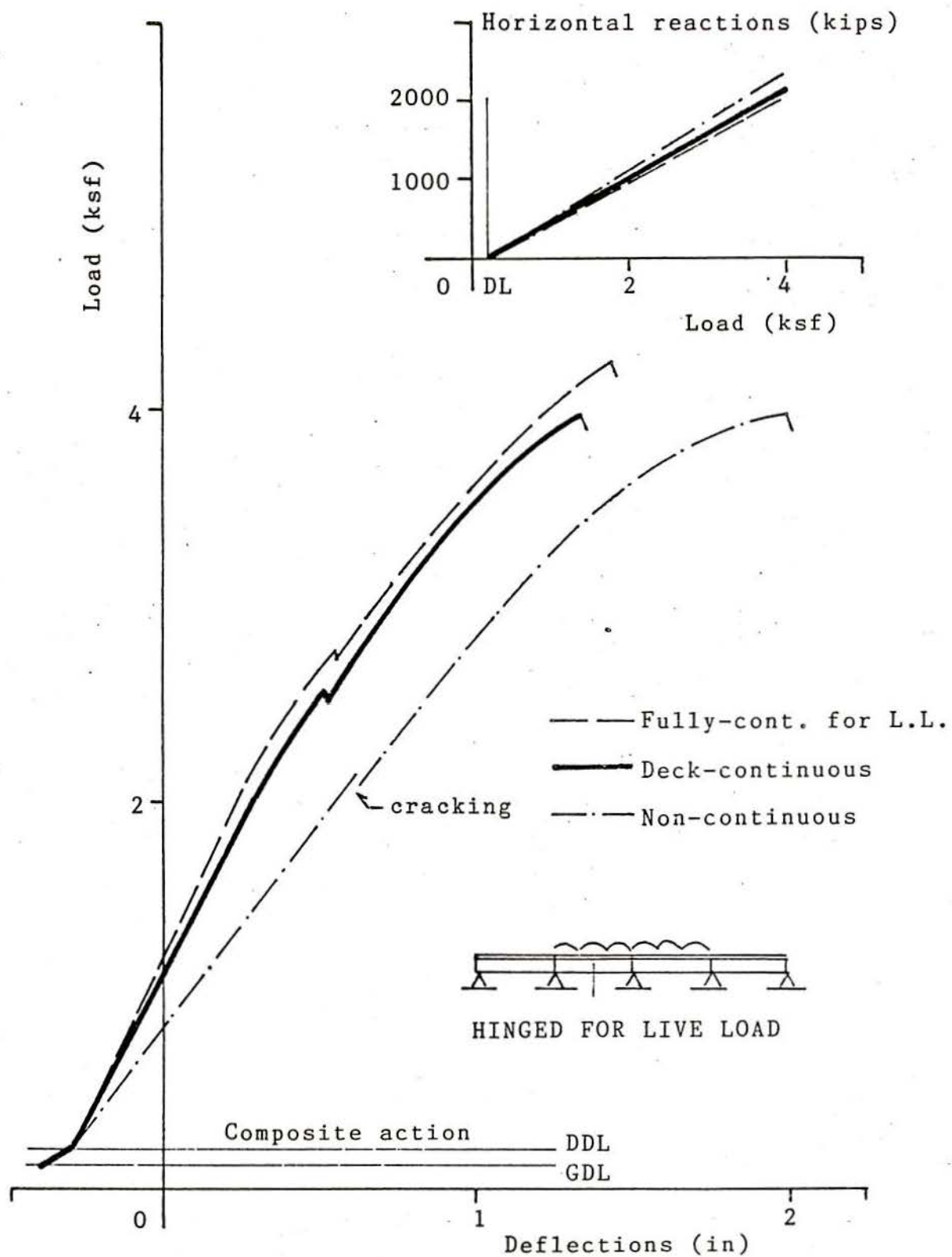


Fig 5.27 - Load-deflection responses for interior spans loading.

(c) Support Conditions

The use of hinged supports improves remarkably the stiffness and thus the response of the beams under service load conditions. However, attention should be paid to the very large reactions created at these hinges as shown in Figs. 5.25, 5.26 and 5.27. It may not be possible in design to accommodate such large reactions with hinges, particularly with precast concrete girders. If it is feasible to design for the large reactions developed in the hinges, the use of deck-continuous beams would be more economical than beams made continuous for live load.

On the other hand, the use of bearing pad supports is much less expensive. Deck-continuous beams with bearing pad supports present an improvement over non-continuous beams. Their responses under service loads are slightly enhanced and joints are avoided.

(d) Time and Temperature Effects

Both a deck-continuous beam and a jointed non-continuous beam are analyzed for their responses under time effects. The beams are left unloaded for a period of one year under the effects of aging, shrinkage and creep of concrete and relaxation of the prestressing steel. After one year the beams are loaded to failure. Their long-term strength is compared to the instantaneous strength when loaded at 28 days as shown in Figs. 5.28 and 5.29. No reduction in strength is found as a consequence of time effects. Both beams once more behave quite similarly.

Under the effects of a temperature gradient no perceptible difference is found in their responses as seen in Fig. 5.30. Camber is

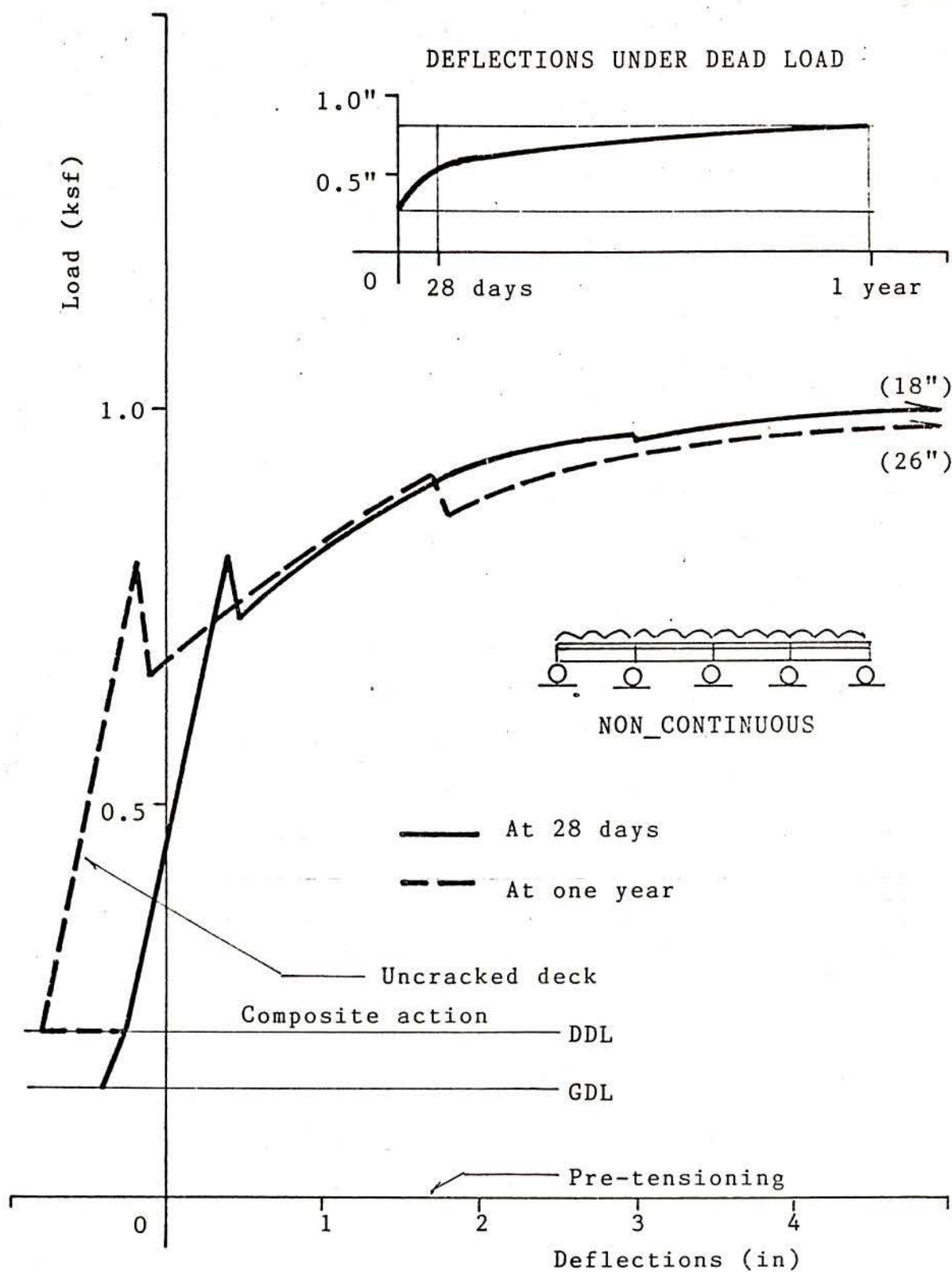


Fig 5.28 - Load-deflection responses under full span loading at ages of 28 days and one year.

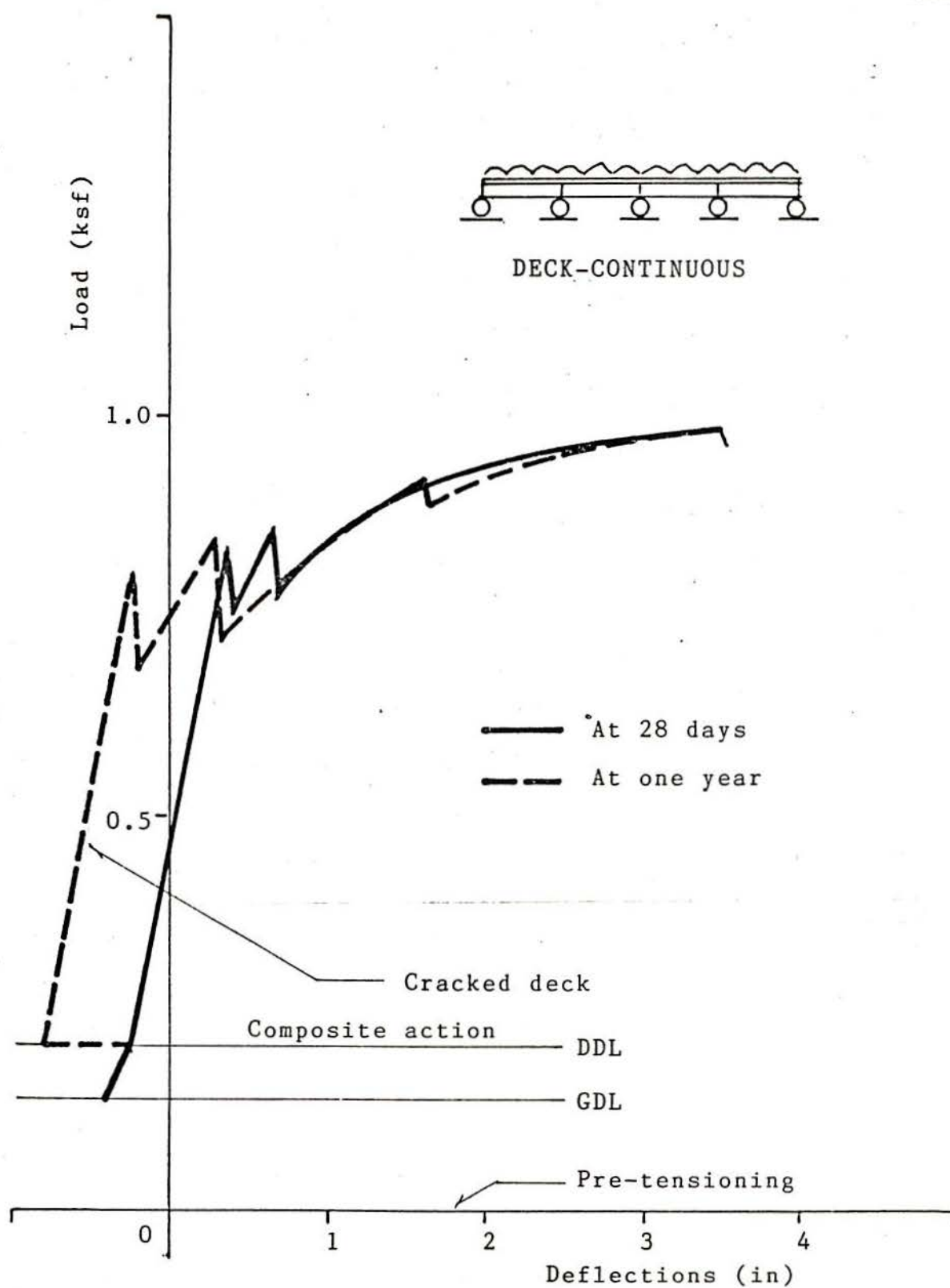


Fig 5.29 - Load-deflection responses under full span loading at ages of 28 days and one year.

increased when temperature varies across the depth of the beams, but under a constant temperature gradient no other effects are encountered.

(e) Unequal Spans

The use of different spans and smaller girders, see Fig. 5.17, by no means change the above conclusions. A similar behavior is found under different loading conditions as shown in Figs. 5.31, 5.32 and 5.33.

In conclusion, one may suggest that continuous-deck beams constitute a valid alternative solution for jointless bridge beams, either with steel or with precast concrete girders, for new construction or for the replacement of bridge decks. This new design concept shows promise as a method for achieving a jointless bridge deck.

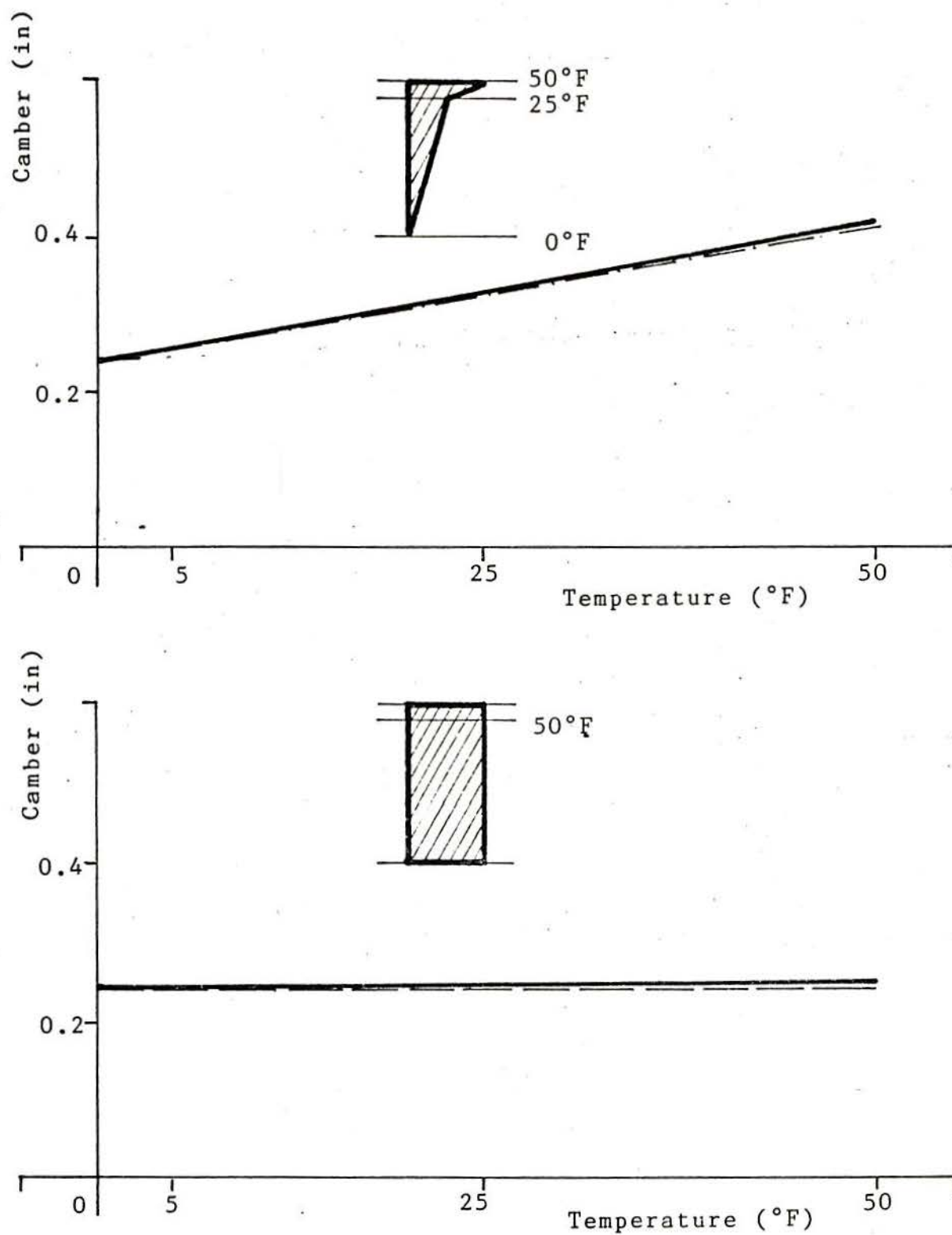


Fig 5.30 - Development of mid-span deflections under prestressing, dead load and temperature.

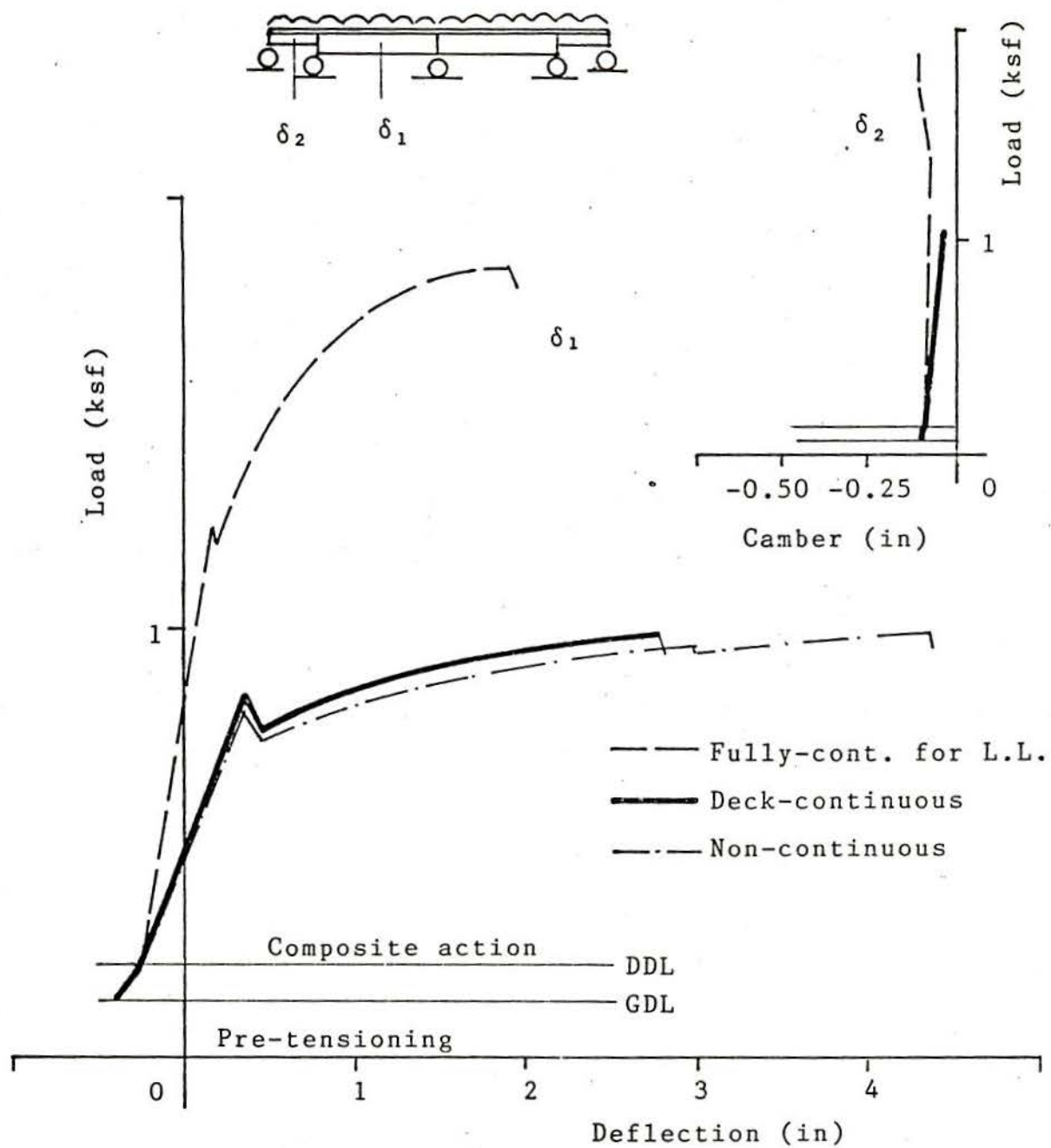


Fig 5.31 - Load-deflection responses under full span loading.

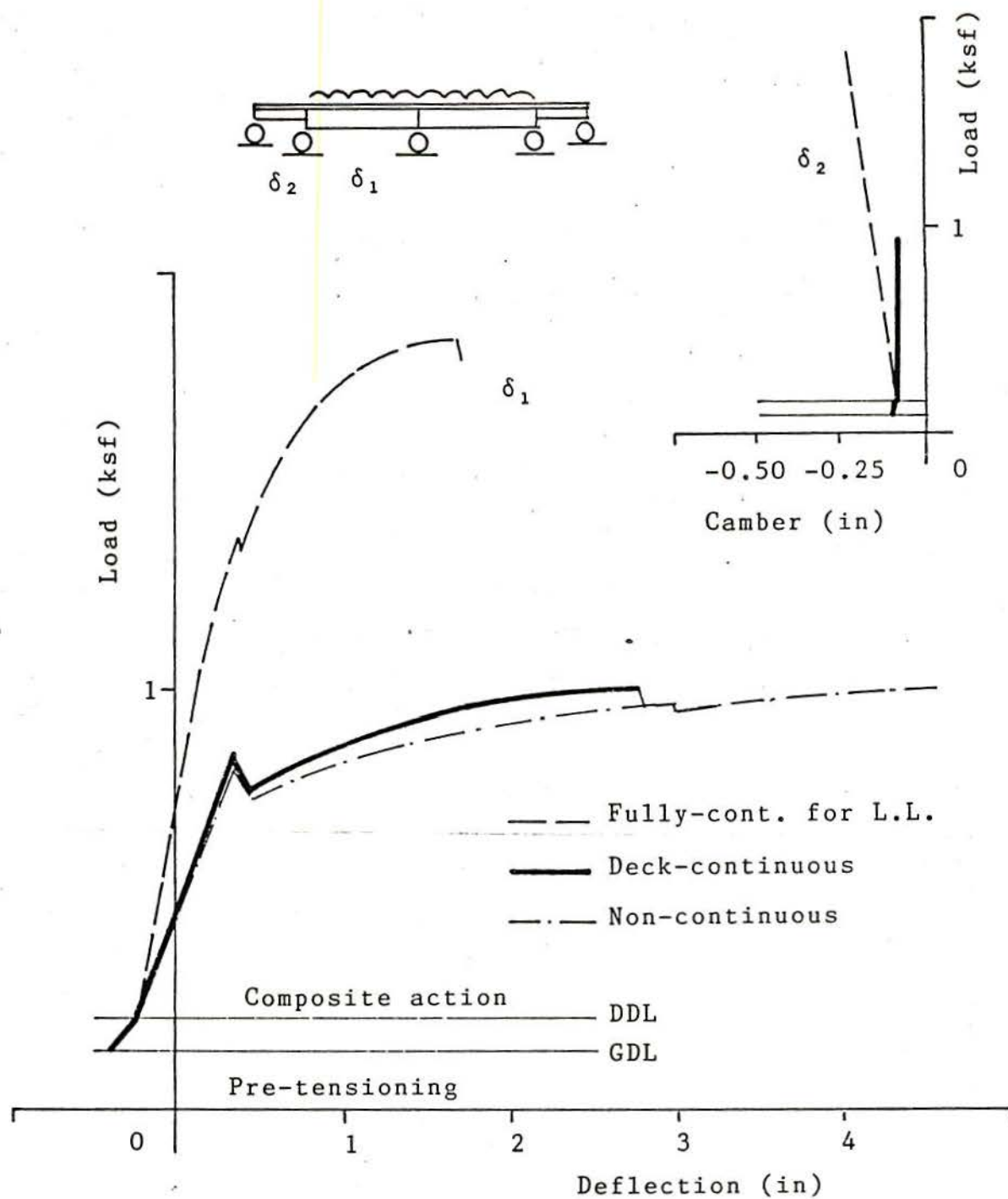


Fig 5.32 - Load-deflection responses for interior spans loading.

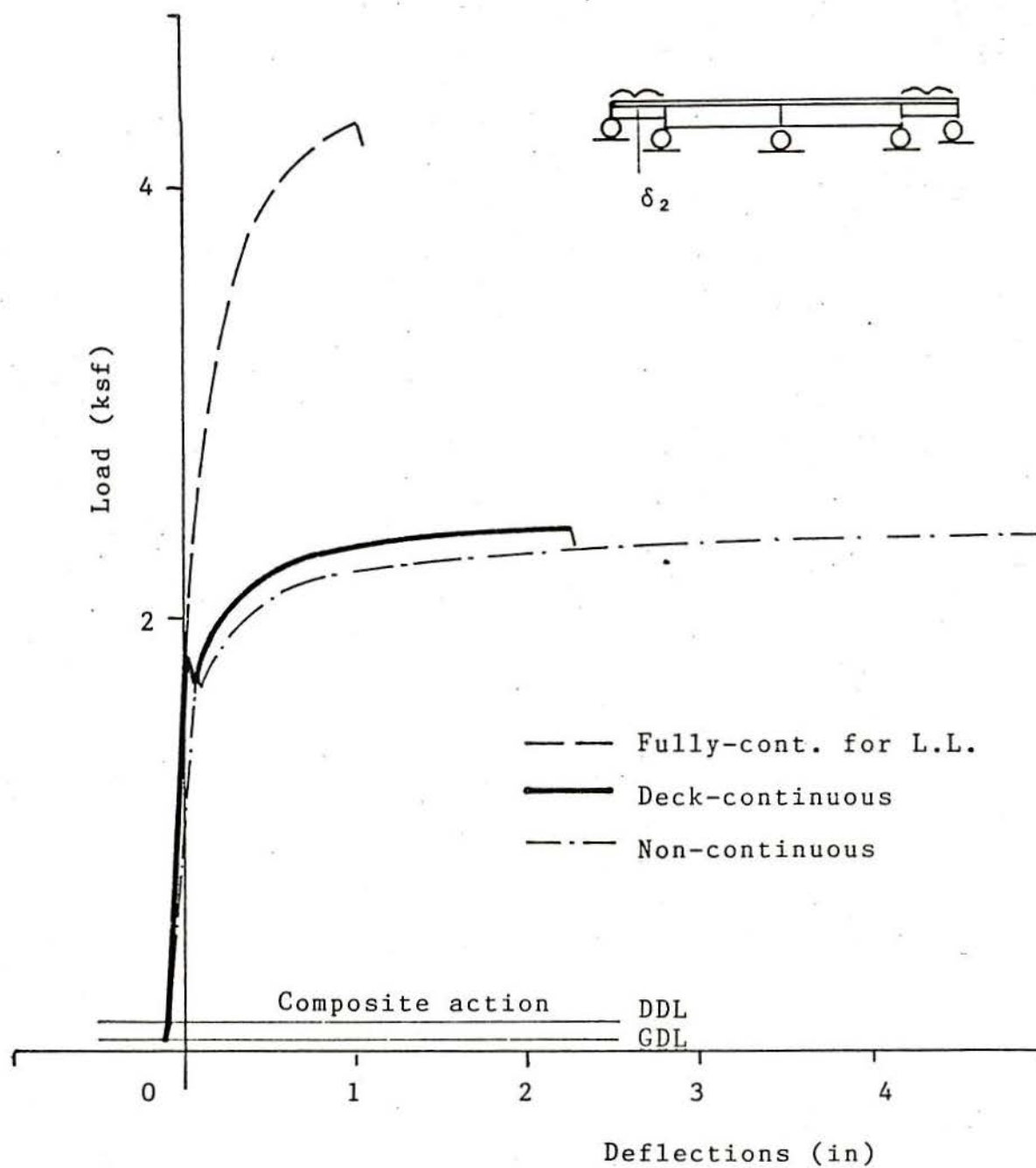


Fig 5.33 - Load-deflection responses for exterior spans loading.

6. SUMMARY, CONCLUSIONS AND RECOMMENDATIONS

6.1 Summary

The use of jointless construction is viewed as a new solution for the design of composite bridge beams. Expansion joints often become such a source of problems in maintaining bridges that their complete elimination seems preferable to some bridge designers. Among the few design solutions for a joint-free beam, the use of a fully-continuous deck slab over non-continuous girders appears a promising alternative. This solution is feasible not only for the construction of new bridges but also for the rehabilitation of old bridges requiring deck replacement.

The analysis of such beams is more complex than that of fully-continuous or non-continuous beams. However, numerical methods for structural analysis can be employed efficiently for either fully-continuous, non-continuous as well as deck-continuous beams. Instantaneous and time-dependent responses can be obtained for both linear and nonlinear ranges.

Many analytical and numerical solutions have been proposed by various investigators. Yet, none was found broad enough to completely suit the needs of the problem under consideration. It is the purpose of this study to propose a new numerical solution for the analysis of linear and nonlinear, instantaneous and time-dependent responses and strength of such beams. A finite element computer program has been developed for the analysis of both composite and non-composite, fully-

continuous, non-continuous and deck-continuous bridge beams. Girders may be cast-in-place or precast, in steel, reinforced or prestressed concrete topped by a reinforced concrete deck slab. Prestressed girders may be pre- or post-tensioned, but with bonded tendons.

Different constructional procedures may be used and analyzed in any desirable sequence. The effects of dead and live loads, prestressing, support displacements and temperature variation as well as time-dependent effects of aging, creep, shrinkage and relaxation are taken into account. Two different methods are used for the application of external loads, by increments of load or displacement[†]. Both the rate of creep method and the superposition method are used in estimating creep strains of concrete under variable stresses. A method similar to the rate of creep method is used in determining the relaxation of prestressing steel under varying stresses. The variation of the prestressing force due to deformation of the beam is also considered.

Different concrete materials may be used for deck slab and for girders. Either a bilinear or a Hognestad stress-strain relationship is assumed for concrete, and an elasto-plastic relationship is assumed for mild steel. For the prestressing steel, a trilinear relationship is assumed. The relationships for strength, creep and shrinkage of concrete, and relaxation of prestressing steel are based on the models proposed by the ACI Committee 209 and the PCI Committee on Prestress Losses. A smeared cracking model is used and concrete cracking is governed by a strain criterion.

The mechanical properties of the materials as well as the methods used for estimating instantaneous and time-dependent responses under

uniaxial load are thoroughly described in Chapter 2. Chapter 3 describes in detail the formulations of two finite elements as well as the fundamental concepts used as the basis for the development of the proposed model. The capability and validity of the solution are demonstrated in Chapter 4. Ten example problems are presented in which eighteen different beams are analyzed and the results are compared with the experimental data reported in the literature.

The application of the proposed solution to deck-continuous beams is treated in Chapter 5. A two-span composite beam with steel girders and a four-span composite beam with prestressed concrete girders are analyzed therein. Various loadings, support conditions and arrangements, continuity and constructional scheme are studied.

6.2 Conclusions

Based on the results obtained, the following conclusion are drawn regarding the proposed model and the behavior of deck-continuous beams.

6.2.1 Model

(1) The possibility of obtaining both instantaneous and time-dependent responses in a single analysis is extremely useful in the determination of long-term strength of beams, i.e. the strength of beams that under long-time sustained load are eventually subjected to its failure load.

(2) The use of two methods for application of loads, by increments of load and increments of displacement, has shown to be very convenient

for the study of different loading conditions. The Displacement Increment Method is capable of capturing the whole range of structural response, up to ultimate.

(3) Good agreement is found between measured and predicted results under the assumption of different stress-strain relationships for concrete. The models for aging, creep, shrinkage and steel relaxation together with the rate of creep and the superposition methods for estimating creep strains under variable stresses, have enabled reasonable predictions of time-dependent responses.

(4) The smeared cracking model for concrete presented a good performance in representing the post-cracking behavior of reinforced and prestressed concrete members.

(5) Both adopted elements have performed very adequately. The beam element with its variable nodal position enables the determination of horizontal reactions of bihinged beams under vertically applied load. Due to this important feature, it is possible to consider the actual horizontal movement of supports and its effect on the behavior of beams, especially deck-continuous beams. The performance of the connection element is yet to be validated by experimental data.

6.2.2 Deck-Continuous Beams

(1) The responses of jointless deck-continuous beams have been observed to be governed primarily by the imposed boundary conditions.

(2) When steel girders are used for which hinged supports are not a difficult task, a deck connection tensile behavior may be achieved by

having a hinge of an adequate shearing capacity at each side of the connection, i.e. for both adjacent girders. A couple will be created at this section, through the deck connection and hinges, and negative or positive moments can be resisted nearly as well as if full continuity were provided. The beam has its response enhanced remarkably and under service loads may be compared to a fully-continuous beam. Under overload conditions more deflections and less strength can be expected; however, this may be corrected by increasing the amount of mild reinforcement.

(3) More ductility may be obtained by increasing the width of the deck connections, either by widening the space between girders or by providing some unbonded length between deck and girders, at each side of the support.

(4) For girders which are simply supported on bearing pads, as are precast prestressed concrete beams, tension is obtained at the deck connections. In this case a deck-continuous beam behaves very similarly to a jointed non-continuous beam, with stiffness slightly enhanced and with the advantage of having no undesirable joints.

(5) In prestressed concrete deck-continuous beams under overload conditions, cracking will occur at the deck connection; but under unloading, cracks are likely to close completely. Should cracks remain unclosed, they should be less damaging than a built-in joint.

(6) Failure of deck-continuous beams eventually occurs by extensive yielding of the reinforcement in the connection and after that the beams behave like a jointed beam, observing all its ductility and strength

properties.

(7) Under sustained loading, due to time effects such as aging, differential creep, differential shrinkage and steel relaxation, and also under temperature variation, the behavior of a deck-continuous beam does not show significant difference from those presented by the correspondent fully-continuous and non-continuous beams. Their long-term strength is also unchanged.

6.3 Recommendations for Further Research

The study of this new type of beams deserves a more extensive investigation. The study presented herein has served only as a first step, a preliminary analysis, which must be improved and extended by other investigators. Some suggestions for further research follow.

- (1) The use of prestressing in the deck slab.
- (2) The use of pre- and post-tensioning in the same structure, often used for dead load carrying.
- (3) The inclusion of the tension stiffening effect found in concrete under cracked conditions.
- (4) The inclusion of the bending stiffness of the deck within the connection elements.
- (5) The effects of differential creep, differential shrinkage, steel relaxation and temperature variation in long multi-span beams with little or no joints.

(6) The investigation of an optimum span length of deck-continuous beams.

(7) It is finally and strongly suggested that some experimental work be done for obtaining a more reliable source of information on the behavior deck-continuous beams.

7. LIST OF REFERENCES

- (1) Loveall, C. L., "Jointless Bridge Decks," Civil Engineering Magazine, ASCE, Nov. 1985.
- (2) Wasserman, E. P., "Jointless Steel Bridges," The National Engineering Conference, AISC, Nashville, Tennessee, June 1986
- (3) Derthick, H. W., "No-Joint Venture," Civil Engineering Magazine, ASCE, Nov. 1975.
- (4) Derthick, H. W., "More About No-Joint Venture," Civil Engineering Magazine, ASCE, Apr. 1976.
- (5) Goodfrey, K. A. Jr., "Bridge Decks," Civil Engineering Magazine, ASCE, Aug. 1975.
- (6) Goodwin, S. R. and Peterson, G. E., "Guide to Assessing Capital Stock Conditions," The Urban Institute Press, Washington D.C., V. 2, 1984.
- (7) Peterson, G. E., et al, "Guide to Benchmarks of Urban Capital Conditions," The Urban Institute Press, Washington D.C., V. 3, 1984.
- (8) Lin, T. Y. and Kulka, F., "Fifty-Year Advancement in Concrete Bridge Construction," Journal of the Structural Division, ASCE, sept. 1975.
- (9) Freyermuth, C. L., "Design of Continuous Highway Bridges with Precast, Prestressed Concrete Girders," PCI Journal, V. 14, No. 2, Apr. 1969.
- (10) "Composite Steel-Concrete Construction," Journal of the Structural Division, ASCE, V. 100, No. ST5, pp. 1085-1139, May 1974.
- (11) Slutter, R. G., and Dirscoll, G. C., "Flexural Strength of Steel-Concrete Composite Beams," Journal of the Structural Division, ASCE, V. 91, No. ST2, Proc. paper 4294, pp. 71-99, Apr. 1965.
- (12) Grouni, H. N., "Prestressed Concrete-A Simplified Method For Loss Computation," ACI Journal, Proceedings, V. 70, No. 2, Feb. 1973.
- (13) Huang, T., "Direct Method For Estimating Prestress Losses," National Research Council, Concrete and Steel Bridges, Transportation Research Record No.547, 1975.
- (14) Tadros, M. K., Ghali, A. and Dilger, W. H., "Time-Dependent Prestress Loss and Deflection in Prestress Concrete Members," PCI Journal, V. 20, No. 3, May 1975.
- (15) Zia, P. Z. T., Preston, K., Scott, N. L. and Worman, E. B., "Estimating Prestress Losses," Concrete International, pp.

32-38, June 1979.

- (16) Ghali, A., and Trevino, J., "Relaxation of Steel in Prestressed Concrete," PCI Journal, Sept-Oct. 1985.
- (17) Tadros, M. K., Ghali, A. and Meyer, A. W., "Prestress Loss and deflections of Precast Concrete Members," PCI Journal, pp. 114-141, Jan 1985.
- (18) "PCI Design Handbook, Precast and Prestressed Concrete," Prestressed Concrete Institute, Chicago, Illinois, 3 rd. Edition 1985.
- (19) Branson, D. E., "The Deformation of Noncomposite and Composite Prestressed Concrete Members," Deflections of Concrete Structures, SP-43, ACI, Detroit, pp. 83-112, 1974.
- (20) Branson, D. E., "Deflections of Concrete Structures," McGraw Hill, New York, 1977.
- (21) Rao, V. J., and Dilger, W. H., "Time-Dependent Deflections of Composite Prestressed Concrete Beams," Deflections of Concrete Structures, SP. 43, ACI, Detroit, 1974.
- (22) Naaman, A. E., "Time-Dependent Deflection of Prestressed Beams by The Pressure Line Method," PCI Journal, pp. 98-119, Mar. 1983.
- (23) PCI Committee on Prestress Losses, "Recommendations for Estimating Prestress Losses," PCI Journal, V. 20, No.4, July-Aug. 1975.
- (24) Sinno, R. and Furr, H. L., "Computer Program for Predicting Prestress Loss and Camber," PCI Journal, V. 17, No. 5, Sept. 1972.
- (25) Branson, D. E., "Time-Dependent Effects in Composite Concrete Beams," ACI Journal, V. 61, Feb. 1964.
- (26) Mossosian, V. and Gamble, W. L., "Time-Dependent Behavior of Noncomposite and Composite Prestressed Concrete Structures Under Field and Laboratory Conditions," Structural Research Series No. 385, Civil Engineering Studies, University of Illinois, Urbana, May 1972.
- (27) Fadl, A. I. and Gamble, W. L., "Time-Dependent Behavior of Non-Composite and Composite Post-Tensioned Concrete Girder Bridges," University of Illinois, Engineering Experimental Station, Structural Research Series No. 430, Oct. 1976.
- (28) Bakoss, S. L., Gilbert, R. I., Faulkes, K. A., and Pulmano, V. A., "Long-Term Deflections of Reinforced Concrete Beams," Magazine of Concrete Research, V. 34, pp. 203-211, 1982.
- (29) Ngo, D., and Scordelis, A. C., "Finite Element Analysis of Reinforced Concrete Beams," ACI Journal, V. 64, No. 3, pp.

152-163, Mar. 1967.

- (30) Nilson, A. R., "Non-Linear Analysis of Reinforced Concrete by the Finite Element Method," ACI Journal, V. 65, No. 9, pp. 757-766, Nov. 1968.
- (31) Lazaro, A. L., and Richards, R. Jr., "Full Range Analysis of Concrete Frames," Journal of the Structural Division, ASCE, pp. 1761-83, Aug. 1973.
- (32) Kroenke, W. C., Gutzwiller, M. T. and Lee, R. H., "Finite Element for Reinforced Concrete Frame Study," Journal of the Structural Division, ASCE, V. 99, No. ST7, July 1973.
- (33) American Society of Civil Engineers, "Finite Element Analysis of Reinforced Concrete," State-of-the-Art Report, 1982.
- (34) Atkins, W. D., "A Generalized Numerical Solution for Prestressed Concrete Beams," Unpublished Master's Thesis, The University of Texas, Austin, Texas, Aug. 1975.
- (35) Pierce, D. M., "A Numerical Method of Analysing Prestress Concrete Members Containing Unbonded Tendons," PhD Dissertation, The University of Texas, Austin, Texas, June 1968.
- (36) Chang, D. C., "A Numerical Method of Analysing Composite Prestressed Concrete Members," unpublished Master's thesis, The University of Texas, Austin, Texas, May 1969.
- (37) Lo, Y., "Comparison of Analytical and Measured Performance of Pre-Tensioned Prestressed Concrete Beams," unpublished Master's report, The University of Texas, Austin, Texas, June 1975.
- (38) Wong, S. P., "A Study of Partially Continuous Composite Prestressed Concrete Members," unpublished Master's thesis, The University of Texas, Austin, Texas, June 1968.
- (39) Mattock, A. H., and Kaar, P. H., "Precast Prestressed Concrete Bridges - 3. Further Tests of Continuous Girders," PCA Journal, Research and Development Laboratories, V. 2, No. 3, pp. 51-78, Sept. 1970.
- (40) Qiu, L., Chunfu, W. and Jinhuan, X. Y. C., "Computed-Aided Design for Long Span Prestressed Concrete Bridges-General Program SABRIJ-B83," Proceeding of the Second International Conference in Computing in Civil Engineering, Science Press, Beijing, China, 1985.
- (41) Barnard, P. R., "Researches Into the Complete Stress-Strain Curve for Concrete," Magazine of Concrete Research, No. 16, pp. 203-210, 1964.
- (42) Ahmad, S. H., and Shah, S. P., "Complete Triaxial Stress-Strain Curves for Concrete," Journal of the Structural Division, ASCE,

V. 108, No. ST4, Apr. 1982.

- (43) Ahmad, S. H., and Shah, S. P., "Complete Stress-Strain Curves of Concrete and Non-Linear Design," Non-Linear Design of Concrete Structures, CSCE-ASCE-ACI-CEB, International Symposium, Univ. of Waterloo, Ontario, Canada, Apr. 1979.
- (44) Hognestad, E., "A Study of Combined Bending and Axial Load in Reinforced Concrete Members," Univ. of Illinois, Engineering Experimental Station, Bulletin Series, No. 399, Nov. 1951.
- (45) Kent, D. C. and Park, R., "Flexural Members with Confined Concrete," Proceedings, ASCE, V. 97, No. ST7, July 1971.
- (46) Lee, L. N. H., "Inelastic Behavior of Reinforced Concrete Members," Transactions, ASCE, V. 120, 1955.
- (47) Kriz, L. B., and Lee, S. L., "Ultimate Strength of Over-Reinforced Beams," Proceedings, ASCE, V. 86, No. EM3, June 1960.
- (48) Popovics, S., "A Review of Stress-Strain Relationships for Concrete," ACI Journal, Proceedings, V. 67, No. 3, Mar. 1970.
- (49) Sargin, M., "Stress-Strain Relationships for Concrete and the Analysis of Structural Concrete Sections," Study No. 4, Solid Mechanics Division, Univ. of Waterloo, Waterloo, Ontario, Canada, 1971.
- (50) Hognestad, E., Hanson, N. W., and McHenry, D., "Concrete Stress Distribution in the Ultimate Strength Design," ACI Journal, Proceedings, V. 52, Dec. 1955.
- (51) Park, R. and Paulay, T., "Reinforced Concrete Structures," John Willey & Sons Inc., 1975.
- (52) Soliman, M. T. M., and Yu, C. W., "The Flexural Stress-Strain Relationship of Concrete Confined by Rectangular Transverse Reinforcement," Magazine of Concrete Research (London), V. 19, No. 61, Dec. 1967.
- (53) Roy, H. E. H., and Sozen, M. A., "Ductility of Concrete," Proceedings of the International Symposium of Flexural Mechanics of Reinforced Concrete, ASCE-ACI, Miami, Nov. 1964.
- (54) Bertero, V. V., and Felipa, C., Discussion of "Ductility of Concrete," by Roy, H. E. H., and Sozen, M. A., Proceedings of the International Symposium of Flexural Mechanics of Reinforced Concrete, ASCE-ACI, Miami, Nov. 1964.
- (55) "Système International de Réglementation Technique Unifiée des Structures Volume II - Code Modèle Pour Les Structures En Béton (3^{ème} Project, Version Originale)," Bulletin D'Information, No. 117-F, Comité Euro-International Du Béton, Paris, Dec. 1976.

- (56) ACI Committee 318, Building Code Requirement for Reinforced Concrete (ACI 318-77), American Concrete Institute, Detroit, 1977.
- (57) Fadl, A. I., Gamble, W. L., and Mohraz, B., "Test of a Precast Post-Tensioned Composite Bridge Girder Having Two Spans of 124 feet," Univ. of Illinois, Engineering Experiment Station, Structural Research Series, No. 439, Apr. 1977.
- (58) Sinha, B. P., Gerstle, K. H. and Tulin, L. C., "Stress-Strain Relations for Concrete Under Cyclic Loading," Journal of the American Concrete Institute, V. 61, No. 2, pp. 195-211, Feb. 1984.
- (59) Karsan, I. D., and Jirsa, J. O., "Behavior of Concrete Under Compressive Loading," Journal of the Structural Division, ASCE, V. 95, ST12, pp. 2543-2563, Dec. 1969.
- (60) Neville, A. M., "Creep of Concrete: Plain, Reinforced and Prestressed," North Holland Publishing Company, Amsterdam, 1970.
- (61) Bazant, Z. P., "Mechanics of Geomaterials - Rocks, Concrete, Soils," John Wiley & Sons, 1985.
- (62) Corley, W. G., "Bibliography on Time-Dependent Effects in Plain and Reinforced Concrete," Department of Civil Engineering, Univ. of Illinois, Urbana, Illinois, Dec. 1959.
- (63) ACI Committee 209, "Designing for the Effects of Creep, Shrinkage and Temperature in Concrete Structures," SP. 27, ACI, Detroit, 1971.
- (64) Branson, D. E., and Christiason, M. L., "Time-Dependent Concrete Properties Related to Design-Strength and Elastic Properties, Creep and Shrinkage," SP. 27-33, ACI, Detroit, pp. 257-277, 1971.
- (65) Zundeleovich, S., Lee, D. L. M. and Chin, A. N. L., "Camber and Deflection Behavior of Prestressed Concrete Beams," Technical Report CE71-R1, CE Department, Univ. of Hawaii, Honolulu, Hawaii, Sept. 1971.
- (66) Ross, A. D., "Creep of Concrete Under Variable Stresses," ACI Journal, Proceedings, V. 34, Mar. 1958.
- (67) McMillan, F. R., "Shrinkage and Time Effects in Reinforced Concrete," Univ. of Minnesota, Bulletin No. 3, Mar. 1915.
- (68) Washa, W. G., and Wendt, K. F., "Fifty-Year Properties of Concrete," ACI Journal, Proceedings, V. 72, No. 1, Jan. 1975.
- (69) Atkan, A. E., Karlson, B. J., and Sozen, M. A., "Stress-Strain Relationship of Reinforcing Bars Subjected to Large Strain Reversals," CE Studies, Structural Research Series, No. 397,

Univ. of Illinois, Urbana, June 1973.

- (70) Podolny, W. Jr., and Melville, T., "Understanding the Relaxation in Prestressing," PCI Journal, V. 14, Aug., 1969.
- (71) Magura, D. D., Sozen, M. A., and Siess, C. P., "A Study of Stress Relaxation in Prestressing Reinforcement," PCI Journal, V. 9, No. 2, Apr. 1964.
- (72) Vinje, L., "Behavior and Design of Plain Elastomeric Bearing Pads in Precast Structures," PCI Journal, V. 30, No. 6, Nov-Dec. 1985.
- (73) Iverson, J. K., And Pfeiffer, D. W., "Criteria for Design of Bearing Pads," Research Project of PCI, PCI, Chicago, Illinois, 1985.
- (74) Gupta, A. K. and Ma, P. S., "Error in Eccentric Beam Formulation," International Journal for Numerical Methods in Engineering, Vol. 2, pp. 1473-1477, 1977.
- (75) Irons, B. M., "Engineering Applications of Numerical Integrations in Stiffness Methods," AIAAJ, V. 4, No. 11, pp. 2035-37, 1966.
- (76) Zienkiewics, O. C., "The Finite Element Method," 3 rd. Ed., McGraw Hill, 1977.
- (77) Cock, R. D., "Concepts and Applications of Finite Element Analysis," John Wiley & Sons, 2 nd. Ed., 1981.
- (78) Weaver, W. Jr., and Johnston, P. R., "Finite Element for Structural Analysis," Prentice Hall, Inc., 1984.
- (79) Pawsey, S. F. and Clough, R. W., "Improved Numerical Integration of Thick Shell Finite Elements," International Journal for Numerical Methods In Engineering, Vol. 3, pp. 575-586, 1971.
- (80) Hoffman, P. C., McClure, R. M., and West, H. H., "Temperature Study of an Experimental Segmental Concrete Bridge," PCI Journal, pp. 78-97, Nar. 1983.
- (81) DeSergio, J. N., "Thermal and Shrinkage Stresses - They Damage Structures!," Designing for the Effect of Creep, Shrinkage and Temperature in Concrete Structures, SP.27.2, ACI, Detroit, 1971.
- (82) Priestley, M. J. N., "Design of Concrete Bridges for Temperature Gradients," ACI Journal, V. 75, No. 5, pp. 209-217, 1978.
- (83) Bathe, K. J., Wilson, E. L., and Peterson, F. E., " SAP IV - A Structural Analysis Program For Static and Dynamic Response of Linear Systems," Report no. EERC, 73-11, Apr. 1974.
- (84) Rashid, Y. R., "Ultimate Strength Analysis of Prestressed Concrete Pressure Vassels," Nuclear Engineering and Design, V. 7, No. 4,

pp. 334-344, Apr. 1968.

- (85) Batoz, J. L., and Dhatt, G., "Incremental Displacement Algorithms for Non-Linear Problems," International Journal for Numerical Methods in Engineering, V. 14, pp. 1262-1267, 1979.
- (86) Haisler, W. E., Strickling, J. A. and Key, J. E., "Displacements Incrementation in Non-Linear Structural Analysis by the Self-Correcting Method," International Journal for Numerical Methods in Engineering, V. 11, pp. 3-10, 1977.
- (87) Zienkiewics, O. C., "Incremental Displacement in Nonlinear Analysis," International Journal for Numerical Methods in Engineering, V. 3, pp. 587-588, 1971.
- (88) Akbar, H., and Gupta, A. K., "Membrane Reinforcement in Concrete Shells - Design vs. Non-Linear Behavior," Research Report, Department of Civil Engineering, North Carolina State University, Jan. 1985.
- (89) Lin, T. Y., and Burnes, N. H., "Design of Prestressed Concrete Structures," John Willey & Sons, 3 rd. Ed., 1981.
- (90) Sprinkel, M. M., "Prefabricated Bridge Elements and Systems," NCHRP-119, Transportation Research Board, Washington DC, Aug. 1985.
- (91) Hanson, N. W., "Precast Prestressed Concrete Bridges - 2, Horizontal Shear Connections," PCA Journal, Research and Development Laboratories, No. 2, pp. 38-58, May 1960.
- (92) Mattock, A. H., and Kaar, P. H., "Precast Prestressed Concrete Bridges - 4, Shear Tests of Continuous Girders," PCA Journal, Research and Development Laboratories, No. 1, pp. 19-46, Jan. 1961.
- (93) "Manual of Steel Construction," American Institute of Steel Construction, 8th ed., Chicago, Illinois, 1980.
- (94) Litle, W. A., and Paparont, M., "Size Effects in Small-Scale Models of Reinforced Concrete Beams," ACI Journal, Nov. 1966.
- (95) Keyder, E., "Strength and Behavior in Flexure of Bonded Prestressed Concrete Beams in Tension Only," unpublished Master's thesis, The University of Texas, Austin, Texas, May 1965.
- (96) Kripanarayanan, K. M., and Brenson, D. E., "Some Experimental Studies of Time-Dependent Deflections of Non-Composite and Composite Reinforced Concrete Beams," Deflections of Concrete Structures, ACI Publication SP-43-16, pp. 409-419, 1974.
- (97) AASHTO - Standart Specifications for Highway Bridges, American Association of State Highway and Transportation Officials, 13 th. Ed. Washington DC, 1983.

8.1 Input and Output Guide

The input data are arranged in 24 different lines or sets of lines containing all the information necessary for the analysis of one or more problems at a time. A sample input is shown in Appendix C. The details for each entering are given below together with the necessary explanation pertaining each type of information. Data are to be input following the last card of the program coding. No blank lines are accepted and free format is to be used. Any desirable physical dimensioning may be used provided it is consistent throughout each problem.

1st line

Number of problems to be analyzed.

2nd line

A sequence of eight different enterings is contained in this single line, corresponding to the following variables:

a) Total number of elements.

b) Number of connection elements.

c) Number of nodal points.

d) Number of supports.

e) Number of loading cases, according to line 17.

f) Number of layers to be used in the girders. For rectangular or steel I-girders a multiple of 6 and for concrete I-girders a multiple of 4.

g) Number of layers to be used in the deck, any number.

h) Number of elements for which a complete information is to be printed. This information is updated at every step of the solution and contains: position, area, strain, stress and instantaneous modulus of elasticity for each of the layers. For every step of the solution, and corresponding to the chosen elements, the following results will be listed at the end of the output: bending moment, curvature, deflection, fraction of the applied load, current time of loading and number of iterations in the step.

3rd line

In a single line the numbers of all the elements chosen (line 2h) are to be listed.

4th line

Stiffnesses of the bearing pads, calculated according to section 2.4.

5th line

When the Displacement Increment Method is used for the application of the live load (line 17), three different entering are necessary for establishing:

a) Displacement increment to be applied at every incremental step. This displacement may be positive or negative according to the deflection presented by the structure at the particular nodal point, under the applied live load.

b) Number of the nodal point at which the incremental displacement

(item a) is to be applied.

c) Fraction of the total live load to be applied.

6th line

Five integer values are needed for defining girder material, section type and variability, reinforcement distribution and concrete stress-strain relationship as follows.

a) Girder material: (0) steel, (1) prestressed concrete and (2) reinforced concrete.

b) Girder cross-sectional type: (0) rectangular and (1) other shapes like I, Tee, double Tee and box girders.

c) Dimensions of the girder cross-sections along the length of the: (0) constant and (1) variable.

d) Reinforcement distribution along the length of the beam: (0) constant and (1) variable.

e) Assumed stress-strain relationship for concrete: (0) Hognestad's and (1) bilinear.

7th line

For establishing the dead loads of the girders and deck the specific weights of the materials are needed. Two values are to be entered in one single line, calculated according to the chosen physical dimensions and corresponding to girders and deck respectively.

8th line

For establishing the ages of the materials and the consequent effects of creep, shrinkage and relaxation five time values, in days,

are to be input in one single line and corresponding to:

- a) Time at which the curing of the girder concrete has ended. 28
- b) Time at which the curing of the deck concrete has ended.
- c) Time at which the girders have been first loaded. 28
- d) Time at which the deck has been first loaded.
- e) Time of prestressing. 28

Lines 9 to 12 correpond to setting of material properties. All six enterings for each line are to be assumed as positive and their proper signs will be assigned inside the program.

9th line

According to Fig. 2.6, the tri-linear stress-strain relationship for the prestressing steel is established by the setting of six different variables. The first three correspond to the moduli of elasticity of the three linear segments, the following two define the two yielding stresses, $fs1$ and $fs2$, and the last one defines its ultimate strain.

10th line

The bilinear stress-strain relationship of reinforcing steel, Fig. 2.5, is defined by the variables: initial modulus of elasticity, yielding strain and ultimate strain.

11th line

The girders may be made of steel or concrete. For steel girders the stress-strain relationship of its material is input in a similar fashion as in line 10 for steel reinforcement. For the concrete girders four variables are used in defining the stress-strain relationship of

concrete: Initial modulus of elasticity, 28-day cylinder strength, tensile rupture strain and ultimate compressive strain.

12th line

The variables used for defining the stress-strain relationship of concrete used in the deck slab are input similarly as the ones for the girder concrete, as in line 11.

13th line

As many lines as the number of elements are needed for defining the connectivity and the type of each element used. Three entering are used in each line. The first two define the number of the two nodal points and the last defines the type of the element as follows:

(0) A beam element defined at the beginning of the solution, representing the girder and deck cross-sections.

(1) A connection element defined at the time when the deck slab is cast and its stiffness is added to the girder stiffness.

(2) A beam element used for obtaining continuity for live load. The element will be defined when the deck slab is cast and continuity is obtained. Its dimensions may be different from the other beam elements for representing a diaphragm for instance.

14th line

Coordinates and nodal conditions are defined by five enterings in as many lines as there are nodal points. The first two numbers define the horizontal and vertical coordinates of each nodal point, respectively. The origin of the horizontal coordinates may be located at any desirable

position, but the vertical coordinates are referred to the bottom face of each girder.

The nodal conditions represent the restrictions applied to each nodal point in each of the three directions, i.e. horizontal, vertical and rotational directions respectively as: (0) free and (1) restricted.

15th line

When the dimensions of the cross-sections of the elements are constant throughout the length of the member, see line 6c, only one line is needed for the input of the sectional dimensions. Otherwise, as many lines as there are elements are needed. The following cases apply for each type of cross-section:

a) Steel I-girders - Eight enterings define the dimensions of the deck and girders, in the following order: deck width and thickness; girder area, depth and moment of inertia; thicknesses of the top flange, web and bottom flange.

b) Rectangular cross-section - Only four enterings are used: deck width and thickness, and girder width and thickness.

c) Girders of other shapes - Any other shape of the girders is modeled as an I cross-section. Width and thickness of the deck, top flange, web and bottom flange are input in a similar sequence.

d) Connection element - For the deck connection, and only when variable cross-sections are used, see line 6c, four enterings are needed: width and thickness of the deck and distances from the C.G.C. of the deck to the bottom faces of the two adjacent girders.

16th line

Three levels of reinforcement may be used, one in the deck slab and two in the girders. Total area and position of each level with respect to the bottom face of the girders are defined by six enterings. When constant steel distribution is used, see line 6d, only one line is needed. Otherwise, as many lines as there are elements are input. The first reinforcement level is defined as the one in the deck, the second and third following downwards, respectively.

17th line

Each loading condition, instantaneous or time-dependent, is defined by a line containing eight integer enterings:

a) A number defining the type of loading, load case, according to the following list:

- 1 Girder dead load
- 2 Prestressing
- 3 Deck dead load
- 4 Support displacements
- 5 Live load
- 6 Temperature
- 7 Time effects

b) A variable, 0 or 1, defining whether the beam is to be assumed noncomposite or composite, respectively, for each load case.

c) Number of steps to be used in each loading. For prestressing one step is assumed and when using the Displacement Increment Method the

variable shall be assigned the value 1000.

d) A variable, 1 or 0, defining whether the results for each step shall be printed or not, respectively. For the last step of each load case the results are always printed regardless of the value assumed.

e) A variable defining which time-effects are to be analyzed.

- 0 None
- 1 Creep
- 2 Shrinkage
- 3 Relaxation
- 4 All

f) Time at which the loading case is to be initiated, in days.

g) Time at which the loading case is to be finished, in days.

h) A variable, 1 or 0, defining whether the bearing supports are to be transformed into hinges or not, respectively. This effect is obtained by assigning a very large stiffness to the bearing supports.

18th line

In as many lines as there are supporting nodes two variables shall define: the number of the supporting nodal point and magnitude of vertical displacements to be applied at the respective supports.

19th line

A temperature variation gradient is defined by three temperature values at the top of the deck slab, at the deck-girder interface and at the bottom of the girders, respectively.

20th line

In as many lines as there are nodal points three concentrated nodal loads may be defined, in the horizontal, transversal and rotational directions respectively.

21st line

Loads applied at the elements are defined by three enterings in as many lines as there are elements: A uniformly distributed load, and a concentrated load and its point of application, measured from the left nodal point, respectively.

Lines 22 to 25 regard information concerning the prestressing cables and their characteristics. They shall be omitted when the girders are not prestressed.

22nd line

One single line with six enterings is used for defining the following prestressing variables:

- a) Type of prestressing, (0) post-tensioned and (1) pre-tensioned.
- b) Type of cable profile, (0) straight, (1) parabolic and (2) other.
- c) Number of prestressing segments, defined by beginning and end of each segment.
- d) Friction coefficient.
- e) Wobbling coefficient.
- f) Type of steel, (0) low-relaxation and (1) stress-relieved.

23rd line

In as many lines as there are prestressing segments, see line 22c, five enterings are used to define:

- a) Number of the element at which the prestressing segment starts.
- b) Number of the element at which the prestressing segment ends.
- c) Cross-sectional area of the tendons.
- d) Initial prestressing force.
- e) Side of the prestressing segment at which the cable will be pulled: (1) left and (2) right, used for the calculation of friction losses.

24th line

When the assumed cable profile is either straight or parabolic, see line 22b, three nodal points are chosen to define the cable profile. In as many lines as there are prestressing segments the number of the nodal points and the distances from the cable to the bottom face of the girders, at those nodal points, are to be defined for each chosen node, respectively. When the cable profile is defined as other the vertical position of the cable shall be informed at each node, in as many lines as there are nodes.

The program output as shown in Appendix D, is divided into two sections: the first section refers to the input properties of each problem. It is repeated as many times as the number of problems analyzed and follows the same order used for data input, as explained in lines 1 through 24. The second section immediately follows, it presents all the results obtained by the finite element program and it is subdivided into

the following subsections:

(1) Global displacements - For each and all nodal points a global displacement number is assigned, in crescent order and skipping the prescribed degrees of freedom for which a zero is assigned.

(2) Storage needed - The total storage capacity needed for each problem is calculated. If the number is considerably different then the provided storage capacity, shown in the first output section, the latter may be changed accordingly.

(3) Dead load - Dead load of the girders and deck are separetely calculated and printed out for each of the elements.

(4) Original section properties - Transformed section properties, centroidal position, area and moments of area, are calculated for both possible situations: noncomposite and composite sections. Those properties refer to the original uncracked sections and are printed for all elements.

(5) New section properties - Updated section properties are printed at every new load case and step. Those properties reflect any changing of the material properties as well as cracking development at the sections.

(6) Nodal displacements - At every increment step, displacements for the step and the total accumulated displacements are printed for all nodal points and for the three possible directions, horizontal, transversal and rotational, respectively.

(7) Element forces - The total updated forces, axial, moment and shear, are calculated and printed for all elements, at every step. Those forces reflect the action of the external loading, reactions and prestressing effects as well.

(8) Reactions - Nodal external reactions, at all nodal supports, are calculated for the three directions and printed at every loading step.

(9) Prestressing cable properties - For all the elements under prestressing, the updated forces, stresses, strains and instant elastic moduli are calculated and printed at every loading step. This section is omitted in non prestressed problems.

(10) Strains - For all elements and at every loading step the updated and the maximum strains reached at the top and bottom surfaces of the girders and deck are printed, respectively.

(11) Cracking - For all elements and at every loading step, cracking length is printed for both girders and deck, starting from the top and bottom surfaces, respectively.

(12) Cracking layout - A complete cracking layout is printed for every loading step. For all elements and layers cracking is represented by 0's and uncracked layers by 1's.

(13) Crack angles - For all elements and layers the angles formed by the cracks with the horizontal direction are printed out, approximated by the nearest integer angle.

(14) Reinforcement stresses - Stresses at the three reinforcement levels, in the deck, top flange and bottom flange of the girders,

respectively, are printed at every load step and for all elements.

(15) Yielding layout - For all three reinforcement levels and all layers of a steel girder, a complete layout of yielding is printed by representing yielded layers by 0's. Similarly as for the cracking layout this is updated at every loading step.

(16) Checking elements - For all the chosen checking elements, see line 2h, and at every layer, centroidal position of the layer, cross-sectional area of the layer, stress, strain and instant modulus of the material are printed.

(17) Moment-curvature-deflection - After all loading steps are printed, a complete list of bending moments, curvatures, deflections, fraction of the applied load, current times and number of iterations are shown for all of the loading steps and every chosen checking elements. This list is immediately followed by a message indicating the reason for which the problem has been terminated.

(18) Support reactions - A complete list of the support reactions is printed for all supports and every loading step.

(19) Plots - Plots of the moment-curvature and moment-deflection distributions are available for each and all of the chosen checking elements.

8.2 Listing of the Program

```

65 C KVAR = GLOBAL DISP. MOD. FOR THEN D.D.N.
66 C ILL = INCIDENCE OF MODS IN EACH ELEM., ELEM.TYPE
67 C DISP = DISPLACEMENTS FOR THIS STEP
68 C SDISP = TOTAL MODAL DISPLACEMENTS
69 C CMF = CURRENT MODAL FORCES (1: UP TO LAST LOAD CASE
70 C 2: CURRENT
71 C 3: TOTAL THIS LOAD CASE )
72 C
73 C FORCE = SECTION FORCES, TOTAL, FROM EQUILIBRIUM
74 C ALOAD = MODAL APPLIED LOADS
75 C ELOAD = ELEMENT APPLIED LOADS
76 C CLOAD = ELEMENT EQUIVALENT MODAL FORCES
77 C DLOAD = MODAL FORCES
78 C DCL = DISTRIBUTED FORCES
79 C
80 C REAC = SUPPORT REACTIONS
81 C RELIST = LIST OF SUPPORT REACTIONS FOR ALL STEPS
82 C LOCA = LOAD CASES AND CONSTRUCTIONAL PATTERN
83 C PZDIS = PRESCRIBED DISPLACEMENTS AT SUPPORTS
84 C B = MODAL FORCES, MODAL DISPLACEMENTS
85 C CABLE = CABLE PROPERTIES AT THE NODES
86 C PNCAB = INIT. CABLE FORCES, MOD. SHEAR, AFTER FR. LOSSES
87 C CLOST = INITIAL CABLE STAINS (IN A STEP)
88 C JTP = SHEAR STRAINS UP TO PRESTRESSING
89 C PSCM = PROPERTIES OF EACH PRESTRESSED SEGMENT
90 C ELONG = CABLE LENGTH AND ELONGATION
91 C PEP = PARABOLIC OR STRAIGHT CABLE PROFILE
92 C Y = SECTION LAYERS: CENTROID, AREA AND WIDTH
93 C STA = STAIN AT CENTER LAYERS AND REINF. STEEL
94 C
95 C STB = STAIN AT SECTION BORDERS
96 C STST = STAIN ONLY FOR THIS STEP
97 C STEL = TOTAL ELASTIC STRAIN
98 C EPEN = ELASTIC STRAIN IN CONCRETE AT CRACKING
99 C STEH = STRESSES AT LAYERS AND REINF. STEEL
100 C
101 C CRACK = CRACKS AT THE LAYERS
102 C CRACK = CRACK ANGLE AT THE LAYERS
103 C CTRFPA = CRACK PROFILE, (0) STRAIGHT (1) PARABOLIC (2) OTHER
104 C YIELD = YIELDING AT STEEL LAYER AND REINF. STEEL
105 C FILL = ELASTIC MOD. FOR CONCR. AND REINF. STEEL
106 C ICHK = CHECKING ELEMENTS
107 C AK12 = S.M. NOW FOR THE DRIVING DISP.
108 C PI = LCAD VECTOR FOR THE D.D.N.
109 C T = CURRENT AND FIXED TIMES
110 C
111 C
112 C IMPLICIT REAL*8(A-H,O-Z)
113 C REAL*4 X(300),YY(10)
114 C DIMENSION A(20000),L(1000),Z(4),CDIM(8),PSCM(10,5),
115 C Y(50,4),I(6)
116 C
117 C READ(1,*)NDATA
118 C DO 999 J=1,NDATA
119 C WRITE(3,222)J
120 C WRITE(3,222)
121 C 2222 FORMAT(1,100(' '),/)
122 C 3000 FORMAT(1,50,'EXAMPLE *',12,/)
123 C WRITE(3,2222)
124 C I=INTP-20000

```

```

1000 WRITE(3,1000)LIMITP
      FORMAT(1X,'STORAGE PROVIDED = ',I10)
      WRITE(3,2222)
      WRITE(3,2000)
2000  FORMAT(1X,45X,' I N P U T   D A T A   ',/)
      WRITE(3,2222)
      READ(1,*)NCL,NCEL,NNOD,NSUP,WLOCA,WGL,WDL,WCHL
      NSOP3=NSUP*3
      NL=NCL+WDL
      NS1=NL+4
      NS2=NL+4
      NS3=NL+3
      NS4=WGL+3
      NCH3=WCHL*6
C.....NON INTEGER ARRAYS.....
C
      N1=1
C.....(N1-N2) COORDINATES ( X )
      N2=1+NNOD*2
C.....(N2-N3) APPLIED NODAL LOADS ( ALOAD )
      N3=N2+NNOD*3
C.....(N3-N4) NODAL FORCES, DISPLACEMENTS ( B )
      N4=N3+NNOD*3
C.....(N4-N5) APPLIED ELEMENT LOADS ( ALOAD )
      N5=N4+NEL*3
C.....(N5-N6) SUPPORT REACTIONS ( REAC )
      N6=N5+NSUP*3
C.....(N6-N7) SECTION DIMENSIONS ( DIM )
      N7=N6+NEL*8
C.....(N7-N8) STEEL CONTENT ( STEEL )
      N8=N7+NEL*6
C.....(N8-N9) SECTION PROPERTIES ( AREA )
      N9=N8+NEL*8
C.....(N9-N10) DEAD LOAD ( DELO )
      N10=N9+NEL*2
C.....(N10-N11) NODAL FORCES ( CLOAD )
      N11=N10+NNOD*3
C.....(N11-N12) DISTRIBUTED FORCES ( DLOAD )
      N12=N11+NEL*3
C.....(N12-N13) NODAL DISPLACEMENTS ( SDISP )
      N13=N12+NNOD*3
C.....(N13-N14)
      N14=N13
C.....(N14-N15) LOAD CASES ( LOCA )
      N15=N14+WLOCA*8
C.....(N15-N16) PRESCRIBED DISPLACEMENTS ( PREDIS )
      N16=N15+NSUP*2
C.....(N16-N17) CABLE POSITION ( YCABLE )
      N17=N16+NNOD
C.....(N17-N18) CABLE PROPERTIES ( CABLE )
      N18=N17+NEL*7
C.....(N18-N19) LAYER STRAINS, TOTAL ( STA )
      N19=N18+NEL*NS1
C.....(N19-N20) BORDER STRAINS, TOTAL ( STRB )
      N20=N19+NEL*8
C.....(N20-N21) STRAINS AT THIS STEP, LAYER ( STRST )
      N21=N20+NEL*NS2
C.....(N21-N22) CRACKING ( CRACK )
      N22=N21+NEL*8
C.....(N22-N23) ELASTIC MOD. VARIATION ( EALL )

```

```

125.      N23=N22+NEL*NS3
126. C.....(N23-N24) STRAINS AT CRACKING ( EPERM )
127.      N24=N23+NEL*NL
128. C.....(N24-N25) STRESSES ( STRE )
129.      N25=N24+NEL*NS3
130. C.....(N25-N26) CURRENT NODAL FORCES ( CNF )
131.      N26=N25+NNOD*9
132. C.....(N26-N27) TOTAL ELASTIC STRAINS ( STREL )
133.      N27=N26+NEL*NL
134. C.....(N27-N28) DISPLACEMENTS FOR THIS STEP ( DISP )
135.      N28=N27+NNOD*3
136. C.....(N28-N29) MOMENT-CURV-DISPL. ( DCM )
137.      N29=N28+NCH3*300
138. C.....(N29-N30) INCKEM. FORCES ( DCL )
139.      N30=N29+NNOD*3
140. C.....(N30-N31) ELASTIC STRAINS IN THE L.C. ( STRLC )
141.      N31=N30+NEL*NL
142. C.....(N31-N32) SECTION FORCES ( FORCE )
143.      N32=N31+NEL*3
144. C.....(N32-N33) S.M. COLUMN ( K12 )
145.      N33=N32+NNOD*3
146. C.....(N33-N34) NEW LOAD VECTOR ( P1 )
147.      N34=N33+NEL*3
148. C.....(N34-N35) DISPLACEMENT VECTOR ( DU )
149.      N35=N34+NNOD*3
150. C.....(N35-N36) INITIAL CABLE FORCES ( FIMCAB )
151.      N36=N35+NEL*3
152. C.....(N36-N37) INITIAL CABLE STRAINS IN STEP ( CABSST )
153.      N37=N36+NEL
154. C.....(N37-N38) SHEAR STRAINS UP TO-PRESTR. ( GTP )
155.      N38=N37+NEL
156. C.....(N38-N39) LIST OFF REACTIONS ( RELIST )
157.      N39=N38+300*10
158. C.....(N39- ) GLOBAL STIFFNESS MATRIX ( ST )
159. C
160. C.....INTEGER ARRAYS.....
161. C
162.      N1=1
163. C.....(N1-N2) GLOBAL DISPLACEMENTS ( NVAR )
164.      N2=N1+NNOD*3
165. C.....(N2-N3) NODAL CONDITION ( IVAR )
166.      N3=N2+NNOD*3
167. C.....(N3-N4) ELEM'S INCIDENCE,TYPE ( IEL )
168.      N4=N3+NEL*3
169. C.....(N4-N5) CRACK AT THE LAYERS ( ICRACK )
170.      N5=N4+NEL*NL
171. C.....(N5-N6) CRACK ANGLE AT LAYERS ( IALPHA )
172.      N6=N5+NEL*NL
173. C.....(N6-N7) YIELDING ( IELD )
174.      N7=N6+NEL*NS4
175. C.....(N7-N8) CHECKING ELEMENTS ( ICHECK )
176.      N8=N7+NCHL
177. C.....(N8-N9) NEW GLOBAL DISP FOR THE D.D.M. ( KVAR )
178.      N9=N8+NNOD*3
179. C
180.      LIMIT1=N9
181.      WRITE(3,2100)NCL
182.      2100 FORMAT(1X,'NUMBER OF ELEMENTS =',I5,///)
183.      WRITE(3,2150)NCHL
184.      2150 FORMAT(1X,'NUMBER OF CONNECTION ELEMENTS =',I5,///)

```



```

2200 WRITE(3,2200)NNOD
      FORMAT(1X,'NUMBER OF NODES =',I5,/)
      WRITE(3,2250)NSUP
2250 FORMAT(1X,'NUMBER OF SUPPORTS =',I5,/)
      WRITE(3,2222)
      CALL INPUT(NNOD,NSUP,NEL,E,A(N1),IA(N3),IA(N2),A(N4),A(N2),A(N3)
      * ,NDISP,BC,A(N6),CDIM,A(N7),A(N8),IGMAT,IATYPE,ICONST,GAMAG,GAMAD
      * ,NLOCA,A(N14),A(N15),A(N16),A(N17),IPRET,MPS,PSEGM,PM,PK,
      * ,MS3,A(N22),NGL,NL,IA(N7),NCHL,ISSC,DRIVIL,NODR,ALPLL,IT1,IT2,
      * ,IT3,T,IST)
      CALL BAND(NEL,IA(N3),NBAND)
      CALL GDISP(NNOD,IA(N3),IA(N2),NDISP)
      LIMIT=N39+NNOD*NBAND
      NODR3=NNOD*3
      WRITE(3,2222)
      LIMIT=LIMIT+LIMIT
      WRITE(3,1500)LIMIT
1500 FORMAT(1X,' STORAGE NEEDED = ',I15)
      IF (LIMIT.LE.LIMITP)GO TO 99
      WRITE(3,1600)
1600 FORMAT(1X,'THE PROGRAM HAS TERMINATED SINCE THE
      * PROVIDED STORAGE IS NOT SUFFICIENT '/')
      CALL EXIT
      99 CONTINUE
      CALL CONSTR(IGMAT,IATYPE,NLOCA,GAMAG,GAMAD,NNOD,NSUP,NEL,NCHL,
      * ,NODR3,NDISP,NBAND,E,BC,IA(N1),IA(N2),IA(N3),A(N1),A(N2),
      * ,A(N3),A(N4),A(N5),A(N6),A(N7),A(N8),A(N9),A(N10),A(N11),A(N12)
      * ,A(N14),A(N15),A(N16),A(N17),IPRET,MPS,PSEGM,PM,PK,
      * ,ICNST,A(N18),A(N19),A(N20),A(N21),NGL,NL,NS1,NS2,MS3,MS4,
      * ,A(N22),T,IA(N4),IA(N5),IA(N6),A(N23),A(N24),A(N25),IA(N7),
      * ,NSUP3,A(N27),A(N28),A(N29),A(N31),A(N36),A(N30),A(N32),
      * ,A(N33),IA(N8),A(N34),A(N35),A(N36),A(N37),A(N38),A(N39),NCHL,
      * ,NCH3,ISSC,DRIVIL,NODR,AK22,ALPLL,ITNST,IT1,IT2,IT3,T,IST)
      CALL PLOT(IX,YY,A(N28),ITNST,NCH3,IA(N7),NCHL)
999 CONTINUE
      STOP
      INC
C *****
      SUBROUTINE INPUT(NNOD,NSUP,NEL,E,X,IEL,IVAR,APLOAD,ALOAD,B
      * ,NDISP,BC,DIM,CDIM,STEEL,AREA,IGMAT
      * ,IATYPE,ICONST,GAMAG,GAMAD,NLOCA,LOCA,
      * ,PREDIS,YCABLE,CABLE,IPRET,MPS,PSEGM,PM,PK,
      * ,MS3,EALL,NGL,NL,ICHECK,NCHL,ISSC,DRIVIL,NODR,ALPLL,IT1,IT2,
      * ,IT3,T,IST)
C *****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION X(NNOD,2),IVAR(NNOD,3),IEL(NEL,3),DIM(NEL,8),CDIM(8)
      * ,B(1),ALOAD(NNOD,3),APLOAD(NEL,3),STEEL(NEL,6)
      * ,E(4,6),AREA(NEL,8),LOCA(NLOCA,8),PREDIS(NSUP,2)
      * ,YCABLE(NNOD),CABLE(NEL,7),PSEGM(10,5),PRF(10,6)
      * ,EALL(NEL,NS3),ICHECK(NCHL),T(6)
      IF (NCHL.GT.0) THEN
        READ(1,*) (ICHECK(I),I=1,NCHL)
      END IF
      READ(1,*) BC
      READ(1,*) DRIVIL,NODR,ALPLL
      WRITE(3,2300)
2300 FORMAT(10X,'P R O P E R T I E S ')
      WRITE(3,1111)

```

```

245. 1111 FORMAT(/,130(' '),/)
246. WRITE(3,2310)
247. 2310 FORMAT(29X,'0',17X,'1',16X,'2',/,/,1X,'GIRDER MATERIAL',8X,
248. * 'STEEL',13X,'PREST. CONC',7X,'REINF. CONC',/,/,
249. * 1X,'GIRDER TYPE ',11X,'RECTANGULAR',7X,'I,T OR BOX',/,/,
250. * 1X,'SECTION DIMENTIONS',5X,'CONSTANT',10X,'VARIABLE',/,/,
251. * 1X,'STEEL DISTRIBUTION',5X,'CONSTANT',10X,'VARIABLE',/,/,
252. * 1X,'COMPOSITE SECTION',6X,'NON COMP.',9X,'COMPOSITE',/,/,
253. * 1X,'STRESS-STRAIN CURVE',4X,'HOGNESTAD',9X,'BILINEAR')
254. WRITE(3,1111)
255. WRITE(3,2400)BC
256. 2400 FORMAT(/,1X,'SEABING COEF.=',D15.5,/)
257. READ(1,*) IGMAT,IATYPE,ICONST,ISTEEL,ISSC
258. READ(1,*) GAMAG,GAMAD
259. T(1)=28
260. READ(1,*) (T(I),I=2,6)
261. WRITE(3,120)GAMAG,GAMAD
262. 120 FORMAT(1X,'GIRDER MAT. UNIT WEIGHT =',D15.8,/,/,
263. * 1X,'DECK MAT. UNIT WEIGHT =',D15.8,/)
264. WRITE(3,1)IGMAT,IATYPE,ICONST,ISTEEL,ISSC
265. 1 FORMAT(1X,'GIRDER MATERIAL=',I2,/,/,
266. * 1X,'SECTION TYPE=',I2,/,/,
267. * 1X,'SECTION DIMENTIONS=',I2,/,/,
268. * 1X,'STEEL DISTRIBUTION=',I2,/,/,
269. * 1X,'STRESS-STRAIN CURVE=',I2,/)
270. WRITE(3,9)T(2),T(4),T(1),T(5),T(6)
271. 9 FORMAT(1X,'TIME LIST :',5X,'GIRDER CASTING',5X,D10.3,' DAYS',/,/,
272. * 17X,' 1ST LOADING',5X,D10.3,' " ',/,/,
273. * 17X,' DECK CASTING',5X,D10.3,' " ',/,/,
274. * 17X,' 1ST LOADING',5X,D10.3,' " ',/,/,
275. * 16X,' PRESTRESSING ',4X,D10.3,' " ')
276. 2222 FORMAT(/,130(' '),/)
277. DO 121 I=1,4
278. READ(1,*) (E(I,J),J=1,6)
279. 121 CONTINUE
280. DO 123 I=1,NEL
281. DO 124 J=1,NL
282. CALL (I,J)=E(3,1)
283. CONTINUE
284. LIM=NS1+1
285. DO 125 J=LIM,NL
286. CALL (2,J)=E(4,1)
287. CONTINUE
288. DO 126 J=1,3
289. CALL (I,NL+J)=E(2,1)
290. CONTINUE
291. 123 CONTINUE
292. WRITE(3,2222)
293. WRITE(3,70)
294. 70 FORMAT(15X,'M A T E R I A L P R O P E R T I E S ')
295. WRITE(3,1111)
296. WRITE(3,71)
297. 71 FORMAT(3X,'P/S : E0, E1, E2, SY1, SY2, EU',/,/,
298. * 3X,'R/S : E0, EY, 0, 0, 0, EU',/,/,
299. * 3X,'G/S : E0, EY, 0, 0, 0, EU',/,/,
300. * 1X,'C/C : E0, FC1, EB, 0, 0, EU',/,/,
301. * 3X,'D/C : E0, FC1, EB, 0, 0, EU',/)
302. WRITE(3,1111)
303. WRITE(3,72) (E(1,1),I=1,6)
304. 72 FORMAT(1X,'PREST. STEEL:',6(3X,D12.5),/)
305.
306.
307.
308.
309.
310.
311.
312.
313.
314.
315.
316.
317.
318.
319.
320.
321.
322.
323.
324.
325.
326.
327.
328.
329.
330.
331.
332.
333.
334.
335.
336.
337.
338.
339.
340.
341.
342.
343.
344.
345.
346.
347.
348.
349.
350.
351.
352.
353.
354.
355.
356.
357.
358.
359.
360.
361.
362.
363.

```

```

WRITE(3,73) (E(2,I), I=1,6)
73 FORMAT(1X,'REINFORCING STEEL',6(3X,D12.5),/)
WRITE(3,74) (Z(3,I), I=1,6)
74 FORMAT(1X,'GIRDER MAT.',6(3X,D12.5),/)
WRITE(3,75) (E(4,I), I=1,6)
75 FORMAT(1X,'DECK CONC.',6(3X,D12.5),/)
WRITE(3,2222)
WRITE(3,1300)
1300 FORMAT(1X,'ELEMENT INCIDENCE & TYPE')
WRITE(3,1311)
WRITE(3,1400)
1400 FORMAT(1X,'ELEM #',8X,'M1',6X,'M2',4X,'TYPE',/)
DO 20 I=1,NEL
  READ(1,*) IEL(I,1), IEL(I,2), IEL(I,3)
  ITYPE=IEL(I,3)
  WRITE(3,1500) I, IEL(I,1), IEL(I,2), ITYPE
1500 FORMAT(2X,15,6X,I3,5X,I3,5X,I3,/)
20 CONTINUE
  WRITE(3,2222)
  DO 10 I=1,NMOD
    READ(1,*) X(I,1), X(I,2), IVAR(I,1), IVAR(I,2), IVAR(I,3)
  10 CONTINUE
  WRITE(3,1000)
1000 FORMAT(1X,'MODAL COORDINATES')
  WRITE(3,1111)
  WRITE(3,1100)
1100 FORMAT(1X,'MODE #',6X,'X',15X,'Y',/)
  WRITE(3,1200) (I,X(I,1), X(I,2), I=1,NMOD)
1200 FORMAT(4X,I3,4X,D12.5,4X,D12.5,/)
  WRITE(3,2222)
C      CONSTANT CROSS SECTION
  IF (ICCWST.EQ.3) THEN
    READ(1,*) (CDIM(I), I=1,8)
    DO 2 I=1,NEL
      DO 3 J=1,8
        DIM(I,J)=CDIM(J)
      3 CONTINUE
      IF (IEL(I,3).EQ.1) THEN
        DIM(I,3)=CDIM(2)/2+CDIM(4)+CDIM(6)+CDIM(8)
        IF (IGMAT.EQ.0) DIM(I,3)=CDIM(2)/2+CDIM(4)
        DIM(I,4)=DIM(I,3)
        DIM(I,5)=0
        DIM(I,6)=0
        DIM(I,7)=0
        DIM(I,8)=0
      END IF
    2 CONTINUE
  ELSE
    VARIABLE CROSS SECTION
    DO 60 I=1,NEL
      READ(1,*) (DIM(I,J), J=1,8)
    60 CONTINUE
    END IF
    WRITE(3,30)
30 FORMAT(20X,'SECTIONAL DIMENSIONS',/)
    WRITE(3,1111)
C      STEEL GIRDER
    IF (IGMAT.EQ.0) THEN
      WRITE(3,4)
4 FORMAT(1X,'ELEM #',3X,'DECK WIDTH', 2X,

```

```

364 *      'DECK THICK.', 2X,
365 *      'GIRDER AREA', 2X,
366 *      'GIRDER HEIGHT', 2X,
367 *      'MOM. INERTIA', //)
368
369 DO 5 I=1,NEL
370   IF (IEL(I,3).EQ.1) THEN
371     WRITE(3,55) I, (DIM(I,J), J=1,4)
372   55 FORMAT(4X,I3,2X,D13.6,2X,D13.6,5X,'H1=',D11.4,9X,'H2=',D11.4,/)
373   ELSE
374     WRITE(3,6) I, (DIM(I,J), J=1,5)
375   6 FORMAT(4X,I3,5(2X,D13.6),/)
376   END IF
377   5 CONTINUE
C      CONCRETE RECTANGULAR GIRDER
378   ELSE
379     IF (ITYPE.EQ.0) THEN
380       WRITE(3,7)
381     7 FORMAT(1X,'ELEM #',3X,'DECK WIDTH', 2X,'DECK THICK.',
382 *      '2X','GIRDER WIDTH', 2X,'GIRDER HEIGHT',/)
383     DO 8 I=1,NEL
384       IF (IEL(I,3).EQ.1) THEN
385         WRITE(3,55) I, (DIM(I,J), J=1,4)
386       ELSE
387         WRITE(3,29) I, (DIM(I,J), J=1,4)
388     29 FORMAT(4X,I3,4(2X,D13.6),/)
389     END IF
390     8 CONTINUE
C      CONCRETE T, I OR BOX GIRDER
391     ELSE
392       WRITE(3,100)
393     100 FORMAT(1X,'ELEM #',3X,'DECK WIDTH', 2X,'DECK THICK.',
394 *      '2X','TOP WIDTH', 2X,'TOP THICK.',
395 *      '2X','WEB WIDTH', 2X,'WEB THICK.',
396 *      '2X','BOTTOM WIDTH', 2X,'BOTTOM THICK.',/)
397     DO 110 I=1,NEL
398       IF (IEL(I,3).EQ.1) THEN
399         WRITE(3,55) I, (DIM(I,J), J=1,4)
400       ELSE
401         WRITE(3,12) I, (DIM(I,J), J=1,8)
402     12 FORMAT(4X,I3,8(2X,D13.6),/)
403     END IF
404     110 CONTINUE
405     END IF
406     END IF
407     WRITE(3,2222)
408     IF (ISTEEL.EQ.0) THEN
409       READ(1,*) (STEEL(I,J), J=1,6)
410     DO 40 I=2,NEL
411       DO 49 J=1,6
412         STEEL(I,J)=STEEL(1,J)
413       IF (IEL(I,3).EQ.1.AND.J.GE.3) STEEL(I,J)=0
414     49 CONTINUE
415     48 CONTINUE
416     ELSE
417       DO 50 I=1,NEL
418         READ(1,*) (STEEL(I,J), J=1,6)
419     50 CONTINUE
420     END IF
421     WRITE(3,13)
422     13 FORMAT(30X,'REINFORCING STEEL CONTENT',/)
423
424
425
426
427
428
429
430
431
432
433
434
435
436
437
438
439
440
441
442
443
444
445
446
447
448
449
450
451
452
453
454
455
456
457
458
459
460
461
462
463
464
465
466
467
468
469
470
471
472
473
474
475
476
477
478
479
480
481
482
483

```



```

WRITE(3,1111)
WRITE(3,14)
14 FORMAT(20X,'DECK',16X,'GIRDER TOP',8X,
* 'GIRDER BOTTOM')
WRITE(3,1111)
WRITE(3,15)
15 FORMAT(1X,'ELEM #',6X,'AREA',8X,'DIST.TO BASE',
* 6X,'AREA',8X,'DIST.TO BASE',
* 6X,'AREA',8X,'DIST.TO BASE',//)
DO 16 I=1,NEL
WRITE(3,17) I, (STEEL(I,J), J=1,6)
17 FORMAT(4X,13,6(2X,D13.6),//)
16 CONTINUE
WRITE(3,2222)
DO 200 I=1,NLOCA
READ(1,*) (LOCA(I,J), J=1,8)
IF (LOCA(I,1).EQ.2) LOCA(I,3)=1
200 CONTINUE
WRITE(3,210)
210 FORMAT(15X,'LOAD CASES')
WRITE(3,1111)
WRITE(3,220)
220 FORMAT(2X,'(1)',2X,'GIRDER DEAD LOAD',//
* 2X,'(2)',2X,'PRESTRESSING',//
* 2X,'(3)',2X,'DECK DEAD LOAD',//
* 2X,'(4)',2X,'SUPPORT DISPLACEMENT',//
* 2X,'(5)',2X,'LIVE LOAD',//
* 2X,'(6)',2X,'TEMPERATURE',//
* 2X,'(7)',2X,'CREEP, SHRINKAGE AND RELAXATION',///
* 8X,'EFFECT TABLE',//
* 8X,' 0 NONE',//
* 8X,' 1 CREEP',//
* 8X,' 2 SHRINKAGE',//
* 8X,' 3 RELAXATION',//
* 8X,' 4 ALL')
WRITE(3,1111)
WRITE(3,230)
230 FORMAT(1X,'LOAD CASE #',3X,'TYPE',3X,'COMP.SECTION',
* 3X,'# STEPS',3X,'PRINT STEP',3X,'EFFECT',3X,'P. DAY',3X,
* 'L. DAY',3X,'HINGED',//)
DO 240 I=1,NLOCA
WRITE(3,250) I, (LOCA(I,J), J=1,8)
250 FORMAT(10X,12,4X,12,9X,11,11X,12,11X,11,9X,11,7X,14,5X,14,
* 5X,14,/)
240 CONTINUE
WRITE(3,1111)
WRITE(3,260)
260 FORMAT(1X,'DESCRIBED DISPLACEMENTS',//
* 1X,'SUP #',2X,'NODE #',3X,'DISP.VALUE',//)
DO 270 I=1,NSUP
READ(1,*) (PREDIS(I,J), J=1,2)
NM=PREDIS(I,1)
WRITE(3,280) I,NM,PREDIS(I,2)
280 FORMAT(4X,12,5X,13,3X,E10.3,/)
270 CONTINUE
WRITE(3,1111)
READ(1,*) IT1,IT2,IT3
WRITE(3,2000)
2000 FORMAT(1X,'TEMPERATURE VARIATION (F)',//)
WRITE(3,2001)

```

```

484 2001 FORMAT(1X,'TOP DECK',5X,'TOP GIRDER',5X,'BOTTOM GIRDER',//)
485 WRITE(3,2002) IT1,IT2,IT3
486 2002 FORMAT(3X,14,10X,14,13X,14)
487 WRITE(3,2222)
488 WRITE(3,1504)
489 1504 FORMAT(30X,'LIVE LOAD')
490 WRITE(3,2222)
491 WRITE(3,1505)
492 1505 FORMAT(/,10X,'NODAL APPLIED LOADS (*) R,UP,CC')
493 WRITE(3,1111)
494 WRITE(3,1506)
495 1506 FORMAT(1X,'NODE #',15X,'FX',16X,'FY',16X,'MZ',//)
496 DO 21 I=1,NMCD
497 READ(1,*) ALOAD(I,1),ALOAD(I,2),ALOAD(I,3)
498 WRITE(3,1507) I,ALOAD(I,1),ALOAD(I,2),ALOAD(I,3)
499 1507 FORMAT(4X,13,8X,D15.8,5X,D15.8,5X,D15.8,/)
500 21 CONTINUE
501 WRITE(3,2222)
502 WRITE(3,1510)
503 1510 FORMAT(/,10X,'ELEMENT APPLIED LOADS (*) DOWN')
504 WRITE(3,1111)
505 WRITE(3,1520)
506 1520 FORMAT(1X,'ELEM #',11X,'U.DIST.',11X,'CONC.',15X,'FR.L.NODE',//)
507 DO 25 I=1,NEL
508 READ(1,*) APLD(I,1),APLND(I,2),APLND(I,3)
509 WRITE(3,1530) I,APLND(I,1),APLND(I,2),APLND(I,3)
510 1530 FORMAT(4X,13,8X,D15.8,5X,D15.8,5X,D15.8,/)
511 25 CONTINUE
512 WRITE(3,2222)
513 IF (DWBVLL.EQ.0) THEN
514 WRITE(3,1535)
515 1535 FORMAT(10X,'LOAD DRIVEN METHOD FOR L.L.',/)
516 ELSE
517 WRITE(3,1541)
518 1541 FORMAT(10X,'DISPLACEMENT DRIVEN METHOD FOR L.L.',/)
519 WRITE(3,1542) NMCD,DRVLL
520 1542 FORMAT(10X,'NODE #',13,5X,'AT',5X,D15.8,/)
521 WRITE(3,1543) A1PLL
522 1543 FORMAT(10X,'L.I UPPER LIMIT = ',D10.3,1X,'X',/)
523 ENC IF
524 C PRESTRESSING
525 DO 31 I=1,NMCD
526 YCAPLE(I)=0
527 31 CONTINUE
528 DO 32 I=1,NEL
529 DO 33 J=1,7
530 CABLE(I,J)=0
531 33 CONTINUE
532 32 CONTINUE
533 IPIET=0
534 NPS=1
535 DO 36 I=1,10
536 DO 37 J=1,5
537 PSEGM(I,J)=0
538 37 CONTINUE
539 36 CONTINUE
540 IF (IGMAT.EQ.1) THEN
541 WRITE(3,2222)
542 WRITE(3,1540)
543 1540 FORMAT(30X,'PRESTRESSING')

```

```

WRITE(3,2222)
READ(1,*)IPRPF,IPROF,NPS,FM,FK,IST
WRITE(3,1570)
1570 FORMAT(5X,'PRESTRESSING AREA AND INITIAL FORCE',/)
IF (IPRPF.EQ.0) THEN
  WRITE(3,1575)
1575 FORMAT(1X,15X,'( POS-TENSIONED CABLE )')
  IF (IST.EQ.0) THEN
    WRITE(3,1577)
1577 FORMAT(1X,15X,'( LOW-RELAXATION STEEL )')
  ELSE
    WRITE(3,1578)
1578 FORMAT(1X,15X,'( STRESS-RELIEVED STEEL )')
  END IF
  ELSE
    FM=0
    FK=0
    WRITE(3,1576)
1576 FORMAT(1X,15X,'( PRE-TENSIONED CABLE )')
    IF (IST.EQ.0) THEN
      WRITE(3,1577)
    ELSE
      WRITE(3,1578)
    END IF
    END IF
    WRITE(3,1111)
    WRITE(3,1580)
1580 FORMAT(1X,'FROM ELEM # TO ELEM #',7X,'AREA',8X,
  * 'INITIAL FORCE',5X,'JACKING SIDE',/)
    DO 40 I=1,NPS
      READ(1,*)PSEGN(I,1),PSEGN(I,2),PSEGN(I,3),PSEGN(I,4),PSEGN(I,5)
      NE1=PSEGN(I,1)
      NE2=PSEGN(I,2)
      AO=PSEGN(I,3)
      FO=PSEGN(I,4)
      IPULL=PSEGN(I,5)
      WRITE(3,1590)NE1,NE2,AO,FO,IPULL
1590 FORMAT(9X,13,9X,13,3X,D12.5,4X,D13.6,12X,I1,/)
    40 CONTINUE
    WRITE(3,2222)
    WRITE(3,1550)
1550 FORMAT(10X,'C A B L E   P R O F I L E',/)
    IF (IPROF.EQ.0) THEN
      WRITE(3,1600)
1600 FORMAT(15X,'( STRAIGHT )')
    END IF
    IF (IPROF.EQ.1) THEN
      WRITE(3,1601)
1601 FORMAT(15X,'( PARABOLIC )')
    END IF
    IF (IPROF.EQ.2) THEN
      WRITE(3,1602)
1602 FORMAT(15X,'( OTHER )')
    END IF
    WRITE(3,1111)
    WRITE(3,1555)
1555 FORMAT(1X,'NODE #',3X,'DIST. TO BASE',/)
    IF (IPROF.LT.2) THEN
      DO 41 I=1,NPS
        READ(1,*) (PRF(I,J),J=1,6)

```

```

604 41 CONTINUE
605 CALL PROFIL(PRF,NPS,IPROF,NNOD,YCABLE,X)
606 ELSE
607 DO 35 I=1,NNCD
608 READ(1,*)YCABLE(I)
609 35 CONTINUE
610 END IF
611 DO 42 I=1,NNCD
612 WRITE(3,1560)I,YCABLE(I)
1560 FORMAT(4X,13,3X,D12.5,/)
613 42 CONTINUE
614 END IF
615 WRITE(3,2222)
616 WRITE(3,1015)
1015 FORMAT(1X,50X,' R E S U L T S ',/)
617 WRITE(3,2222)
618 RETURN
619
620 C*****
621
622 SUBROUTINE PROFIL(PRF,NPS,IPROF,NNOD,YCABLE,X)
623 C*****
624 IMPLICIT REAL*8 (A-H,O-Z)
625 DIMENSION PRF(10,6),YCABLE(NNOD),X(NNOD,2)
626 DO 10 I=1,NPS
627 N1=PRF(I,1)
628 N2=PRF(I,2)
629 N3=PRF(I,3)
630 X2=X(N1,1)-X(N1,1)
631 X3=X(N2,1)-X(N1,1)
632 Y1=PRF(I,4)
633 Y2=PRF(I,4)
634 Y3=PRF(I,6)
635 IF (IPROF.EQ.1) THEN
636 A=((Y3-Y2)-(Y2-Y1)*(X3/X2-1))/((X3**2-X2**2)-X2*(X3-X2))
637 B=((Y2-Y1)/X2)-A*X2
638 DO 20 J=N1,N3
639 XN=X(J,1)-X(N1,1)
640 YCABLE(J)=A*XN**2+B*XN+Y1
641 20 CONTINUE
642 ELSE
643 DO 30 J=N1,N3
644 XN=X(J,1)-X(N1,1)
645 IF (XN.LE.X2) THEN
646 YCABLE(J)=Y2+(Y1-Y2)*(X2-XN)/X2
647 ELSE
648 YCABLE(J)=Y2+(Y3-Y2)*(XN-X2)/(X3-X2)
649 30 CONTINUE
650 END IF
651 10 CONTINUE
652 RETURN
653
654 C*****
655
656 SUBROUTINE BAND(NEL,I2L,NDAND)
657 C*****
658 IMPLICIT REAL*8 (A-H,O-Z)
659 DIMENSION I2L(NEL,4)
660 INTEGER DIF,IOIP
661
662
663
664
665
666
667
668
669
670
671
672
673
674
675
676
677
678
679
680
681
682
683
684
685
686
687
688
689
690
691
692
693
694
695
696
697
698
699
700
701
702
703
704
705
706
707
708
709
710
711
712
713
714
715
716
717
718
719
720
721

```

```

      NBAND=0
      IDIF=0
      DO 10 I=1,NEL
        DIF=IEL(I,1)-IEL(I,2)
        IF (DIF-1E-0) DIF=-DIF
        IF (DIF.GT.IDIF) IDIF=DIF
      10 CONTINUE
      NBAND=3*IDIF+1
      WRITE(3,1010)NBAND
1010  FORMAT(1X,'NBAND=',I5,/)
      RETURN
      END
C*****
      SUBROUTINE GDISP(NMOD,NVAR,IVAR,NDISP)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION NVAR(NMOD,3),IVAR(NMOD,3)
      NDISP=0
C
      NVAR - STORES THE GLOBAL DISPLACEMENTS
C
      DO 11 I=1,NMOD
        DO 9 J=1,3
          NVAR(I,J)=IVAR(I,J)
          IF (NVAR(I,J).EQ.0) THEN
            NDISP=NDISP+1
            NVAR(I,J)=NDISP
          ELSE
            NVAR(I,J)=0
          END IF
        9 CONTINUE
      11 CONTINUE
      WRITE(3,2222)
      WRITE(3,1600)
1600  FORMAT(1/,10X,'GLOBAL DISPLACEMENT #')
      WRITE(3,1111)
1111  FORMAT(1/,130(' '),/)
      WRITE(3,1700)
1700  FORMAT(1X,'NODE #',7X,'X',5X,'Y',3X,'THETA',///)
      WRITE(3,1800) (I,(NVAR(I,J),J=1,3),I=1,NMOD)
1800  FORMAT(2X,15,5X,I3,3X,I3,3X,I3,/)
      WRITE(3,2222)
2222  FORMAT(1/,130(' '),/)
      RETURN
      END
C*****
      SUBROUTINE CONSTR(IGMAT,IATYPE,NLOCA,GAMAG,GAMAD,
      * NMOD,NSUP,NEL,NCEL,NODE3,NDISP,NBAND,E,DC,NVAR,IVAR,
      * IEL,X,ALOAD,D,APLOAD,REAC,DIM,STEEL,AREA,DELO,CLCAD,
      * CLOAD,SDISP,LOCA,PREDIS,YCABLE,CABLE,IPRET,
      * NPS,PSEJM,FM,FK,ICONST,STA,STRB,STRST,CRACK,
      * NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPERM,
      * STRE,CWF,ICHECK,NSUP3,DISP,DCM,DCL,FORCE,STREL,STRIC,
      * AK12,NVAR,P1,EU,FINCAB,CABSST,GTP,RELIST,ST,NCHEL,NCH3,ISSC,
      * EDIVLE,NCDR,AK22,ALPLL,ITNST,IT1,IT2,IT3,T,IST)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION E(4,6),NVAR(NMOD,3),IEL(NEL,3),X(NMOD,2),ALOAD(NMOD,3),

```

```

722  *B(1),AFLOAD(NEL,3),REAC(NSUP,3),DIM(NEL,8),IVAR(NMOD,3)
723  *STEEL(NEL,6),AREA(NEL,8),DELO(NEL,2),ST(NODE3,NBAND)
724  *CLOAD(NMOD,3),CLOAD(NEL,3),SDISP(NMOD,3),DISP(NMOD,3)
725  *LOCA(NLOCA,8),PREDIS(NSUP,2),YCABLE(NMOD),CABLE(NEL,7),
726  *RELIST(300,10),PSEJM(10,3),ELONG(10,2),STA(NEL,NS1),STRB(NEL,8),
727  *FINCAB(NEL,3),CABSST(NEL),STRST(NEL,NS2),CRACK(NEL,8),Y(NL,3),
728  *GTP(NGL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3),STRIC(NEL,NL)
729  *EPERM(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CWF(NODE3,3),
730  *ICHECK(NCHEL),DCM(300,NCH3),DCL(NMOD,3),STREL(NEL,NL),
731  *FORCE(NEL,3),AK12(1),P1(1),DU(1),NVAR(NMOD,3),T(6)
732  C
733  C
734  C
735  C
736  C
737  C
738  C
739  C
740  C
741  C
742  C
743  C
744  C
745  C
746  C
747  C
748  C
749  C
750  C
751  C
752  C
753  C
754  C
755  C
756  C
757  C
758  C
759  C
760  C
761  C
762  C
763  C
764  C
765  C
766  C
767  C
768  C
769  C
770  C
771  C
772  C
773  C
774  C
775  C
776  C
777  C
778  C
779  C
780  *B(1),AFLOAD(NEL,3),REAC(NSUP,3),DIM(NEL,8),IVAR(NMOD,3)
781  *STEEL(NEL,6),AREA(NEL,8),DELO(NEL,2),ST(NODE3,NBAND)
782  *CLOAD(NMOD,3),CLOAD(NEL,3),SDISP(NMOD,3),DISP(NMOD,3)
783  *LOCA(NLOCA,8),PREDIS(NSUP,2),YCABLE(NMOD),CABLE(NEL,7),
784  *RELIST(300,10),PSEJM(10,3),ELONG(10,2),STA(NEL,NS1),STRB(NEL,8),
785  *FINCAB(NEL,3),CABSST(NEL),STRST(NEL,NS2),CRACK(NEL,8),Y(NL,3),
786  *GTP(NGL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3),STRIC(NEL,NL)
787  *EPERM(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CWF(NODE3,3),
788  *ICHECK(NCHEL),DCM(300,NCH3),DCL(NMOD,3),STREL(NEL,NL),
789  *FORCE(NEL,3),AK12(1),P1(1),DU(1),NVAR(NMOD,3),T(6)
790  C
791  C
792  C
793  C
794  C
795  C
796  C
797  C
798  C
799  C
800  C
801  C
802  C
803  C
804  C
805  C
806  C
807  C
808  C
809  C
810  C
811  C
812  C
813  C
814  C
815  C
816  C
817  C
818  C
819  C
820  C
821  C
822  C
823  C
824  C
825  C
826  C
827  C
828  C
829  C
830  C
831  C
832  C
833  C
834  C
835  C
836  C
837  C
838  C
839  C

```



```

302 CONTINUE
301 CONTINUE
DO 303 I=1,300
DO 304 J=1,NCH3
CCM(I,J)=0
304 CONTINUE
DO 305 K=1,10
RELIST(I,K)=0
305 CONTINUE
303 CONTINUE
CALL DELOAD(IGMAT,IATYPE,GAMAG,GAMAD,DIM,WEL,IEL,DELC)
* CALL SCAO(IGMAT,IATYPE,GAMAG,GAMAD,DIM,E,STEEL,WEL,
IEL,AREA)
C
C
C
GO TO ALL LOAD CASES
C
LLCEL=0
INCLUD=0
ICOUNT=0
IAPTR=0
NOWPRO=0
ITEST=0
MTITER=0
FINISH=0
ICSTR=0
SHEAL=1
AKZ2=0
DO 500 LC=1,MLOCA
C
C
C
LATE HINGED SUPPORT
IF (LOCA(LC,6).EQ.1) BC=1.E30
IF (LOCA(LC,1).EQ.-5) THEN
LOCA(LC,1)=5
LIVLO=-1
ELSE
LIVLO=1
END IF
ICSTR=LCCA(LC,2)
C
C
C
UPDATE LATE CONNECTION ELEMENTS
FOR LIVE LOAD CONTINUITY
IF (WCEL.GT.0.AND.ICOMP.EQ.0) THEN
DO 10 NE=1,NEL
IF (IEL(NE,3).EQ.2) THEN
IEL(NE,3)=1
LLCEL=2
END IF
10 CONTINUE
END IF
IF (LLCEL.EQ.2.AND.ICOMP.EQ.1) THEN
DO 20 NE=1,NEL
IF (IEL(NE,3).EQ.1) IEL(NE,3)=0
20 CONTINUE
END IF
C
C
C
UPDATE CURRENT TIME
T(1)=LCCA(LC,6)
C
C
C
UPDATE LOADING TIMES
IF (LOCA(LC,1).LE.5) THEN
IF (ICOMP.EQ.0) THEN
T(4)=LCCA(LC,6)
ELSE
T(4)=LCCA(LC,6)

```

```

840 T(5)=LOCA(LC,6)
841 END IF
842 END IF
843 C
844 IF (NOWPRO.EQ.1) IAPTR=1
845 NOWPRO=0
846 IF (ICOUNT.EQ.1) INCLUD=1
847 IF (LOCA(LC,1).GE.6) ICSTR=1
848 C
849 IF (LCCA(LC,1).EQ.1) GO TO 1
850 IF (LCCA(LC,1).EQ.2) GO TO 2
851 IF (LOCA(LC,1).EQ.3) GO TO 3
852 IF (LOCA(LC,1).EQ.4) GO TO 4
853 IF (LCCA(LC,1).EQ.5) GO TO 5
854 IF (LOCA(LC,1).EQ.6) GO TO 6
855 IF (LCCA(LC,1).EQ.7) GO TO 7
856 C
857 1 DO 510 J=1,NEL
858 DLOC(J,1)=DELC(J,1)
859 DLOC(J,2)=0
860 DLOC(J,3)=0
861 510 CONTINUE
862 DO 511 J=1,NMOD
863 DO 512 K=1,3
864 CLCAD(J,K)=0
865 512 CONTINUE
866 511 CONTINUE
867 GO TO 1000
868 C
869 2 DO 520 J=1,NMOD
870 DO 521 K=1,3
871 CLCAD(J,K)=0
872 521 CONTINUE
873 520 CONTINUE
874 DO 522 J=1,NEL
875 DO 523 K=1,3
876 DLOC(J,K)=0
877 523 CONTINUE
878 522 CONTINUE
879 CALL PRETEN(CABLE,CLOAD,X,CABLE,IEL,WEL,NMOD,NOWPRO,
880 * NPS,PSEGN,ELONG,PM,FK,E,FINCAD)
881 IF (IFRET.EQ.3) ICOUNT=1
882 IF (IFRET.EQ.1) INCLUD=1
883 NOWPRO=1
884 GO TO 1000
885 C
886 3 DO 530 J=1,NEL
887 DLOC(J,1)=DELC(J,2)
888 DLOC(J,2)=0
889 DLOC(J,3)=0
890 530 CONTINUE
891 DO 531 J=1,NMOD
892 DO 532 K=1,3
893 CLCAD(J,K)=0
894 532 CONTINUE
895 531 CONTINUE
896 GO TO 1000
897 C
898 C
899 4 CALL SUPDIS(IGMAT,IATYPE,MLOCA,GAMAG,GAMAD,ICSTR,

```

```

900
901
902
903
904
905
906
907
908
909
910
911
912
913
914
915
916
917
918
919
920
921
922
923
924
925
926
927
928
929
930
931
932
933
934
935
936
937
938
939
940
941
942
943
944
945
946
947
948
949
950
951
952
953
954
955
956
957
958
959

```



```

*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR,
*      IEL, X, ALOAD, B, APLOAD, REAC, DIM, STEEL, AREA, DELC,
*      SDISP, LOCA, PREDIS, YCABLE, CABLE, IPRET,
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK,
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM,
*      STRE, CNF, ICHECK, NSUP3, DISPL, FORCE, STRIC,
*      ITER, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, RELIST, SREAL,
*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICOMP, ELONG, LC, T)
IF (FINISH.GT.0) GO TO 9000
GO TO 500
C      LIVE LOAD
5 DO 550 J=1, NEL
DO 551 K=1, 3
DLCAD(J,K)=APLOAD(J,K)*LIVLO
551 CONTINUE
550 CONTINUE
DO 552 J=1, NNOD
DO 553 K=1, 3
CLOAD(J,K)=ALOAD(J,K)*LIVLO
553 CONTINUE
552 CONTINUE
IF (LOCA(LC,3).LT.1000) GO TO 1000
C      DISPLACEMENT INCREMENT METHOD
C
C      CALL DINLL (IGMAT, IATYPE, NLOCA, GAMAG, GAMAD, ICSTR,
*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR,
*      IEL, X, ALOAD, B, APLOAD, REAC, DIM, STEEL, AREA, DELO, CLOAD,
*      DLOAD, SDISP, LOCA, PREDIS, YCABLE, CABLE, IPRET,
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK,
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM,
*      STRE, CNF, ICHECK, NSUP3, DISP, DCM, DCL, FORCE, STRIC,
*      AK12, KVAR, PI, DO, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, DBIVLL,
*      NODR, AK22, ALP11, ITER, RELIST, SREAL,
*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICOMP, ELONG, LC, T)
IF (FINISH.GT.0) GO TO 9000
GO TO 500
C      LOAD INCREMENT METHOD
C
1000 CALL LIN (IGMAT, IATYPE, NLOCA, GAMAG, GAMAD, ICSTR,
*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR,
*      IEL, X, ALOAD, APLOAD, REAC, DIM, STEEL, AREA, DELC, CLOAD,
*      DLOAD, SDISP, B, LOCA, PREDIS, YCABLE, CABLE, IPRET,
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK,
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM,
*      STRE, CNF, ICHECK, NSUP3, DISP, DCM, DCL, FORCE, STRIC,
*      ITER, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, RELIST, SREAL,
*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICOMP, ELONG, LC, T)
IF (FINISH.GT.0) GO TO 9000
GO TO 500
C      TEMPERATURE
C
6 CALL TEMPER (IT1, IT2, IT3, IGMAT, IATYPE, NLOCA, GAMAG, GAMAD, ICSTR,
*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR,
*      IEL, X, ALOAD, APLOAD, REAC, DIM, STEEL, AREA, DELC, CLOAD,
*      DLOAD, SDISP, B, LOCA, PREDIS, YCABLE, CABLE, IPRET,
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK,
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM,
*      STRE, CNF, ICHECK, NSUP3, DISP, DCM, DCL, FORCE, STRIC,
*      ITER, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, RELIST, SREAL,

```

```

*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICCMF, ELCNG, LC, T) 1020
IF (FINISH.GT.0) GO TO 9000 1021
GO TO 500 1022
C      CREEP, SHRINKAGE AND RELAXATION 1023
C 1024
7 CALL TIMEP (IGMAT, IATYPE, NLOCA, GAMAG, GAMAD, ICSTR, 1025
*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR, 1026
*      IEL, X, ALOAD, APLOAD, REAC, DIM, STEEL, AREA, DELC, CLOAD, 1027
*      DLOAD, SDISP, B, LOCA, PREDIS, YCABLE, CABLE, IPRET, 1028
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK, 1029
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM, 1030
*      STRE, CNF, ICHECK, NSUP3, DISP, DCM, DCL, FORCE, STRIC, 1031
*      ITER, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, RELIST, SREAL, 1032
*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICCMF, ELONG, LC, 1033
*T, IEL) 1034
IF (FINISH.GT.0) GO TO 9000 1035
GO TO 500 1036
500 CONTINUE 1037
9000 IF (NCHEL.GT.0) THEN 1038
CALL PLIST (NCHEL, ICHECK, ITNST, DCM, FINISH, NCH3, ITER) 1039
END IF 1040
CALL RICLIST (RELIST, ITNST, NDISP, NNOD, PREDIS, NSUP, NVAR) 1041
RETURN 1042
END 1043
C***** 1044
SUBROUTINE SUPDIS (IGMAT, IATYPE, NLOCA, GAMAG, GAMAD, ICSTR, 1045
*      NNOD, NSUP, NEL, NODE3, NDISP, NBAND, E, BC, NVAR, IVAR, 1046
*      IEL, X, ALOAD, B, APLOAD, REAC, DIM, STEEL, AREA, DELO, 1047
*      SDISP, LOCA, PREDIS, YCABLE, CABLE, IPRET, 1048
*      NPS, PSEGM, FM, FK, ICONST, STA, STRB, STRST, CRACK, 1049
*      NGL, NL, NS1, NS2, NS3, NS4, EALL, Y, ICRACK, IALPHA, IELD, EPERM, 1050
*      STRE, CNF, ICHECK, NSUP3, DISP, DCM, DCL, FORCE, STRIC, 1051
*      ITER, FINCAB, CABSSST, GTP, ST, NCHEL, NCH3, ISSC, RELIST, SREAL, 1052
*FINISH, ITNST, INCLUD, NOWPRO, ICOUNT, IAFTEH, NTITER, ICOMP, ELONG, LC, T) 1053
C***** 1054
IMPLICIT REAL*8 (A-H, O-Z) 1055
DIMENSION E(4,6), NVAR(NNOD,3), IEL(NEL,3), X(NNOD,2), ALOAD(NNOD,3), 1056
B(1), APLOAD(NEL,3), REAC(NSUP,3), DIM(NEL,8), IVAR(NNOD,3) 1057
STEEL(NEL,6), AREA(NEL,6), DELO(NEL,2), ST(NODE3,NBAND) 1058
SCISP(NNOD,3), DISP(NNOD,3), STRIC(NEL,NL) 1059
LOCA(NLOCA,8), PREDIS(NSUP,2), YCABLE(NNOD), CABLE(NEL,7) 1060
PSEGM(10,5), ELONG(10,2), STA(NEL,NS1), STRB(NEL,8), 1061
FINCAB(NEL,3), CABSSST(NEL), STNGT(NEL,NS2), CRACK(NEL,8), Y(NL,3), 1062
GTP(NEL), ICRACK(NEL,NL), IALPHA(NEL,NL), EALL(NEL,NS3), 1063
EPERM(NEL,NL), STRE(NEL,NS3), IELD(NEL,NS4), CNF(NODE3,3), 1064
ICHECK(NCHEL), DCM(100,NCH3), DCL(NNOD,3), 1065
FORCE(NEL,3), RELIST(100,10), T(6) 1066
C 1067
MODIFY=0 1068
CALL ACDDJ (NNOD, NSUP, NVAR, IVAR, NDISP, PREDIS, MODIFY) 1069
C 1070
DO 10 J=1, NODE3 1071
CNF(J,3)=0 1072
10 CONTINUE 1073
C 1074
NSTEPS=LCCA(LC,3) 1075
DO 2010 J=1, NSUP 1076
PREDIS(J,2)=PREDIS(J,2)/NSTEPS 1077
2010 CONTINUE 1078

```

```

C
DO 3000 ISTEP=1,NSTEPS
ITNST=ITNST+1
ND=0
DO 20 J=1,NMOD
DO 30 K=1,J
ND=ND+1
B(ND)=0
DISP(J,K)=0
30 CONTINUE
20 CONTINUE
CALL NWARD(NEL,DIM,ICOMP,IATYP2,IGMAT,IEL,NGL,NL,STRE,ICRACK,
* CALL,STEEL,NS3,Y,AREA,E,FINISH)
IF (FINISH.EQ.7) GO TO 5000
CALL ADSTIF(NMOD,NDISP,NBAND,NEL,IEL,NVAR,X,ST,BC,DIM,AREA,
* YCABLE,CABLE,INCLUD,NSUP3,NSUP,PREDIS)
CALL NEWSOL(ST,B,NDISP,NBAND,NVAR,NMOD,NSUP,PREDIS)
CALL SOLVE(NDISP,NBAND,ST,B)
CALL DISPLA(B,NDISP,NVAR,NMOD,DISP,SDISP)
CALL STRAIN(B,DIM,NEL,STEEL,IEL,NVAR,IGMAT,IATYP2,IPRET,NMOD,
* X,ICOMP,STA,STRE,STST,NGL,NDL,NL,NS1,NS2,Y,CTP,NOWPRO)
DO 5555 ME=1,NEL
DO 5556 L=1,NL
STELC(ME,L)=STELC(ME,L)+STST(ME,L)
5556 CONTINUE
5555 CONTINUE
IF (IGMAT.EQ.1.AND.INCLUD.EQ.1) THEN
NWSTR=1
CALL MODCAB(CABLE,YCABLE,B,NEL,IEL,NVAR,X,NMOD,E,CABSST,
* NWSTR,NODE3)
END IF
CALL ECLBMM(CNF,NEL,FORCE,STST,NS2,EALL,NS3,IPRET,ICSTN,
* X,NL,NGL,DIM,ICOMP,IATYP2,IGMAT,IEL,ICRACK,
* STRE,AREA,STEEL,ISTOP,DCL,B,X,NMOD,STELC,LC,LOCA,NLOCA,
* NVAR,E,NDL,IEL,NS4,EPEM,STA,NS1,NDISP,NBAND,
* ST,DISP,SDISP,STRE,ITER,NTITER,ISSC,NODE3,ISTEP,FINISH,
* INCLUD,CABLE,FINCAB,YCABLE,CABSST,GTP,NOWPRO,NSTEPS,T,SREAL,BC)
IF (FINISH.GT.0) GO TO 5000
IF (IGMAT.EQ.0) THEN
IF (ICOMP.EQ.0) GO TO 1235
END IF
ERG=E(3,3)
IF (IGMAT.EQ.0) ERG=E(3,6)
END IF
CALL CRACKS(STRE,DIM,NEL,IGMAT,CBACK,ERG,ERD,ICOMP,X,IEL,NMOD,
* ICRACK,NGL,NL)
CALL ACRACK(NEL,AREA,STA,NS1,NS3,EALL,DIM,IATYP2,IGMAT,NGL,NL,
* IEL,ICOMP,ICRACK,IALPHA,ERG,ERD,Y,ICSTN)
1235 CONTINUE
CALL REACT(NSUP,NMOD,NVAR,REAC,PREDIS,ITNST,BELIST,DCL)
IF (ISTEP.LT.NSTEPS) THEN
IF (LOCA(LC,4).EQ.0) GO TO 2900
END IF
5000 CALL OUTPUT(NEL,ICOMP,AREA,NMOD,NVAR,FORCE,SDISP,IGMAT,CABLE,
* NOWPRO,FM,FK,NPS,PSEGN,ELCNG,ICHECK,NCHL,IATYP2,DIM,
* NGL,NL,STA,NS1,STRE,NS3,EALL,STRE,ERG,ERD,CRACK,
* ICRACK,IALPHA,IELD,NS4,IEL,Y,NSUP,NSUP3,REAC,PREDIS,
* DISP,ISTEP,LC,NSTEPS,ITER,NTITER)
2900 IF (NCHL.GT.0) THEN
STIP=ISTEP

```

```

1079 STEPS=NSTEPS
1080 SALPHA=STEP/STEPS
1081 TIME=T(1)
1082 CALL HOCURV(DCM,NCH3,NCHL,NEL,FCBCE,SDISP,NMOD,STRE,
1083 ITNST,ICHECK,DIM,IGMAT,IEL,ITER,SALPHA,TIME)
1084 END IF
1085 IF (FINISH.GT.0) GO TO 6000
1086 3000 CONTINUE
1087 MCIFY=1
1088 CALL MODCD(NMOD,NSUP,NVAR,IVAR,NDISP,PREDIS,MODIFY)
1089 DO 2500 J=1,NSUP
1090 PREDIS(J,2)=NSTEPS*PREDIS(J,2)
1091 2500 CONTINUE
1092 6000 RETURN
1093 END
1094 C*****
1095 SUBROUTINE DIMIL(IGMAT,IATYP2,NLOCA,GAMAG,GAMAD,ICSTN,
1096 * NMOD,NSUP,NEL,NODE3,NDISP,NBAND,Z,BC,NVAR,IVAR,
1097 * IEL,X,ALOAD,B,APLOAD,REAC,DIM,STEEL,AREA,DELC,CLCAD,
1098 * DLOAD,SDISP,LOCA,PREDIS,YCABLE,CABLE,IPRET,
1099 * NPS,PSEGN,FM,FK,ICONST,STA,STRE,STST,CRACK,
1100 * NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPEM,
1101 * STRE,CNF,ICHECK,NSUP3,DISP,DCM,DCL,FORCE,STELC,
1102 * AK12,KVAR,P1,DU,FINCAB,CABSST,GTP,ST,NCHL,NCH3,ISSC,DRIVL,
1103 * NOCH,AK22,ALPLI,ITER,BELIST,SREAL,
1104 * FINISH,ITNST,INCLUD,NOWPRO,ICOUNT,IAPTER,NTITER,ICOMP,ELONG,LC,T)
1105 C*****
1106 IMPLICIT REAL*8(A-H,G-Z)
1107 DIMENSION E(4,6),NVAR(NMOD,3),IEL(NEL,3),X(NMOD,2),ALOAD(NMOD,3),
1108 * B(1),AFLOAD(NEL,3),REAC(NSUP,3),DIM(NEL,9),IVAR(NMOD,3),
1109 * STEEL(NEL,6),AREA(NEL,6),DELC(NEL,2),ST(NODE3,NBAND),
1110 * CLCAD(NMOD,3),DLOAD(NEL,3),SDISP(NMOD,3),DISP(NMOD,3),
1111 * LOCA(NLOCA,8),PREDIS(NSUP,2),YCABLE(NMOD),CABLE(NEL,7),
1112 * BELIST(300,10),PSEGN(10,5),ELONG(10,2),STA(NEL,NS1),STRE(NEL,8),
1113 * FINCAB(NEL,3),CABSST(NEL),STST(NEL,NS2),CRACK(NEL,8),Y(NL,3),
1114 * GTP(NEL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3),
1115 * EPEM(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CNF(NODE3,3),
1116 * ICHECK(NCHL),DCM(300,NCH3),DCL(NMOD,3),STELC(NEL,NL),
1117 * FORCE(NEL,3),AK12(1),AK1(1),DU(1),KVAR(NMOD,3),T(6)
1118 ISTEP=0
1119 NEXT=C
1120 ALPHA=J
1121 SALPHA=0
1122 SALCLO=0
1123 C
1124 OBTAIN NEW GLOBAL DISPLACEMENTS ( KVAR )
1125 ANDISP=0
1126 IVAR(NMOD,2)=1
1127 DO 7011 J=1,NMOD
1128 DO 7009 K=1,3
1129 IF (IVAR(J,K).EQ.0) THEN
1130 NNCISP=NDISP+1
1131 KVAR(J,K)=NDISP
1132 ELSE
1133 KVAR(J,K)=0
1134 END IF
1135 7009 CONTINUE
1136 7011 CONTINUE
1137 C
1138 CALL ELOAD(NMOD,NEL,IEL,DLOAD,CLCAD,X,P1,KVAR)

```



```

C
C      STORE THE EXTERNAL LOAD VECTOR
C
ND=0
DO 7003 J=1,NMOD
DO 7004 K=1,3
IF (NVAR(J,K).NE.0) THEN
ND=ND+1
CNF(ND,3)=CLOAD(J,K)
END IF
7004 CONTINUE
7003 CONTINUE
C
C      BEGIN NEW STEP
C
7005 ITSP=0
NSTEP=1
ISTEP=ISTEP+1
ITNS1=ITNS1+1
DENOM=0
P2=CLOAD(NCDB,2)
ND=0
DO 7001 J=1,NMOD
DO 7002 K=1,3
DISP(J,K)=0
IF (KVAR(J,K).NE.0) THEN
ND=ND+1
P1(ND)=CLOAD(J,K)
END IF
7002 CONTINUE
7001 CONTINUE
CALL NWAREA(NEL,DIM,ICOMP,IATYPE,IGMAT,IEL,NGL,NL,STRE,
* ICRACK,EALL,STEEL,NS1,Y,AREA,E,FINISH)
IF (FINISH.EQ.7) GO TO 7099
CALL ADSTIF(NMOD,NDISP,NBAND,NEL,IEL,NVAR,X,ST,BC,DIM,
* AREA,YCABLE,CABLE,INCLUD,MSUF,NSUP,
* FBEDIS)
CALL SPLIT(NBAND,NVAR,NODR,NDISP,ST,NMOD,AK12,AK22)
CALL NWSTIF(NMOD,NNDISP,NBAND,NEL,IEL,KVAR,X,ST,BC,DIM,
* AREA,YCABLE,CABLE,INCLUD,NODR)
CALL SOLVE(NNDISP,NBAND,ST,P1)
DO 7010 J=1,NNDISP
DU(J)=-AK12(J)*DRIVLL
7010 CONTINUE
C
C      ITERATIONS LOOP
C
7015 CONTINUE
CALL RESOLV(NNDISP,NBAND,ST,DU)
CALL FRACTN(NWSTP,AK12,DU,P2,P1,NNDISP,DENOM,ALPHA,SALPHA,
* AK22,DRIVLL)
JUMP=NVAR(NODR,2)
DO 7020 J=1,NDISP
IF (J.LT.JUMP) THEN
SMALL=DSQRT(DABS(ALPHA))*DSQRT(DABS(P1(J)))
IF (SMALL.LT.1.E-38) THEN
B(J)=DU(J)
ELSE
B(J)=ALPHA*P1(J)+DU(J)
END IF
END IF
IF (J.EQ.JUMP) B(J)=DRIVLL*NWSTP
IF (J.GT.JUMP) THEN

```

```

1198 SMALL=DSQRT(DABS(ALPHA))*DSQRT(DABS(P1(J-1)))
1199 IF (SMALL.LT.1.E-38) THEN
1200 B(J)=DU(J-1)
1201 ELSE
1202 B(J)=ALPHA*P1(J-1)+DU(J-1)
1203 END IF
1204 END IF
1205 7020 CONTINUE
1206 CALL DISPLA(B,NDISP,NVAR,NMOD,DISP,SDISP)
1207 CALL STRAIN(B,DIM,NEL,STEEL,IEL,NVAR,IGMAT,IATYPE,IPRET,NMOD,
1208 * X,ICOMP,STA,STRB,STRT,NGL,NDL,NL,NS1,NS2,Y,GTP,NOWPRO)
1209 DO 5555 NE=1,NEL
1210 DO 5556 L=1,NL
1211 STRLC(NE,L)=STRLC(NE,L)+STRT(NE,L)
1212 5556 CONTINUE
1213 5555 CONTINUE
1214 IF (IGMAT.EQ.1) THEN
1215 IF (IAFTER.EQ.1) THEN
1216 CALL MDCAB(CABLE,YCABLE,B,NEL,IEL,NVAR,X,NMOD,E,CABSST,NWSTP,
1217 * NODE3)
1218 END IF
1219 END IF
1220 C
1221 C      EXTERNAL LOAD LINEAR ADJUST
1222 C
DO 7021 J=1,NODE3
CNF(J,2)=CNF(J,1)+SALPHA*CNF(J,3)
7021 CONTINUE
C
CALL STRESS(B,STRE,NEL,NS3,IEL,NS4,EPERM,NL,STA,STRT,ICSTR,
* SREAL,NS1,NS2,EALL,IGMAT,NGL,STEEL,ICOMP,ICRACK,IEL,ISSC,
* FINISH,NWSTP,T)
CALL FGRSCT(NEL,FORCE,NS1,EALL,NS1,Y,NL,NGL,DIM,ICOMP,
* IATYPE,IGMAT,IEL,ICRACK,STRE,AREA,STEEL,STA,
* INCLUD,FINCAB,CABLE,YCABLE,NMOD,GTP,NOWPRO)
IF (FINISH.GT.0) GO TO 7050
CALL CHECKQ(FORCE,CNF,NEL,ISTOP,IOL,DCI,DIM,B,AREA,
* X,NMOD,NVAR,NODE3,NDISP,FINCAB,INCLUD,BC)
IF (ISTOP.EQ.1) THEN
NEXST=0
GO TO 7050
END IF
DO 7040 J=1,NDISP
IF (J.LT.JUMP) DU(J)=B(J)
IF (J.EQ.JUMP) P2=B(J)
IF (J.GT.JUMP) DU(J-1)=B(J)
7040 CONTINUE
NSTEP=0
ITEL=ITEL+1
NTITER=NTITER+1
IF (ITEL.GE.500) FINISH=1
C
C      INCREASE STEP
C
IF (ITER.GE.50) THEN
NEXST=NEXST+1
IF (NEXST.GE.6) THEN
FINISH=6
GO TO 7050
ELSE
DRIVLL=1.2*DRIVLL
GO TO 7005

```

```

C      END IF
C      ENCL IF
C
C      GO TO 7015
C
7050 IF (IGNAT.EQ.0) THEN
      IF (ICOMP.EQ.0) GO TO 1236
      END IF
      ERG=E(3,3)
      IF (IGNAT.EQ.0) ERG=E(3,6)
      ERG=E(4,3)
      CALL CRACKS(STRB,DIN,NEL,IGNAT,CRACK,ERG,ERD,ICOMP,X,IEL,MNOD,
      *          ICRACK,NGL,NL)
      CALL ACRACK(NEL,AREA,STA,NS1,NS3,EALL,DIM,IATYPE,IGNAT,NGL,NL,
      *          IEL,ICOMP,ICRACK,IALPHA,ERG,ERD,Y,ICSTR)
1236 CONTINUE
      DO 7051 J=1,MNOD
      DO 7052 K=1,3
      JA=NVAR(J,K)
      IF (JA.NE.0) D(JA)=DISP(J,K)
7052 CONTINUE
7051 CALL REACT(NSUP,MNOD,NVAR,REAC,PREDIS,ITNST,RELIST,DCL)
      NSTEPS=LOCA(LC,3)
      IF (SALPHA.GE.ALPL) FINISH=2
C
C      IF (MNSTP.EQ.0) THEN
C      IF (SALCLD.GT.0) THEN
C      IF (SALPHA/SALOLD.GT.1) THEN
C      IF (SALPHA/SALOLD.LT.1.0001) FINISH=5
C      END IF
C      END IF
C      END IF
C      SALCLD=SALPHA
C      IF (FINISH.GT.0) GO TO 7099
C      IF (LOCA(LC,4).EQ.0) GO TO 7100
7099 CALL OUTPUT(NEL,ICOMP,AREA,MNOD,NVAR,FORCE,SDISP,IGNAT,
      *          CABLE,NOMP,PRO,FM,FK,NFS,PSEGN,ELONG,ICHECK,NCHL,
      *          IATYPE,DIM,NGL,NL,STA,NS1,STRE,NS3,EALL,STRB,ERG,
      *          ERD,CRACK,ICRACK,IALPHA,IELD,NS4,IEL,Y,NSUP,NSUP3,
      *          REAC,PREDIS,DISP,ISTEP,LC,NSTEPS,ITER,MTITER)
7100 IF (NCHL.GT.0) THEN
      TIME=T(1)
      CALL MOCUBV(DCM,NCH3,NCH2L,NEL,FORCE,SDISP,MNOD,STRB,ITNST,
      *          ICHECK,DIM,IGNAT,IEL,ITER,SALPHA,TIME)
      END IF
      IF (FINISH.EQ.0) GO TO 7005
C
C      UPDATE THE EXTERNAL LOAD VECTOR
      DO 1000 K=1,NODE3
      CNF(K,1)=CNF(K,1)+CNF(K,3)*SALPHA
1000 CONTINUE
C
C      RETURN
C      ENCL
C*****
      SUBROUTINE LIN(IGNAT,IATYPE,NLCCA,GAMAG,GAMAD,ICSTR,
      *          MNOD,NSUP,NEL,NODE3,NDISP,NBAND,Z,BC,NVAR,IVAR,
      *          IEL,X,ALOAD,APLOAD,REAC,DIM,STEEL,AREA,DELC,CLOAD,
      *          DLOAD,SDISP,B,LCCA,PREDIS,YCABLE,CABLE,IPRET,

```

```

1318 *          MPS,PSEGN,FM,FK,ICONST,STA,STRB,STNST,CRACK, 1377
1319 *          NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPERN, 1378
1320 *          STRE,CNF,ICHECK,NSUP3,DISP,DCM,DCL,FORCE,STRLC, 1379
1321 *          ITER,FINCAD,CABST,STP,ST,NCHL,NCH3,ISSC,RELIST,SREAL, 1380
1322 *          FINISH,ITNST,INCLUD,NOMP,PRO,ICOUNT,IAFTER,MTITER,ICOMP,ELONG,LC,T) 1381
1323 C***** 1382
1324 IMPLICIT REAL*8(A-H,O-Z) 1383
1325 DIMENSION L(4,6),NVAR(MNOD,3),IEL(NEL,3),X(MNOD,2),ALOAD(MNOD,3), 1384
1326 *          B(1),AFLOAD(NEL,3),REAC(NSUP,3),DIM(NEL,8),IVAR(MNOD,3), 1385
1327 *          STEEL(NEL,8),AREA(NEL,8),DELO(NEL,2),ST(NODE3,NBAND) 1386
1328 *          ,CLOAD(MNOD,3),CLOAD(NEL,3),SDISP(MNOD,3),DISP(MNOD,3) 1387
1329 *          ,LOCA(MNOD,8),PREDIS(NSUP,2),YCABLE(MNOD),CABLE(NEL,7) 1388
1330 *          ,PSEGN(10,5),ELONG(10,2),STA(NEL,NS1),STRB(NEL,8), 1389
1331 *          FINCAD(NEL,3),CABST(NEL),STNST(NEL,NS2),CRACK(NEL,8),Y(NL,3), 1390
1332 *          GTP(NEL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3), 1391
1333 *          EPERN(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CNF(NODE3,3), 1392
1334 *          ICHECK(NCHL),DCM(100,NCH3),DCL(MNOD,1), 1393
1335 *          FORCE(NEL,3),RELIST(100,10),T(6),STRLC(NEL,NL) 1394
1336 NSTEPS=LOCA(LC,3) 1395
C 1396
C      CALL ELOAD(MNOD,NEL,IEL,DLOAD,CLOAD,X,B,NVAR) 1397
C 1398
C      STORE THE EXTERNAL LOAD VECTOR 1399
C 1400
C      LVEC=1 1401
C      IF (NCOMP.EQ.1.AND.IPRET.EQ.1) LVEC=0 1402
C      ND=0 1403
C      DO 7003 J=1,MNOD 1404
C      DO 7004 K=1,3 1405
C      IF (NVAR(J,K).NE.0) THEN 1406
C      ND=ND+1 1407
C      CNF(ND,3)=CICAD(J,K)*LVEC 1408
C      END IF 1409
7004 CONTINUE 1410
7003 CONTINUE 1411
C 1412
C      DO 5000 ISTEP=1,NSTEPS 1413
C      ITNST=ITNST+1 1414
C      ND=0 1415
C      DO 5010 L=1,MNOD 1416
C      DO 5020 M=1,3 1417
C      DISP(L,M)=0 1418
C      IF (NVAR(L,M).NE.0) THEN 1419
C      ND=ND+1 1420
C      B(ND)=CLOAD(L,M)/NSTEPS 1421
C      END IF 1422
5020 CONTINUE 1423
5010 CONTINUE 1424
C      CALL ANALIS(IGNAT,IATYPE,NLOCA,GAMAG,GAMAD,ISTEP,NSTEPS,ICSTR, 1425
      *          MNOD,NSUP,NEL,NODE3,NDISP,NBAND,Z,BC,NVAR,IVAR, 1426
      *          IEL,X,ALOAD,APLOAD,REAC,DIM,STEEL,AREA,DELC,CLOAD, 1427
      *          DLOAD,DISP,B,LCCA,PREDIS,YCABLE,CABLE,IPRET, 1428
      *          MPS,PSEGN,FM,FK,ICONST,STA,STRB,STNST,CRACK, 1429
      *          NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPERN, 1430
      *          STRE,CNF,ICHECK,NSUP3,DISP,DCM,DCL,FORCE,STRLC, 1431
      *          ITER,FINCAD,CABST,STP,ST,NCHL,NCH3,ISSC,RELIST,SREAL, 1432
      *          FINISH,ITNST,INCLUD,NOMP,PRO,ICOUNT,IAFTER,MTITER,ICOMP,ELONG,LC,T) 1433
      IF (FINISH.GT.0) GO TO 5001 1434
5000 CONTINUE 1435
C 1436

```



```

C          UPDATE THE EXTERNAL LOAD VECTOR
C
      IF (NCVPRO.NZ.1) THEN
      DO 6000 J=1,MODE3
      CNF(J,1)=CNF(J,1)+CNF(J,3)
6000    CONTINUE
      END IF
C
      SC01 RETURN
      END
C*****
      SUBROUTINE ANALIS(IGMAT,IATYPE,NLOCA,GAMAG,GAMAD,ISTEP,NSTEPS,
      * ICSTR,NMOD,NSUP,NEL,MODE3,NDISP,NBAND,E,BC,NVAR,IVAR,
      * IEL,X,ALOAD,APLOAD,REAC,CIM,STEEL,AREA,DELO,CLOAD,
      * DLOAD,SDISP,B,LCCA,PREDIS,YCABLE,CABLE,IPRET,
      * NPS,PSEGN,FM,FK,ICONST,STA,STRB,STRT,CRACK,
      * NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPERM,
      * STRE,CNF,ICHECK,NSUP3,DISP,DCH,DCL,FORCE,STRIC,
      * ITER,PINCAB,CABSST,GTP,ST,NCHNL,NCH3,ISSC,BELIST,SREAL,
      * FINISH,ITNST,INCLUD,NOWPRO,ICOUNT,IAFTER,NTITER,ICOMP,ELONG,LC,T)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION E(4,6),NVAR(NMOD,3),IEL(NEL,3),X(NMOD,2),ALOAD(NMOD,3),
      * B(1),APLOAD(NEL,3),REAC(NSUP,3),CIM(NEL,6),IVAR(NMOD,3),
      * STEEL(NEL,6),AREA(NEL,6),DELO(NEL,2),ST(NODE3,NBAND),
      * CLOAD(NMOD,3),DLOAD(NEL,3),SDISP(NMOD,3),DISP(NMOD,3),
      * LOCA(NLOCA,4),PREDIS(NSUP,2),YCABLE(NMOD),CABLE(NEL,7),
      * PSEGN(10,5),ELONG(10,2),STA(NEL,NS1),STRB(NEL,8),
      * FINCAB(NEL,3),CABSST(NEL),STRT(NEL,NS2),CRACK(NEL,8),Y(NL,3),
      * GTP(NEL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3),
      * EPERM(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CNF(NODE3,3),
      * ICHECK(NCHNL),DCH(300,NCH3),DCL(NMOD,3),
      * FORCE(NEL,3),BELIST(300,10),T(6),STLCL(NEL,NL)
      CALL NWAREA(NEL,DIM,ICOMP,IATYPE,IGMAT,IEL,NGL,NL,STRE,ICRACK,
      * IALL,STEEL,NS3,Y,AREA,E,FINISH)
      IF (FINISH.EQ.7) GO TO 4800
      CALL AESTIF(NMOD,NDISP,NBAND,NEL,IEL,NVAR,X,ST,BC,DIM,AREA,
      * YCABLE,CABLE,INCLUD,NSUP3,NSUP,PREDIS)
      CALL SCLYE(NDISP,NBAND,ST,E)
      CALL DISPLA(B,NDISP,NVAR,NMOD,DISP,SDISP)
      CALL STRAIN(B,DIM,NEL,STEEL,IEL,NVAR,IGMAT,IATYPE,IPRET,NMOD,
      * X,ICOMP,STA,STRB,STRT,NGL,NGL,NL,NS1,NS2,Y,GTP,NOWPRO)
      IF (LOCA(LC,1).NE.7) THEN
      DO 5555 NE=1,NEL
      DO 5556 L=1,NL
      STLCL(NL,L)=STLCL(NL,L)+STRT(NL,L)
5556    CONTINUE
5555    CONTINUE
      END IF
      IF (IGMAT.EQ.1) THEN
      IF (INCLUD.EQ.1) THEN
      NSTEP=1
      CALL NCDCAB(CABLE,YCABLE,B,NEL,IEL,NVAR,X,NMOD,E,CABSST,
      * NSTEP,MODE3)
      IF (NCVPRO.EQ.1.AND.IPRET.EQ.1) THEN
      DO 6000 JK=1,NEL
      FINCAB(JK,1)=CABLE(JK,3)
6000    CONTINUE
      END IF

```



```

70 CONTINUE
C
200 IF (INCLUD.EQ.1.AND.ITYPE.EQ.0) THEN
  M1=IEL(NE,1)
  M2=IEL(NE,2)
  X=(YCABLE(M1)+YCABLE(M2))/2
  STRAIN=-AS*(IT3-(IT2-IT3)*X/TH)
  CAESST(NE)=-STRAIN
  STRESS=CABLE(NE,7)*STRAIN
  CABLE(NE,5)=CABLE(NE,5)+STRESS
  ENF IF
50 CONTINUE
RETURN
END
C*****
SUERCUTIME TIMEF(IGMAT,IATYPE,MLCCA,GAMAG,GAMAD,ICSTR,
  MNOD,NSUP,NEL,NODE3,NDISP,NBAND,E,BC,NVAR,IVAR,
  IEL,X,ALOAD,APLOAD,REAC,DIM,STEEL,AREA,DELC,CLOAD,
  DLOAD,SDISP,B,LCCA,PREDIS,YCABLE,CABLE,IPRET,
  MPS,PSEGM,PK,ICONST,STA,STRB,STRT,CRACK,
  NGL,NL,NS1,NS2,NS3,NS4,EALL,Y,ICRACK,IALPHA,IELD,EPRM,
  STRE,CNF,ICHECK,NSUP3,DISP,DCM,DCL,FORCE,STREL,STRLC,
  ITER,PINCAB,CABSST,GTP,SI,NCHL,NCH3,ISSC,RELIST,SREAL,FINISH,
  ITNST,INCLUD,NOWPRO,ICOUNT,IAPTEB,NTITER,ICOMP,ELONG,LC,T,IST)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION E(4,6),NVAR(NNCD,3),IEL(NEL,3),X(MNOD,2),ALOAD(MNOD,3),
  B(1),AELoad(NEL,3),REAC(NSUP,3),DIM(NEL,8),IVAR(MNOD,3),
  STEEL(NEL,6),AREA(NEL,8),DELO(NEL,2),ST(MODE3,NBAND),
  CLOAD(MNOD,3),DLOAD(NEL,3),SDISP(MNOD,3),DISF(MNOD,3),
  LOCA(MLOCA,8),PREDIS(NSUP,4),YCABLE(MNOD),CABLE(NEL,7),
  PSEGM(10,5),ELONG(10,2),STA(NEL,NS1),STRB(NEL,8),
  PINCAB(NEL,3),CABSST(NEL),STNST(NEL,NS2),CRACK(NEL,8),Y(NL,3),
  GTP(NEL),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3),
  EPRM(NEL,NL),STRE(NEL,NS3),IELD(NEL,NS4),CNF(MODE3,3),
  ICHECK(NCHL),DCM(300,NCH3),DCL(MNOD,3),
  FORCE(NEL,3),RELIST(300,10),T(6),STREL(NEL,NL),STRLC(NEL,NL)
EL=LCCA(LC,5)
NSTEP=LCCA(LC,3)
DO 10 I=1,MODE3
  CNF(I,3)=0
10 CONTINUE
C
STEP CALCULATION
PS=1./24
DT=LCCA(LC,7)-LCCA(LC,6)
RT=(DT/PS)**(1./(NSTEP-1))
C
INCREMENT STEPS
DO 20 ISTEP=1,NSTEP
  ITNST=ITNST+1
  DO 30 J=1,NNCD
    DO 40 K=1,5
      DISP(J,K)=0
    40 CONTINUE
  30 CONTINUE
C
CALCULATE TIMES
IF (ISTEP.EQ.1) THEN
  TSI=LCCA(LC,6)
  TSF=TSI*PS
  ENF IF

```

```

1674 IF (ISTEP.EQ.2) THEN
1675 TSI=LCCA(LC,6)*PS
1676 TSF=LCCA(LC,6)*PS*BT
1677 ENF IF
1678 IF (ISTEP.GE.3) THEN
1679 TSI=LCCA(LC,6)*PS*BT** (ISTEP-2)
1680 TSF=LCCA(LC,6)*PS*BT** (ISTEP-1)
1681 ENF IF
1682 C
1683 T(1)=TSF
1684 C
1685 DO 45 NE=1,NEL
1686 CAESST(NE)=0
1687 DO 46 K=1,NS2
1688 STST(NE,K)=0
1689 46 CONTINUE
1690 45 CONTINUE
1691 C
1692 IF (EL.EQ.1.OR.EL.EQ.4) THEN
1693 CALL CREEP(TSI,TSF,T,IGMAT,ICOMP,NEL,NGL,NL,IEL,STST,
  + NS2,STREL,STRLC)
1694 ENF IF
1695 IF (EL.EQ.2.OR.EL.EQ.4) THEN
1696 CALL SHRINK(TSI,TSF,T,IGMAT,ICOMP,NEL,NGL,NL,IEL,STST,NS2)
1697 ENF IF
1698 IF (ISTEP.GT.1) THEN
1699 IF (EL.GE.3.AND.INCLUD.EQ.1) THEN
1700 CALL RELAX(IST,TSI,TSF,T,E,IEL,NEL,CABLE,CABSST,PINCAB)
1701 ENF IF
1702 ENF IF
1703 IF (EL.NE.3) THEN
1704 C
1705 ADD THE TCTAL STRAINS
1706 DO 50 NE=1,NEL
1707 DO 60 K=1,NS2
1708 STA(NE,K)=STA(NE,K)+STST(NE,K)
1709 60 CONTINUE
1710 50 CONTINUE
1711 C
1712 OBTAIN EFFECT STRESSES
1713 NWSIF=0
1714 SREAL=0
1715 CALL STRESS(E,STRE,NEL,NS3,IELD,NS4,EPRM,NL,STA,STST,
  + ICSTR,SREAL,NS1,NS2,EALL,
  + IGMAT,NGL,STEEL,ICOMP,ICRACK,IEL,ISSC,FINISH,NWSTP,T)
1716 SREAL=1
1717 C
1718 TAKE OFF FROM TOTAL STRAINS
1719 DO 70 NE=1,NEL
1720 DO 80 K=1,NS2
1721 STA(NE,K)=STA(NE,K)-STST(NE,K)
1722 STST(NL,K)=STST(NE,K)
1723 80 CONTINUE
1724 70 CONTINUE
1725 ENF IF
1726 C
1727 OBTAIN THE LOAD VECTOR
1728 C
1729 CALL LVSECTB(DCL,NEL,STST,NS2,EALL,NS3,Y,NL,NGL,DIM,ICOMP,
  + IATYPE,IGMAT,IEL,ICRACK,STRE,AREA,STEEL,INCLUD,
  + CABSST,CABLE,YCABLE,MNOD,NOWPRO,X,NVAR,B)
1730
1731
1732 C

```

1733
1734
1735
1736
1737
1738
1739
1740
1741
1742
1743
1744
1745
1746
1747
1748
1749
1750
1751
1752
1753
1754
1755
1756
1757
1758
1759
1760
1761
1762
1763
1764
1765
1766
1767
1768
1769
1770
1771
1772
1773
1774
1775
1776
1777
1778
1779
1780
1781
1782
1783
1784
1785
1786
1787
1788
1789
1790
1791
1792

```

C
C
C      PROCEED ANALYSIS
C
C      CALL ANALIS(IGNAT,IATYPE,WLOCA,GANAG,GANAD,ISTEP,NSTEPS,ICSTR,
C      *      WMOD,NSUP,WEL,MODE3,NDISP,WBAND,E,BC,WVAR,IVAR,
C      *      IEL,X,ALOAD,APLOAD,REAC,CIR,STEEL,AREA,DELC,CLOAD,
C      *      DLOAD,SDISP,B,LCCA,PREDIS,YCABLE,CABLE,IPRET,
C      *      WPS,PSEGN,FM,FK,ICONST,STA,STRB,STRT,CRACK,
C      *      WGL,WL,WS1,NS2,WS1,NS4,CALL,Y,ICRACK,IALPHA,IELD,EPENN,
C      *      STRE,CNF,ICHECK,NSUPJ,DISP,DCH,DCL,FORCE,STRIC,
C      *      ITER,FINCAD,CABSST,GTP,ST,NCHL,NCH3,ISSC,BELIST,SREAL,
C      *      FINISH,ITWST,INCLUD,NOWPRO,ICOUNT,IAPTR,NTITER,ICCRP,ELONG,LC,T)
C      IF (FINISH.GT.0) GO TO 100
20 CONTINUE
DO 200 NE=1,WEL
EO 201 L=1,WL
STREL(WL,L)=STREL(WL,L)+STELC(WL,L)
STELC(WL,L)=0
201 CONTINUE
200 CONTINUE
100 RETURN
END
C*****
C      SUBROUTINE CREEP(TSI,TSP,T,IGNAT,ICOMP,WEL,WGL,WL,IEL,
C      *      STRST,NS2,STREL,STRLC)
C*****
C      IMPLICIT REAL*8(A-H,O-Z)
C      DIMENSION T(6),STRST(WEL,NS2),IEL(WEL,3)
C      *      ,STREL(WL,WL),STRLC(WL,WL)
C
C      ASSUMED CREEP CONSTANTS
C
C      C=0.60
C      D=10.0
C      CUC=2.35
C      CUE=2.35
C
C      TPLG=T(4)
C      TFLD=T(5)
C      GCC=0
C      ECC=0
C
C      GIRDER CREEP COEFFICIENT
C
C      IF (IGNAT.WE.0) THEN
C      IF (TSI.GT.TPLG) THEN
C      DT=(TSI-TPLG)**C
C      CTSI=(CUC*DT)/(D*DT)
C      ELSE
C      CTSI=0
C      END IF
C      DT=(TSP-TPLG)**C
C      CTSF=(CUG*DT)/(U*DT)
C      GCC=CTSIF-CTS1
C      END IF
C
C      DECK CREEP COEFFICIENT
C
C      IF (ICOMP.EQ.1) THEN
C      IF (TSI.GT.TFLD) THEN
C      DT=(TSI-TFLD)**C
C      CTSI=(CUD*DT)/(D*DT)
C      ELSE
C      CTSI=0
C      END IF

```

1793
1794
1795
1796
1797
1798
1799
1800
1801
1802
1803
1804
1805
1806
1807
1808
1809
1810
1811
1812
1813
1814

1815
1816
1817
1818
1819
1820
1821
1822
1823
1824
1825
1826
1827
1828
1829
1830
1831
1832
1833
1834
1835
1836
1837
1838
1839
1840
1841
1842
1843
1844
1845
1846
1847
1848
1849
1850
1851

```

C      DT=(TSF-TFLD)**C
C      CTSF=(CUD*DT)/(D*DT)
C      DCC=CTSIF-CTSI
C      END IF
C
C      DO 50 M2=1,WEL
C      ITYPE=IEL(WL,3)
C      IF (ITYPE.EQ.1.AND.ICOMP.EQ.0) GO TO 50
C      LIM1=1
C      IF (IGNAT.EQ.0.OR.ITYPE.EQ.1) LIM1=WGL+1
C      LIMF=M1
C      IF (ICOMP.EQ.0) LIMF=WGL
C      DO 60 I=LIM1,LIMF
C      CC=JCC
C      IF (L.GT.WGL) CC=DCC
C      REC=STREL(WL,L)+STRLC(WL,L)
C      IRECOV=1
C      IF (REC.GE.0) IRECOV=0
C      STRAIN=STREL(WL,L)+STRLC(WL,L)
C      STST(WL,L)=-CC*(STRAIN+IRECOV*STRLC(WL,L))
C      60 CONTINUE
C      50 CONTINUE
C      RETURN
C      END
C*****
C      SUBROUTINE SHRINK(TSI,TSF,T,IGNAT,ICOMP,WEL,WGL,WL,
C      *      IEL,STRST,NS2)
C*****
C      IMPLICIT REAL*8(A-H,O-Z)
C      DIMENSION T(6),STRST(WEL,NS2),IEL(WEL,3)
C
C      ASSUMED SHRINKAGE COEFFICIENTS
C
C      E=1
C      F=45
C      ESUG=0.000000
C      ESUD=C.000000
C
C      TGC=T(2)
C      TCC=T(3)
C
C      GIRDER SHRINKAGE STRAIN
C
C      IF (IGNAT.WE.0) THEN
C      DT=TSI-TGC
C      STSI=(ESUG*DT)/(F*DT)
C      DT=TSF-TGC
C      STSF=(ESUG*DT)/(F*DT)
C      GSS=STSF-STSI
C      END IF
C
C      DECK SHRINKAGE STRAIN
C
C      IF (ICOMP.EQ.1) THEN
C      DT=TSI-TCC
C      STSI=(ESUD*DT)/(F*DT)
C      DT=TSF-TCC
C      STSF=(ESUD*DT)/(F*DT)
C      DSI=STSF-STSI
C      END IF
C
C      DO 50 M2=1,WEL
C      ITYPE=IEL(WL,3)
C      IF (ITYPE.EQ.1.AND.ICOMP.EQ.0) GO TO 50

```

1852
1853
1854
1855
1856
1857
1858
1859
1860
1861
1862
1863
1864
1865
1866
1867
1868
1869
1870
1871
1872
1873
1874
1875
1876

1877
1878
1879
1880
1881
1882
1883
1884
1885
1886
1887
1888
1889
1890
1891
1892
1893
1894
1895
1896
1897
1898
1899
1900
1901
1902
1903
1904
1905
1906
1907
1908
1909
1910


```

IF (IGNAT.NE.0) THEN
DO 60 I=1,NGL
STRT(NE,L)=STRT(NE,L)+GSS
60 CONTINUE
END IF
IF (ICOMP.EQ.1) THEN
LIN=NGL+1
DO 70 I=LIN,NL
STRT(NE,L)=STRT(NE,L)+DSS
70 CONTINUE
END IF
50 CONTINUE
RETURN
END
C*****
SUBROUTINE RELAX(IST,TSI,TSF,T,E,IEL,NEL,CABLE,CABSST,PINCAB)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION T(6),E(4,6),IEL(NEL,3),CABLE(NEL,7),CABSST(NEL),
PINCAB(NEL,3)
C
C      ASSUMED CONSTANTS
C
IF (IST.EQ.0) THEN
LOW-RELAXATION STEEL
A=45
B=0.9
ELSE
STRESS-BELIEVED STEEL
A=10
B=0.85
END IF
C
TP=T(6)
RT=DLOG10((TSF-TP)/(TSI-TP))
PPU=E(1,5)*E(1,3)*(E(1,6)-(E(1,4)/E(1,1))-(E(1,5)-E(1,4))/E(1,2))
C
DO 50 NE=1,NEL
IF (IEL(NE,3).EQ.1-OR.CABLE(NE,4).EQ.0) GO TO 50
PST=PINCAB(NE,1)/CABLE(NE,4)
BELX=(PST*RT/A)*(PST/(0*PPU)-0.55)
CABLE(NE,5)=CABLE(NE,5)-BELX
CABSST(NE)=BELX/CABLE(NE,7)
50 CONTINUE
RETURN
END
C*****
SUBROUTINE PLIST(NCHEL,ICHECK,ITNST,DCN,FINISH,NCH,ITER)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION ICHECK(NCHEL),DCN(100,NCH)
WRITE(3,6000)
6000 FORMAT(10X,'M O M E N T - C U R V A T U R E - ',
'D E F L E C T I O N')
WRITE(3,1111)
DO 6010 NK=1,NCHEL
NEC=ICHECK(NK)
WRITE(3,6020)NEC
6020 FORMAT(20X,'ELEMENT #',2X,13)

```

```

1911 WRITE(3,1111)
1912 WRITE(3,6030)
1913 6030 FORMAT(1X,'STEP #',5X,'MOUSENT',6X,'CURVATURE',3X,'DEFLECTION',
1914 3X,'LOAD FACTOR',3X,'CURT. TIME',3X,'ITERATIONS',//)
1915 DO 6040 I=1,ITNST
1916 LIN=NK*6-5
1917 LIEF=NK*6-1
1918 ITERA=DCN(I,NK*6)
1919 WRITE(3,6050)I,(DCN(I,J),J=LIN,LINF),ITERA
1920 6050 FORMAT(4X,13,5(3X,D10.3),6X,13,/)
1921 6040 CONTINUE
1922 IF (FINISH.EQ.1) THEN
1923 WRITE(3,6051)ITER
1924 6051 FORMAT(10X,'****',13,' ITERATIONS EXCEEDED IN ONE STEP ****')
1925 END IF
IF (FINISH.EQ.3) THEN
WRITE(3,6052)
6052 FORMAT(10X,'**** R. STEEL OR STEEL GIRDER RUPTURE ****')
END IF
IF (FINISH.EQ.2) THEN
WRITE(3,6053)
6053 FORMAT(10X,'**** LIVE LOAD UPPER LIMIT HAS BEEN REACHED ****')
END IF
IF (FINISH.EQ.4) THEN
WRITE(3,6054)
6054 FORMAT(10X,'**** CONCRETE ULTIMATE STRAIN HAS BEEN REACHED ****')
END IF
IF (FINISH.EQ.5) THEN
WRITE(3,6055)
6055 FORMAT(10X,'**** LOAD INCREMENT IS LESS THEN 0.01/100 ****')
END IF
IF (FINISH.EQ.6) THEN
WRITE(3,6056)
6056 FORMAT(10X,'**** DRIVING DISPL. HAS BEEN INCREASED FIVE TIMES ****')
END IF
IF (FINISH.EQ.7) THEN
WRITE(3,6057)
6057 FORMAT(10X,'**** SECTION IS ALL CRACKED OR YIELDED ****')
END IF
WRITE(3,1111)
1111 FORMAT(/,130(' '),/)
6010 CONTINUE
RETURN
END
C*****
SUBROUTINE RECL (RELIST,ITNST,NDISP,NMOD,PREDIS,NSUP,NVAR)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION RELIST(100,10),PREDIS(NSUP,2),NVAR(NMOD,3),NUN(20)
NNT=NMOD+1-NDISP
WRITE(3,2222)
2222 FORMAT(/,130(' '),/)
WRITE(3,1000)
1000 FORMAT(30X,'S U P P O R T R E A C T I O N S')
WRITE(3,1111)
1111 FORMAT(/,130(' '),/)
DO 5 I=1,20
NUM(I)=0
5 CONTINUE

```

```

J=0
DO 10 NS=1, NSUP
NM=PREDIS(NS,1)
DO 20 I=1,3
IF (NVAR(NM,I).EQ.0) THEN
J=J+1
NUR(J)=NS
J=J+1
NUR(J)=I
END IF
20 CONTINUE
10 CONTINUE
NR12=NR1+2
WRITE(3,1100) (NUR(I),I=1,NR12)
1100 FORMAT(1X,'STEP',10(2X,'S',I2,1X,'R',I2),//)
DO 30 I=1,ITNST
WRITE(3,1200) I, (RELIST(I,J),J=1,NR12)
1200 FORMAT(14,1X,10(1X,D10.3),/)
30 CONTINUE
RETURN
END
C*****
SUBROUTINE PLOT(IX,YY,DCN,ITNST,NCH3,ICHECK,NCHL)
C*****
IMPLICIT REAL*8(A-H,O-Z)
REAL*4 XX(ITNST),YY(ITNST)
DIMENSION DCH(300,NCH3),ICHECK(NCHL)
ITER=0
DO 1 I=1,ITNST
XX(I)=0
YY(I)=0
1 CONTINUE
WRITE(3,2222)
2222 FORMAT(/,130(' '),/)
WRITE(3,10)
10 FORMAT(50X,'P L O T S')
DO 20 I=1,NCHL
WRITE(3,2222)
DO 30 J=1,ITNST
K=(I-1)*5
XX(J)=DCH(J,K+2)
YY(J)=DCH(J,K+1)
30 CONTINUE
CALL GENPT(XX,YY,ITNST,ITER)
NCH=ICHECK(I)
WRITE(3,100) NCH
100 FORMAT(50X,'ELEM #',I4,5X,'M O M E N T - C U R V A T U R E',//)
DO 40 J=1,ITNST
K=(I-1)*5
XX(J)=DCH(J,K+3)
40 CONTINUE
CALL GENPT(XX,YY,ITNST,ITER)
WRITE(3,110) NCH
110 FORMAT(50X,'ELEM #',I4,5X,'M O M E N T - D E F L E C T I O N',//)
20 CONTINUE
RETURN
END
C*****

```

```

2028 SUBROUTINE EQULEN(CMF,NEL,FORCE,STRST,NS2,EALL,NS3,IPRET,ICSTR,
2029 Y,NL,NGL,DIM,ICOMP,IATYPE,IGNAT,IEL,ICRACK,
2030 STRE,AREA,STEEL,ISTOP,DCL,B,I,NMOD,STRLC,LC,LOCA,WLOCA,
2031 NVAR,E,NGL,IELD,NS4,EPEM,STA,NS1,NDISP,NBAND,
2032 ST,DISP,SDISP,STRB,ITER,ITER,ISSC,MODE3,ISTEP,FINISH,
2033 INCLUD,CABLE,PINCAB,YCABLE,CABSST,GTP,NOWPRO,MSTEPS,T,SREAL,BQ
2034 C*****
2035 IMPLICIT REAL*8(A-H,O-Z)
2036 DIMENSION FORCE(NEL,3),STRST(NEL,NS2),EALL(NEL,NS3),
2037 Y(NL,3),DIM(NEL,8),IEL(NEL,3),ICRACK(NEL,NL),
2038 STRE(NEL,NS3),AREA(NEL,8),STEEL(NEL,6),DCL(NMOD,3),
2039 B(1),X(NMOD,2),NVAR(NMOD,3),E(4,6),STRLC(NEL,NL),LCCA(WLOCA,8),
2040 IELD(NEL,NS4),EPEM(NEL,NL),STA(NEL,NS1),GTP(NEL),T(6),
2041 ST(NODE3,NBAND),DISP(NMOD,3),SDISP(NMOD,3),STRB(NEL,8)
2042 ,PINCAB(NEL,3),CABSST(NEL),CABLE(NEL,7),YCABLE(NMOD),CMF(NODE3,3)
2043 ITER=0
2044 NMSTP=1
2045 100 CONTINUE
2046 CALL STRESS(I,STRE,NEL,NS3,IELD,NS4,EPEM,NL,STA,STRST,
2047 ICSTR,SREAL,NS1,NS2,EALL,
2048 IGNAT,NGL,STEEL,ICOMP,ICRACK,IEL,ISSC,FINISH,NMSTP,T)
2049 CALL FORSC(NEL,FORCE,NS1,EALL,NS3,Y,NL,NGL,DIM,ICOMP,
2050 IATYPE,IGNAT,IEL,ICRACK,STRE,AREA,STEEL,STA,
2051 INCLUD,PINCAB,CABLE,YCABLE,NMOD,GTP,NOWPRO)
2052 C
2053 UPDATE THE EXTERNAL LOAD VECTOR
2054 C
2055 DO 400 J=1,NODE3
2056 CMF(J,2)=CMF(J,1)*CMF(J,3)*ISTEP/MSTEPS
2057 400 CONTINUE
2058 C
2059 CALL CHECKE(FORCE,CMF,NEL,ISTOP,IEL,DCL,DIM,B,AREA,X,NMOD,
2060 NVAR,MODE3,NDISP,PINCAB,INCLUD,BQ)
2061 IF (ISTOP.EQ.1) GO TO 200
2062 CALL RESOLV(NDISP,NBAND,ST,B)
2063 ITER=ITER+1
2064 NTITER=NTITER+1
2065 CALL DISPLA(B,NDISP,NVAR,NMOD,DISP,SDISP)
2066 CALL STRAIN(E,DIM,NEL,STEEL,IEL,NVAR,IGNAT,IATYPE,IPRET,NMOD,
2067 X,ICOMP,STA,STRB,STRST,NGL,NGL,NS1,NS2,Y,GTP,NOWPRO)
2068 IF (LOCA(LC,1).NE.7) THEN
2069 DO 555 NE=1,NEL
2070 DO 555 L=1,NL
2071 STRLC(NE,L)=STRLC(NE,L)+STEST(NE,L)
2072 555 CONTINUE
2073 555 CONTINUE
2074 END IF
2075 IF (IGNAT.EQ.1) THEN
2076 IF (INCLUD.EQ.1) THEN
2077 CALL MDCAB(CABLE,YCABLE,B,NEL,IEL,NVAR,X,NMOD,E,CABSST,NMSTP,
2078 MODE3)
2079 IF (NOWPRO.EQ.1.AND.IPRET.EQ.1) THEN
2080 DO 8000 JK=1,NEL
2081 PINCAB(JK,1)=CABLE(JK,3)
2082 8000 CONTINUE
2083 END IF
2084 END IF
2085 END IF
2086 IF (ITER.GE.500) THEN
2087 FINISH=1
2088 2086
2087
2088
2089
2090
2091
2092
2093
2094
2095
2096
2097
2098
2099
2100
2101
2102
2103
2104
2105
2106
2107
2108
2109
2110
2111
2112
2113
2114
2115
2116
2117
2118
2119
2120
2121
2122
2123
2124
2125
2126
2127
2128
2129
2130
2131
2132
2133
2134
2135
2136
2137
2138
2139
2140
2141
2142
2143
2144
2145

```

```

GO TO 300
END IF
MNSTP=0
GO TO 100
200 CONTINUE
DO 10 I=1,NMOD
DO 20 J=1,3
JA=MVAR(I,J)
IF (JA.NE.0) B(JA)=DISP(I,J)
20 CONTINUE
10 CONTINUE
300 CONTINUE
RETURN
END
C.....

SUBROUTINE DISPLA(B,NDISP,MVAR,NMOD,DISP,SDISP)
C.....
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION B(1),MVAR(NMOD,3),DISP(NMOD,3),SDISP(NMOD,3)
DO 200 I=1,NMOD
DO 100 J=1,3
JA=MVAR(I,J)
IF (JA.EQ.0) THEN
DISP(I,J)=0
SDISP(I,J)=0
ELSE
DISP(I,J)=DISP(I,J)+B(JA)
SDISP(I,J)=SDISP(I,J)+B(JA)
END IF
100 CONTINUE
200 CONTINUE
RETURN
END
C.....

SUBROUTINE MOCURV(DCM,NCH3,MCHL,WEL,FORCE,SDISP,NMOD,
* STRB,ITNST,ICHECK,DIM,IGMAT,IEL,ITER,SALPHA,TIME)
C.....
IMPLICIT REAL*8 (A-H,O-Z)
DIMENSION DCM(300,NCH3),FORCE(NEL,3),SDISP(NMOD,3),STRB(WEL,8),
* ICHECK(MCHL),DIM(WEL,8),IEL(WEL,3)
DO 10 WK=1,MCHL
MCH=ICHECK(WK)
GH=DIM(WK,4)
IF (IGMAT.NE.0) GH=GH+DIM(WK,6)+DIM(WK,8)
M1=IEL(WK,1)
M2=IEL(WK,2)
CURV=(STRB(WK,1)-STRB(WK,2))/GH
IF (IEL(WK,3).EQ.1) CURV=(STRB(WK,3)-STRB(WK,4))/DIM(WK,2)
DISP=(SDISP(M1,2)+SDISP(M2,2))/2
ANCH=FORCE(WK,2)
DCM(ITNST,WK*6-5)=ANCH
DCM(ITNST,WK*6-4)=CURV
DCM(ITNST,WK*6-3)=DISP
DCM(ITNST,WK*6-2)=SALPHA
DCM(ITNST,WK*6-1)=TIME
DCM(ITNST,WK*0)=ITER
10 CONTINUE
RETURN

```

```

2146 END
2147 C.....
2148
2149 SUBROUTINE MODGD(NMOD,MSUP,MVAR,IVAR,NDISP,PREDIS,MODIFY)
2150 C.....
2151 C THIS SUBROUTINE CALCULATES THE NEW GLOBAL DISPLACEMENTS
2152 C THAT INCLUDE THE PRESCRIBED SUPPORT DISPLACEMENTS
2153 C
2154 IMPLICIT REAL*8 (A-H,O-Z)
2155 DIMENSION MVAR(NMOD,3),IVAR(NMOD,3),PREDIS(MSUP,2)
2156 C
2157 C CHANGE NODE CONDITION AT SUPPORTS
2158 C
2159 DO 10 I=1,MSUP
2160 IF (PREDIS(I,2).NE.0) THEN
2161 NODE=PREDIS(I,1)
2162 IF (MODIFY.EQ.0) IVAR(NODE,2)=J
2163 IF (MODIFY.EQ.1) IVAR(NODE,2)=1
2164 END IF
2165 10 CONTINUE
2166 C OBTAIN NEW MVAR AND NDISP
2167 MDISP=0
2168 DO 11 I=1,NMOD
2169 DO 9 J=1,3
2170 MVAR(IJ)=IVAR(I,J)
2171 IF (MVAR(IJ).EQ.0) THEN
2172 NDISP=NDISP+1
2173 MVAR(I,J)=NDISP
2174 ELSE
2175 MVAR(I,J)=0
2176 END IF
2177 9 CONTINUE
2178 11 CONTINUE
2179 RETURN
2180 END
2181 C.....
2182 SUBROUTINE NEWSOL(ST,B,NDISP,WEAND,MVAR,NMOD,MSUP,PREDIS)
2183 C.....
2184 C THIS SUBROUTINE CHANGES ST AND B FOR A NEW SOLUTION OF DISPL.
2185 C
2186 IMPLICIT REAL*8 (A-H,O-Z)
2187 DIMENSION ST(NDISP,NDAND),B(NDISP),MVAR(NMOD,3),PREDIS(MSUP,2)
2188 DO 10 I=1,MSUP
2189 IF (PREDIS(I,2).NE.0) THEN
2190 NODE=PREDIS(I,1)
2191 IGDISP=MVAR(NODE,2)
2192 ST(IGDISP,1)=ST(IGDISP,1)+1.E12
2193 B(IGDISP)=ST(IGDISP,1)*PREDIS(I,2)
2194 END IF
2195 10 CONTINUE
2196 RETURN
2197 END
2198 C.....
2199 SUBROUTINE FELCAD(IGMAT,IATYPE,GAMAG,GAMAD,DIM,WEL,IEL,DELO)
2200 C.....
2201 IMPLICIT REAL*8 (A-H,O-Z)
2202 DIMENSION DIM(WEL,8),IEL(WEL,3),DELO(WEL,2)
2203 C
2204
2205
2206
2207
2208
2209
2210
2211
2212
2213
2214
2215
2216
2217
2218
2219
2220
2221
2222
2223
2224
2225
2226
2227
2228
2229
2230
2231
2232
2233
2234
2235
2236
2237
2238
2239
2240
2241
2242
2243
2244
2245
2246
2247
2248
2249
2250
2251
2252
2253
2254
2255
2256
2257
2258
2259
2260

```



```

TDI = (DM*UD*HB**3) * ICOMP / 12 * TDA * (HT*HW*HB*HD/2) **2
GI = (BT*HT**3) / 12 * (BT*HT) * (HW*HB*HT/2) **2 *
  * (BW*HW**3) / 12 * (BW*HW) * (HD*H4/2) **2 *
  * (EB*HB**3) / 12 * (EB*HB) * (HD/2) **2
TGI = GI + TRSAT * STEEL(I,4) **2 + TRSAB * STEEL(I,6) **2
TCI = TDI + TGI
IF (IEL(I,3) .EQ. 0) THEN
  AREA(I,4*JK-3) = TCI
  AREA(I,4*JK-2) = TCA
  AREA(I,4*JK-1) = TCM
  AREA(I,4*JK) = TCI - TCA + TCI **2
ELSE
  AREA(I,4*JK-3) = 0
  AREA(I,4*JK-2) = TDA
  AREA(I,4*JK-1) = 0
  AREA(I,4*JK) = 0
END IF
20 CONTINUE
END IF
100 CONTINUE
WRITE(3,2222)
2222 FORMAT(/,130(' '),/)
WRITE(3,30)
30 FORMAT(10X,'O R I G I N A L   S E C T I O N   P R O P E R T I E S'
  * ,10X,'( TRANSFORMED )',/)
WRITE(3,40)
40 FORMAT(20X,'( NON-COMPOSITE SECTION )',
  * ,40X,'( COMPOSITE SECTION )')
WRITE(3,1111)
1111 FORMAT(/,130(' '),/)
WRITE(3,50)
50 FORMAT(1X,'ELEM ',4X,'CENTROID',10X,'AREA',9X,'AREA NON.',
  * ,8X,'INERTIA',6X,'CENTROID',10X,'AREA',9X,'AREA NON.',
  * ,8X,'INERTIA',/)
DO 60 I=1,NEL
  WRITE(3,70) I, (AREA(I,J), J=1,8)
70 FORMAT(4X,13,8(2X,D13.6),/)
60 CONTINUE
RETURN
END
C*****
SUBROUTINE NWAREA(NEL,DIM,ICOMP,IATYPE,IGNAT,IEL,NGL,NL,STRE,
  * ICRACK,EALL,STEEL,NS3,Y,AREA,E,FINISH)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION DIM(NEL,8),IEL(NEL,3),STRE(NEL,NS3),ICRACK(NEL,NL),
  * EALL(NEL,NS3),STEEL(NEL,6),Y(NL,3),AREA(NEL,8),E(4,6)
DO 10 NE=1,NEL
  DO 2 J=1,8
    AREA(NE,J)=0
2 CONTINUE
EA=0
ES=0
EI=0
GA=0
ITYPE=IEL(NE,3)
CALL LAYER(DIM,ICOMP,IATYPE,IGNAT,ITYPE,NEL,NE,Y,TH,NGL,NL)
IF (ITYPE.EQ.1) GO TO 100
IF (ICOMP.EQ.0) LIM=NGL

```

2380
2381
2382
2383
2384
2385
2386
2387
2388
2389
2390
2391
2392
2393
2394
2395
2396
2397
2398
2399
2400
2401
2402
2403
2404
2405
2406
2407
2408
2409
2410
2411
2412
2413
2414
2415
2416
2417
2418
2419
2420
2421
2422
2423
2424
2425
2426
2427
2428
2429
2430
2431
2432
2433
2434
2435
2436
2437
2438

```

IF (ICOMP.EQ.1) LIM=NGL
DO 20 I=1,LIM
  IF (EALL(NE,I) .LT. 0) THEN
    EMCD=0
  ELSE
    EMCD=EALL(NE,I)
  END IF
  IF (ICRACK(NE,I) .EQ. 0) THEN
    IF (STRE(NE,I) .GE. 0) GO TO 20
  END IF
  EA=EA+Y(L,2)*EMCD
  ES=ES+Y(L,1)*Y(L,2)*EMCD
  EI=EI+Y(L,2)**3/12/Y(L,3)**2+Y(L,2)*Y(L,1)**2*EMCD
20 CONTINUE
IF (ICOMP.EQ.0) LIM=2
IF (ICOMP.EQ.1) LIM=1
DO 30 K=LIM,J
  J=2*K-1
  EA=EA+STEEL(NE,J)*EALL(NE,NL*K)
  ES=ES+STEEL(NE,J)*EALL(NE,NL*K)*STEEL(NE,J+1)
  EI=EI+STEEL(NE,J)*EALL(NE,NL*K)*STEEL(NE,J+1)**2
30 CONTINUE
GO TO 100
100 IF (ICOMP.EQ.0) GO TO 10
LIM=NGL+1
DO 40 I=LIM,NL
  IF (EALL(NE,I) .LT. 0) THEN
    EMCD=0
  ELSE
    EMCD=EALL(NE,I)
  END IF
  IF (ICRACK(NE,I) .EQ. 0) THEN
    IF (STRE(NE,I) .GE. 0) GO TO 40
  END IF
  EA=EA+Y(L,2)*EMCD
40 CONTINUE
EA=EA+STEEL(NE,1)*EALL(NE,NL+1)
200 CONTINUE
IF (ITYPE.EQ.0) THEN
  IF (EA.EQ.0) THEN
    FINISH=7
    GO TO 1000
  ELSE
    AREA(NE,1) = ES/EA
    AREA(NE,2) = EA/F(3,1)
    AREA(NE,3) = ES/(3,1)
    AREA(NE,4) = EI/E(3,1)
    AREA(NE,5) = EA
    AREA(NE,6) = ES
    AREA(NE,7) = EI
    V=0.2
    AREA(NE,8) = EA/(2*(1+V))
  END IF
  ELSE
    AREA(NE,5) = EA
  END IF
10 CONTINUE
1000 CONTINUE
RETURN
END

```

2439
2440
2441
2442
2443
2444
2445
2446
2447
2448
2449
2450
2451
2452
2453
2454
2455
2456
2457
2458
2459
2460
2461
2462
2463
2464
2465
2466
2467
2468
2469
2470
2471
2472
2473
2474
2475
2476
2477
2478
2479
2480
2481
2482
2483
2484
2485
2486
2487
2488
2489
2490
2491
2492
2493
2494
2495
2496
2497
2498

```

C *****
SUBROUTINE FJLOAD(NMOD,NEL,IEL,DLOAD,CLOAD,X,B,NVAB)
C *****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION IEL(NEL,3),CLOAD(NMOD,3),DLOAD(NEL,3),
* ELOAD(2,3),X(NMOD,2),B(1),NVAR(NMOD,3)
REAL*8 L
C
C CLCAD = NODAL FORCES
C DLCAD = DISTRIBUTED FORCES
C
DO 10 I=1,NEL
C
C AP=POSITION OF THE VERT. FORCE IN THE ELEMENT
C
AP=DLOAD(I,3)
N1=IEL(I,1)
N2=IEL(I,2)
L=1(N2,1)-X(N1,1)
BP=L*AF
DO 1 K=1,2
DO 2 J=1,3
ELCAD(K,J)=0
2 CONTINUE
1 CONTINUE
C1=(3*AP*BP)/L**3
C2=(AP*3*BP)/L**3
C
C DISTRIB (,1) AND COMC (,2) VERTICAL FORCES ARE
C TRANSFORMED TO EQUIVALENT NODAL FORCES
C
ELOAD(1,2)=-DLOAD(I,2)*C1*BP**2-CLOAD(I,1)*L/2
ELCAD(2,2)=-DLOAD(I,2)*C2*AP**2-DLOAD(I,1)*L/2
DO 20 J=1,3
C
C NODAL FORCES = NODAL LCADS + EQUIVALENT NODAL LOADS
C
CLOAD(N1,J)=CLOAD(N1,J)+ELCAD(1,J)
CLOAD(N2,J)=CLOAD(N2,J)+ELOAD(2,J)
20 CONTINUE
10 CONTINUE
C
C B - STORES THE NODAL FORCES
C
NDIS=0
DO 11 I=1,NMOD
DO 9 J=1,3
NVAR(I,J)=NVAR(I,J)
IF (NVAR(I,J).EQ.0) THEN
NDIS=NDIS+1
B(NDIS)=CLOAD(I,J)
END IF
9 CONTINUE
11 CONTINUE
RETURN
END
C *****
SUBROUTINE ADSTIF(NMOD,NDISP,NBAKD,NEL,IEL,

```

```

2499 * NVAB,X,ST,DC,DIM,AREA,YCABLE,CABLE,INCLUD, 2557
* NSUP3,NSUP,FREDIS) 2558
C ***** 2559
IMPLICIT REAL*8(A-H,O-Z) 2560
DIMENSION IEL(NEL,3),ELST(6,6),NVAR(NMOD,3),ST(NDISP,NBAKD), 2561
* X(NMOD,2),DIM(NEL,8),ABEA(NEL,8),YCABLE(NMOD),CABLE(NEL,7) 2562
* ,FREDIS(NSUP,2) 2563
INTEGER EN,DISF 2564
DO 700 I=1,NDISP 2565
EO 600 J=1,NBAKD 2566
ST(I,J)=0 2567
600 CONTINUE 2568
700 CONTINUE 2569
DO 500 I1=1,NEL 2570
EN=11 2571
CALL ELSTIF(X,ELST,NMOD,NEL,IEL,EN,DIM,AREA,YCABLE, 2572
* CABLE,INCLUD) 2573
DO 400 J1=1,2 2574
NOCF1=IEL(I1,J1) 2575
DO 300 K1=1,3 2576
IVAR1=NVAR(NODE1,K1) 2577
IF (IVAR1.EQ.0) GO TO 300 2578
JK1=3*(J1-1)+K1 2579
DO 200 J2=J1,2 2580
NOCF2=IEL(I1,J2) 2581
JK2=1 2582
IF (J2.EQ.J1) JK=K1 2583
EO 150 K2=JK,J 2584
IVAR2=NVAR(NODE2,K2) 2585
IF (IVAR2.EQ.0) GO TO 150 2586
JK2=3*(J2-1)+K2 2587
IV1=IVAR1 2588
IV2=IVAR2 2589
IF (IVAR2.GE.IVAR1) GO TO 100 2590
IV1=IVAR2 2591
IV2=IVAR1 2592
100 IV2=IV2-IV1+1 2593
ST(IV1,IV2)=ST(IV1,IV2)+ELST(JK1,JK2) 2594
150 CONTINUE 2595
200 CONTINUE 2596
300 CONTINUE 2597
400 CONTINUE 2598
500 CONTINUE 2599
C ***** ADD BEARING COEFFICIENT 2600
IF (BC.EQ.0) GO TO 900 2601
DO 800 I=1,NMOD 2602
IF (NVAR(I,2).EQ.0.AND.NVAR(I,1).GT.0) THEN 2603
DISP=NVAR(I,1) 2604
ST(DISP,1)=ST(DISP,1)+BC 2605
END IF 2606
800 CONTINUE 2607
900 CONTINUE 2608
RETURN 2609
END 2610
C ***** 2611
SUBROUTINE ELSTIF(X,ST,NMOD,NEL,IEL,EN,DIM,AREA, 2612
* YCABLE,CABLE,INCLUD) 2613
C ***** 2614
IMPLICIT REAL*8(A-H,O-Z) 2615

```

```

DIMENSION X(NMOD,2), ST(6,6), IEL(NEL,3), CS(6,6)
* DIM(NEL,8), AREA(NEL,8), YCABLE(NMOD), CABLE(NEL,7)
REAL*8 L
INTEGER EN,TYPE
DO 10 I=1,6
DO 20 J=1,6
ST(I,J)=0
CS(I,J)=0
20 CONTINUE
10 CONTINUE
N1=IEL(EN,1)
N2=IEL(EN,2)
L=X(N2,1)-X(N1,1)
Y1=X(N1,2)
Y2=X(N2,2)
TYPE=IEL(EN,3)

```

C
C
C

GIBDA ELEMENT STIFFNESS MATRIX

```

IF (TYPE.EQ.0) THEN
EA=AREA(EN,5)
ES=AREA(EN,6)
EI=AREA(EN,7)
GA=AREA(EN,8)
ST(1,1)=EA/L
ST(1,3)=-ES/L-EA*Y1/L
ST(3,1)=-ES/L-EA*Y1/L
ST(1,4)=-EA/L
ST(4,1)=-EA/L
ST(1,6)=ES/L+EA*Y2/L
ST(6,1)=ES/L+EA*Y2/L
ST(2,2)=GA/L
ST(2,3)=GA/2
ST(3,2)=GA/2
ST(2,5)=-GA/L
ST(5,2)=-GA/L
ST(2,6)=GA/2
ST(6,2)=GA/2
ST(3,3)=EI/L+GA*L/4+{EA*Y2**2+2*ES*Y1}/L
ST(3,4)=ES/L+EA*Y1/L
ST(4,3)=ES/L+EA*Y1/L
ST(3,5)=-GA/2
ST(5,3)=-GA/2
ST(3,6)=-EI/L+GA*L/4-{EA*Y1*Y2+ES*Y1+ES*Y2}/L
ST(6,3)=-EI/L+GA*L/4-{EA*Y1*Y2+ES*Y1+ES*Y2}/L
ST(4,4)=EA/L
ST(4,6)=-ES/L-EA*Y2/L
ST(6,4)=-ES/L-EA*Y2/L
ST(5,5)=GA/L
ST(5,6)=-GA/2
ST(6,5)=-GA/2
ST(6,6)=EI/L+GA*L/4+{EA*Y2**2+2*ES*Y2}/L

```

C
C
C

PRESTRESSING CABLE STIFFNESS

```

IF (INCLUD.EQ.0.OR.CABLE(EN,4).EQ.0) GO TO 100
ALPHA=CABLE(EN,1)
ACCS=DCOS(ALPHA)
ASIN=DSIN(ALPHA)
YP1=YCABLE(N1)*Y1

```

```

2616 YP2=YCABLE(N2)*Y2
2617 AEI=CABLE(EN,4)*CABLE(EN,7)/CABLE(EN,2)
2618 CS(1,1)=ACCS**2
2619 CS(4,4)=ACCS**2
2620 CS(4,1)=-ACCS**2
2621 CS(1,4)=-ACCS**2
2622 CS(2,2)=ASIN**2
2623 CS(5,5)=ASIN**2
2624 CS(2,5)=-ASIN**2
2625 CS(5,2)=-ASIN**2
2626 CS(1,5)=ASIN*ACCS
2627 CS(5,1)=ASIN*ACCS
2628 CS(2,4)=ASIN*ACCS
2629 CS(4,2)=ASIN*ACCS
2630 CS(1,2)=-ASIN*ACCS
2631 CS(2,1)=-ASIN*ACCS
2632 CS(4,5)=-ASIN*ACCS
2633 CS(5,4)=-ASIN*ACCS
2634 CS(3,4)=YP1*ACCS**2
2635 CS(4,3)=YP1*ACCS**2
2636 CS(1,3)=-YP1*ACCS**2
2637 CS(3,1)=-YP1*ACCS**2
2638 CS(3,2)=YP1*ASIN*ACCS
2639 CS(2,3)=YP1*ASIN*ACCS
2640 CS(3,5)=-YP1*ASIN*ACCS
2641 CS(5,3)=-YP1*ASIN*ACCS
2642 CS(3,3)=(YP1*ACCS)**2
2643 CS(1,6)=YP1*ACCS**2
2644 CS(6,1)=YP1*ACCS**2
2645 CS(4,6)=-YP2*ACCS**2
2646 CS(6,4)=-YP2*ACCS**2
2647 CS(5,6)=YP2*ASIN*ACCS
2648 CS(6,5)=YP2*ASIN*ACCS
2649 CS(2,6)=-YP2*ASIN*ACCS
2650 CS(6,2)=-YP2*ASIN*ACCS
2651 CS(3,6)=-YP1*YP2*ACCS**2
2652 CS(6,3)=-YP1*YP2*ACCS**2
2653 CS(6,6)=(YP2*ACCS)**2
2654 DO 40 I=1,6
2655 DO 50 J=1,6
2656 ST(I,J)=ST(I,J)+CS(I,J)*AEI
2657 50 CONTINUE
2658 40 CONTINUE
2659 ELSE
2660 C
2661 C
2662 C
2663 H1=DIM(EN,3)*Y1
2664 H2=DIM(EN,4)*Y2
2665 EA=AREA(EN,5)/L
2666 ST(1,1)=EA
2667 ST(4,4)=EA
2668 ST(1,4)=-EA
2669 ST(4,1)=-EA
2670 ST(1,6)=EA*H2
2671 ST(6,1)=EA*H2
2672 ST(4,3)=-EA*H1
2673 ST(3,4)=-EA*H1
2674 ST(1,3)=-EA*H1
2675 ST(3,1)=-EA*H1

```

2676
2677
2678
2679
2680
2681
2682
2683
2684
2685
2686
2687
2688
2689
2690
2691
2692
2693
2694
2695
2696
2697
2698
2699
2700
2701
2702
2703
2704
2705
2706
2707
2708
2709
2710
2711
2712
2713
2714
2715
2716
2717
2718
2719
2720
2721
2722
2723
2724
2725
2726
2727
2728
2729
2730
2731
2732
2733
2734
2735


```

      ST(6,6)=-EA*H2
      ST(6,4)=-EA*H2
      ST(3,3)=EA*H1*H1
      ST(6,6)=EA*H2*H2
      ST(3,6)=-EA*H1*H2
      ST(6,3)=-EA*H1*H2
      END IF
100 RETURN
      END
C.....
      SUBROUTINE SOLVE (NEQ,NBAND,A,E)
C.....
C      A = GLOBAL STIFFNESS MATRIX
C      B = INPUT AS THE NODAL FORCES
C      OUTPUT AS THE NODAL DISPLACEMENTS
C
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION A(NEQ,NBAND),B(NEQ)
      NEQ=NEQ-1
      DO 400 I=1,NEQ1
      DIAG=A(I,I)
      IF (DIAG.GT.0.000000001)GO TO 100
      WRITE(3,1000)I,DIAG
1000 FORMAT(5X,'EQUATION #',I3,' HAS DIAG TERM=',D20.13,///)
      CALL EXIT
100 CONTINUE
      II=I+1
      IJ=I+NEAND-1
      IF (IJ.GT.NEQ) IJ=NEQ
      JJ=1
      DO 300 J=II,IJ
      JJ=JJ+1
      COEF=A(I,JJ)
      IF (COEF.EQ.0)GO TO 300
      COEF=COEF/DIAG
      NB=NBAND+I-J
      JJJ=JJ+1
      DO 200 K=1,NB
      JJJ=JJJ+1
      A(J,K)=A(J,K)-COEF*A(I,JJJ)
200 CONTINUE
      B(J)=B(J)-COEF*B(I)
      A(I,JJ)=COEF
300 CONTINUE
      B(I)=B(I)/DIAG
400 CONTINUE
      DIAG=A(NEQ,I)
      IF (DIAG.GT.0.000000001)GO TO 450
      WRITE(3,1000)NEQ,DIAG
      CALL EXIT
450 CONTINUE
      B(NEQ)=B(NEQ)/DIAG
      I=NEQ
      DO 600 II=1,NEQ1
      I=I-1
      JJ=I+1
      JK=I+NEAND-1
      IF (JK.GT.NEQ) JK=NEQ

```

```

2736      KK=1
2737      DO 500 J=JJ,JK
2738      KK=KK+1
2739      B(I)=B(I)-A(I,KK)*B(J)
2740      500 CONTINUE
2741      600 CONTINUE
2742      RETURN
2743      END
2744 C.....
2745
      SUBROUTINE RESCLV(NEQ,NBAND,A,E)
C.....
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION A(NEQ,NBAND),B(NEQ)
      NEQ=NEQ-1
      DO 400 I=1,NEQ1
      II=I+1
      IJ=I+NEAND-1
      IF (IJ.GT.NEQ) IJ=NEQ
      JJ=1
      DO 300 J=II,IJ
      JJ=JJ+1
      B(J)=B(J)-A(I,JJ)*B(I)
300 CONTINUE
      B(I)=B(I)/A(I,I)
400 CONTINUE
      B(NEQ)=B(NEQ)/A(NEQ,I)
      I=NEQ
      DO 600 II=1,NEQ1
      I=I-1
      JJ=I+1
      JK=I+NEAND-1
      IF (JK.GT.NEQ) JK=NEQ
      KK=1
      DO 500 J=JJ,JK
      KK=KK+1
      B(I)=B(I)-A(I,KK)*B(J)
500 CONTINUE
600 CONTINUE
      RETURN
      END
C.....
      SUBROUTINE STRAIN(E,DIM,NEL,STEEL,IEL,NVAR,IGNAT,IATYPE,IPRET,
      *NRCD,I,ICOMP,STA,STRO,STNST,NL1,NL,NL,NL1,NL2,Y,STP,NOWPHO)
C.....
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION B(1),DIM(NEL,N),STEEL(NEL,N),IEL(NEL,3),
      * NVAR(NMOD,3),DISP(6),STNU(NEL,8),STA(NEL,NL1),
      * X(NMOD,2),Y(NL,3),STBST(NEL,NL2),GTP(NEL)
      INTEGER EN,TYPE
      DO 10 I=1,NEL
      DO 11 JK=1,NL2
      STBST(I,JK)=0
11 CONTINUE
      EN=1
      DO 20 J=1,1
      NI=IEL(I,1)
      JA=NVAR(NI,J)
      IF (JA.L.E.0) THEN

```



```

DISP(J)=0
ELSE
DISP(J)=B(JA)
END IF
N2=IEL(I,2)
J3=J+3
JA=NVAR(N2,J)
IF (JA.EQ.0) THEN
DISP(J3)=0
ELSE
DISP(J3)=B(JA)
END IF
20 CONTINUE
EL=X(N2,1)-X(N1,1)
TYPE=IEL(I,3)
CALL LAYER(DIM,ICOMP,IATYPE,IGMAT,TYPE,NEL,EN,Y,TH,NCL,NL)
IF (TYPE.EQ.0) THEN
DO 30 J=1,NCL
Y1=Y(J,1)+X(N1,2)
Y2=Y(J,1)+X(N2,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STST(I,J)=EX
STA(I,J)=STA(I,J)+EX
30 CONTINUE
Y1=X(N1,2)
Y2=X(N2,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STSB(I,1)=STSB(I,1)+EX
Y1=Y1+TH
Y2=Y2+TH
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STRB(I,2)=STRB(I,2)+EX
END IF
IF (ICOMP.EQ.0) GO TO 1000
LIE=NCL+1
DO 40 J=LIE,NL
IF (TYPE.EQ.0) THEN
Y1=Y(J,1)+X(N1,2)
Y2=Y(J,1)+X(N2,2)
ELSE
Y1=X(J,1)+X(N1,2)+DIM(I,3)-DIM(I,2)/2
Y2=X(J,1)+X(N2,2)+DIM(I,4)-DIM(I,2)/2
END IF
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STST(I,J)=EX
STA(I,J)=STA(I,J)+EX
40 CONTINUE
IF (TYPE.EQ.0) THEN
Y1=TH+X(N1,2)
Y2=TH+X(N2,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STSB(I,3)=STSB(I,3)+EX
Y1=Y1+DIM(I,2)
Y2=Y2+DIM(I,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STRB(I,4)=STRB(I,4)+EX
ELSE
Y1=X(N1,2)+DIM(I,3)-DIM(I,2)/2
Y2=X(N2,2)+DIM(I,4)-DIM(I,2)/2
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL

```

```

2853 STSB(I,3)=STSB(I,3)+EX
2854 Y1=Y1+DIM(I,2)
2855 Y2=Y2+DIM(I,2)
2856 EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
2857 STRB(I,4)=STRB(I,4)+EX
2858 END IF
2859 IF (STEEL(I,1).GT.0) THEN
2860 Y1=STEEL(I,2)+X(N1,2)
2861 Y2=STEEL(I,2)+X(N2,2)
2862 LX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
2863 STST(I,NL+1)=EX
2864 STA(I,NL+1)=STA(I,NL+1)+EX
2865 END IF
1000 IF (STEEL(I,3).GT.0) THEN
Y1=STEEL(I,4)+X(N1,2)
Y2=STEEL(I,4)+X(N2,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STST(I,NL+2)=EX
STA(I,NL+2)=STA(I,NL+2)+EX
END IF
IF (STEEL(I,5).GT.0) THEN
Y1=STEEL(I,6)+X(N1,2)
Y2=STEEL(I,6)+X(N2,2)
EX=(DISP(4)-DISP(1)+Y1*DISP(3)-Y2*DISP(6))/EL
STST(I,NL+3)=EX
STA(I,NL+3)=STA(I,NL+3)+EX
END IF
IF (TYPE.EQ.0) THEN
GXY=(DISP(2)-DISP(5))/EL*(DISP(3)+DISP(6))/2
IF (INC4PRO.EQ.1.AND.IPRIT.EQ.0) GTP(I)=STA(I,NL+4)+GXY
IF (INC4PRO.EQ.1.AND.IPRIT.EQ.1) GTP(I)=STA(I,NL+4)
STST(I,NL+4)=GXY
STA(I,NL+4)=STA(I,NL+4)+GXY
END IF
DO 60 J=1,4
K=J+4
STANEX=DABS(STSB(I,J))
STANAX=DABS(STRB(I,K))
IF (STANEX.GT.STANAX) STSB(I,K)=STSB(I,J)
60 CONTINUE
10 CONTINUE
RETURN
END
C*****
SUENROUTINE LVECTR(NCL,NEL,STST,NS2,CALL,NS3,Y,NL,NCL,DIM,
* LCOMP,IATYPE,IGMAT,IEL,ICRACK,STRE,AREA,
* STEEL,INCLUD,CASST,CABLE,YCABLE,NMOD,
* NOMPLO,X,NVAR,0)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION DCL(NMOD,3),STST(NEL,NL2),STEEL(NEL,6),CALL(NEL,NS3),
* Y(NL,3),DIM(NEL,4),IEL(NEL,1),STRE(NEL,NS3),
* AREA(NEL,N),ICRACK(NEL,NL),CASST(NEL),CABLE(NEL,7),
* YCABLE(NMOD),X(NMOD,2),NVAR(NMOD,3),0(1)
DO 5 I=1,NMOD
DO 6 J=1,3
BCI(I,J)=0
5 CONTINUE
6 CONTINUE

```

```

DO 10 NE=1,NEL
FM=0
FM=0
ITYPE=IEL(NE,3)
CALL LAYER(DIM,ICOMP,IATYPE,IGMAT,ITYPE,NEL,NE,Y,TH,WGL,NL)
IF (ITYPE.EQ.1) GO TO 100
IF (ICOMP.EQ.0) LIM=NGL
IF (ICOMP.EQ.1) LIM=NL
DO 20 L=1,LIM
IF (EALL(NE,L).LT.0) THEN
ENCD=0
ELSE
ENCD=EALL(NE,L)
END IF
IF (ICRACK(NE,L).EQ.0) THEN
IF (STRE(NE,L).GE.0) GO TO 20
END IF
FM=FM+STRT(NE,L)*ENOD*Y(L,2)
FM=FM+STRT(NE,L)*ENOD*Y(L,2)*(AREA(NE,1)-Y(L,1))
20 CONTINUE
IF (ICOMP.EQ.0) LIM=2
IF (ICOMP.EQ.1) LIM=1
DO 30 K=LIM,1
J=2*K-1
FM=FM+STRT(NE,NL*K)*EALL(NE,NL*K)*STEEL(NE,J)
FM=FM+STRT(NE,NL*K)*EALL(NE,NL*K)*STEEL(NE,J)*
(AREA(NE,1)-STEEL(NE,J*1))
30 CONTINUE
GO TO 100
100 IF (ICOMP.EQ.0) GO TO 10
LIE=NGL+1
DO 40 L=LIM,NL
IF (EALL(NE,L).LT.0) THEN
ENCD=0
ELSE
ENCD=EALL(NE,L)
END IF
IF (ICRACK(NE,L).EQ.0) THEN
IF (STRE(NE,L).GE.0) GO TO 40
END IF
FM=FM+STRT(NE,L)*ENOD*Y(L,2)
40 CONTINUE
FM=FM+STRT(NE,NL*1)*EALL(NE,NL*1)*STEEL(NE,1)
200 CONTINUE
N1=IEL(NE,1)
N2=IEL(NE,2)
IF (INCLUD.EQ.1.AND.ITYPE.EQ.0) THEN
ALPHA=CABLE(NE,1)
F=CABSST(N1)*CABLE(NE,7)*CABLE(NE,4)
ARM=AREA(NE,1)-(YCABLE(N1)*YCABLE(N2))/2
FM=FM+F*DCOS(ALPHA)*ARM
END IF
AL=X(N2,1)-X(N1,1)
IF (IEL(N1,3).EQ.0) THEN
FM1=FM+FA*(AREA(NE,1)+X(N1,2))
FM2=FM+FM*(AREA(NE,1)+X(N2,2))
ELSE
FM1=FM*(DIM(NE,3)+X(N1,2))
FM2=FM*(DIM(NE,4)+X(N2,2))
END IF

```

```

2972 ECL(N1,1)=DCL(N1,1)-FM
2973 DCL(N1,3)=DCL(N1,3)+FM1
2974 DCL(N2,1)=DCL(N2,1)+FM
2975 DCL(N2,3)=DCL(N2,3)-FM2
2976 10 CONTINUE
2977 DC 50 I=1,NMOD
2978 DO 60 J=1,3
2979 JA=NVAR(I,J)
2980 IF (JA.NE.0) E(JA)=DCL(I,J)
2981 60 CONTINUE
2982 50 CONTINUE
2983 RETURN
2984 ENF
2985 C*****
2986
2987 SUBROUTINE FORSCT(NEL,FORCE,NS1,EALL,NS3,Y,NL,WGL,DIM,
2988 * ICOMP,IATYPE,IGMAT,IEL,ICRACK,STRE,AREA,STEEL,STA,
2989 * INCLUD,FINCAB,CABLE,YCABLE,NMOD,GTP,NOWPRO)
2990 C*****
2991 IMPLICIT REAL*8(A-H,O-Z)
2992 DIMENSION FCBC(NEL,3),STEEL(NEL,6),EALL(NEL,NS3),GTP(NEL)
2993 *,Y(NL,3),DIM(NEL,8),IEL(NEL,3),STRE(NEL,NS3),AREA(NEL,8)
2994 *,ICRACK(NEL,NL),STA(NEL,NS1),FINCAB(NEL,3),CABLE(NEL,7),
2995 * YCABLE(NMOD)
2996 C
2997 C
2998 C
2999 C
3000 C
3001 C
3002 C
3003 C
3004 C
3005 C
3006 C
3007 C
3008 C
3009 C
3010 C
3011 C
3012 C
3013 C
3014 C
3015 C
3016 C
3017 C
3018 C
3019 C
3020 C
3021 C
3022 C
3023 C
3024 C
3025 C
3026 C
3027 C
3028 C
3029 C
3030 C
3031 C
3032 ECL(N1,1)=DCL(N1,1)-FM
3033 DCL(N1,3)=DCL(N1,3)+FM1
3034 DCL(N2,1)=DCL(N2,1)+FM
3035 DCL(N2,3)=DCL(N2,3)-FM2
3036 10 CONTINUE
3037 DC 50 I=1,NMOD
3038 DO 60 J=1,3
3039 JA=NVAR(I,J)
3040 IF (JA.NE.0) E(JA)=DCL(I,J)
3041 60 CONTINUE
3042 50 CONTINUE
3043 RETURN
3044 ENF
3045 C*****
3046
3047 SUBROUTINE FORSCT(NEL,FORCE,NS1,EALL,NS3,Y,NL,WGL,DIM,
3048 * ICOMP,IATYPE,IGMAT,IEL,ICRACK,STRE,AREA,STEEL,STA,
3049 * INCLUD,FINCAB,CABLE,YCABLE,NMOD,GTP,NOWPRO)
3050 C*****
3051 IMPLICIT REAL*8(A-H,O-Z)
3052 DIMENSION FCBC(NEL,3),STEEL(NEL,6),EALL(NEL,NS3),GTP(NEL)
3053 *,Y(NL,3),DIM(NEL,8),IEL(NEL,3),STRE(NEL,NS3),AREA(NEL,8)
3054 *,ICRACK(NEL,NL),STA(NEL,NS1),FINCAB(NEL,3),CABLE(NEL,7),
3055 * YCABLE(NMOD)
3056 C
3057 C
3058 C
3059 C
3060 C
3061 C
3062 C
3063 C
3064 C
3065 C
3066 C
3067 C
3068 C
3069 C
3070 C
3071 C
3072 C
3073 C
3074 C
3075 C
3076 C
3077 C
3078 C
3079 C
3080 C
3081 C
3082 C
3083 C
3084 C
3085 C
3086 C
3087 C
3088 C
3089 C
3090 C

```

```

      PQ=PQ+STA(NE,NS1)*G*Y(L,2)
20 CONTINUE
      IF (ICOMP.EQ.0) LIM=2
      IF (ICOMP.EQ.1) LIM=1
      DO 30 K=LIM,3
        J=K-1
        FM=FM+STRE(NE,NL+K)*STEEL(NE,J)
        FN=FN+STRE(NE,NL+K)*STEEL(NE,J)*
          * (AREA(NE,1)-STEEL(NE,J+1))
        G=EALL(NE,NL+K)/2/(1+V)
        PQ=PQ+STA(NE,NS1)*G*STEEL(NE,J)
30 CONTINUE
      GO TO 200
100 IF (ICOMP.EQ.0) THEN
      DO 101 JK=1,3
        FORCE(NE,JK)=0
101 CONTINUE
      GO TO 10
      ENC IF
      LIM=NJL+1
      DO 40 L=LIM,NL
        IF (ICHECK(NE,L).EQ.0) THEN
          IF (STRE(NE,L).GE.0) GO TO 40
          ENC IF
          FM=FM+STRE(NE,L)*Y(L,2)
40 CONTINUE
          FN=FN+STRE(NE,NL+1)*STEEL(NE,1)
          FM=0
          PQ=0
200 CONTINUE
          IF (INCLUD.EQ.1) THEN
            IF (ITYPE.EQ.0) THEN
              N1=IEL(NE,1)
              N2=IEL(NE,2)
              ALPHA=CABLE(N2,1)
              F=CABLE(NE,3)
              ARM=AREA(NE,1)-(YCABLE(N1)+YCABLE(N2))/2
              FN=FN+F*DCOS(ALPHA)*ARM
              G=CABLE(NE,7)/2/(1+V)
              FJ=FJ+STA(NE,NS1)-GTP(NE)*G*CABLE(NE,8)
              FM=FM+F
            ENC IF
          ENC IF
          FORCE(NE,1)=FM
          FORCE(NE,2)=FN
          FORCE(NE,3)=FJ
10 CONTINUE
      NEXT NS
      ENC
C.....
      SUBROUTINE CHEKEQ(FORCE,CMP,NEL,ISTOP,IEL,DCL,DIM,
        * B,AREA,X,NMOD,NVAR,NODE1,NDISP,FINCAB,INCLUD,RC)
C.....
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION FORCE(NEL,3),CMP(NODE1,3),B(1),
        * IEL(NEL,3),AREA(NEL,6),X(NMOD,2),DCL(NMOD,3),
        * NVAR(NMOD,3),FINCAB(NEL,3),DIM(NEL,8)
      DO 300 J=1,NMOD
        DO 400 K=1,3

```

```

3091'      DCL(J,K)=0
3092' 400 CONTINUE
3093' 300 CONTINUE
3094'      DO 30 I=1,NEL
3095'        N1=IEL(I,1)
3096'        N2=IEL(I,2)
3097'        AL=X(N2,1)-X(N1,1)
3098'        FX=-FORCE(I,1)
3099'        FY=FORCE(I,3)
3100'        IF (IEL(I,3).EQ.0) THEN
3101'          FM1=FORCE(I,2)+FORCE(I,1)*X(N1,2)/X(N1,2)+FORCE(I,3)*AL/2
3102'          FM2=-FORCE(I,2)+FORCE(I,1)*X(N2,2)/X(N2,2)-FORCE(I,3)*AL/2
3103'          ELSE
3104'            FM1=FORCE(I,1)*X(N1,2)/X(N1,2)+X(N1,2)
3105'            FM2=FORCE(I,1)*X(N2,2)/X(N2,2)+X(N2,2)
3106'          ENC IF
3107'          DCL(N1,1)=DCL(N1,1)+FX
3108'          DCL(N1,2)=DCL(N1,2)+FY
3109'          DCL(N1,3)=DCL(N1,3)+FM1
3110'          DCL(N2,1)=DCL(N2,1)+FX
3111'          DCL(N2,2)=DCL(N2,2)+FY
3112'          DCL(N2,3)=DCL(N2,3)+FM2
3113'          IF (INCLUD.EQ.1) THEN
3114'            FORCE(I,1)=FORCE(I,1)-FINCAB(I,1)
3115'            FORCE(I,2)=FORCE(I,2)-FINCAB(I,2)
3116'            FORCE(I,3)=FORCE(I,3)-FINCAB(I,3)
3117'          ENC IF
3118' 30 CONTINUE
3119'      DO 50 I=1,NMOD
3120'        DO 60 J=1,3
3121'          JA=NVAR(I,J)
3122'          IF (JA.NE.0) B(JA)=DCL(I,JA)
3123' 60 CONTINUE
3124' 50 CONTINUE
3125' C      ASSUMED APPROXIMATION LIMITS
3126'      APROX=1
3127'      SMALL=1
3128' C
3129'      ISICP=1
3130'      ANTL=(100-APROX)/100
3131'      POSL=(100+APROX)/100
3132'      DO 10 J=1,NMOD
3133'        DO 20 K=1,3
3134'          I=NVAR(J,K)
3135'          IF (I.EQ.0) GO TO 20
3136'          IF (K.EQ.1.AND.NVAR(J,2).EQ.0) THEN
3137'            IF (DCGT(I).GT.0) GO TO 20
3138'          ENC IF
3139'          IF (ISTOP.EQ.0) GO TO 200
3140'          IF (DABS(CMP(I,2)).LT.SMALL) THEN
3141'            IF (DABS(B(I)).GT.SMALL) ISTOP=0
3142'          ELSE
3143'            IF (DABS(B(I)).LT.1.E-75) THEN
3144'              ISTOP=0
3145'            GO TO 200
3146'          ENC IF
3147'          RATE=B(I)/CMP(I,2)
3148'          IF (RATE.LT.POSL) ISTOP=C
3149'          IF (RATE.LT.ANTL) ISTOP=0
3150'          ENC IF
3151'
3152'
3153'
3154'
3155'
3156'
3157'
3158'
3159'
3160'
3161'
3162'
3163'
3164'
3165'
3166'
3167'
3168'
3169'
3170'
3171'
3172'
3173'
3174'
3175'
3176'
3177'
3178'
3179'
3180'
3181'
3182'
3183'
3184'
3185'
3186'
3187'
3188'
3189'
3190'
3191'
3192'
3193'
3194'
3195'
3196'
3197'
3198'
3199'
3200'
3201'
3202'
3203'
3204'
3205'
3206'
3207'
3208'
3209'

```



```

20 CONTINUE
10 CONTINUE
200 IF (ISTOP.EQ.1) GO TO 100
DO 40 I=1,NDISP
  B(I)=CWF(1,2)-B(I)
40 CONTINUE
100 CONTINUE
RETURN
END
C*****
      SUBROUTINE STRESS(E,STRE,NEL,NS3,IELD,NS4,EPEM,NL,STA,
+      STST,ICSTR,SREAL,NS1,NS2,EALL,IGHAT,NGL,
+      STEEL,ICOMP,ICRACK,IEL,ISSC,FINISH,NWSTP,T)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION E(4,6),STRE(NEL,NS3),IELD(NEL,NS4),EPEM(NEL,NL),
+      STA(NEL,NS1),STST(NEL,NS2),CALL(NEL,NS3),IEL(NEL,3),
+      STEEL(NEL,6),ICRACK(NEL,NL),T(6)
      DO 10 NE=1,NEL
        IF (IEL(NE,3).EQ.1) GO TO 100
        DO 20 L=1,3JL
          WHICH=3
          ET=STA(NE,L)
          ES=STST(NE,L)
          SIG=STRE(NE,L)
          ELAST=EALL(NE,L)
          IF (IGHAT.EQ.0) THEN
            YLD=IELD(NE,L)
            CALL RSTEEL(E,ET,ES,SIG,ELAST,YLD,WHICH,FINISH,NWSTP)
            IELD(NE,L)=YLD
          ELSE
            EPLAST=EPEM(NE,L)
            CRK=ICRACK(NE,L)
            CALL CONCRE(E,WHICH,ET,ES,ELAST,SIG,EPLAST,CRK,ISSC,FINISH,
+            NWSTP,ICSTR,T,SREAL)
            EPEM(NE,L)=EPLAST
            ICRACK(NE,L)=CRK
          END IF
          STRE(NE,L)=SIG
          EALL(NE,L)=ELAST
20 CONTINUE
        IF (IGHAT.EQ.0) GO TO 100
        DO 30 J=1,2
          IF (STEEL(NE,2*J+1).EQ.0) GO TO 30
          L=NEL+1+J
          ET=STA(NE,L)
          ES=STST(NE,L)
          SIG=STRE(NE,L)
          ELAST=EALL(NE,L)
          YLD=IELD(NE,NEL+1+J)
          WHICH=2
          CALL RSTEEL(E,ET,ES,SIG,ELAST,YLD,WHICH,FINISH,NWSTP)
          STRE(NE,L)=SIG
          EALL(NE,L)=ELAST
          IELD(NE,NEL+1+J)=YLD
30 CONTINUE
100 IF (ICOMP.EQ.0) GO TO 10
    LIN=NEL+1
    DO 40 I=LIN,NL

```

```

3210 WHICH=4
3211 ET=STA(NE,L)
3212 ES=STST(NE,L)
3213 ELAST=EALL(NE,L)
3214 SIG=STRE(NE,L)
3215 EPLAST=EPEM(NE,L)
3216 CRK=ICRACK(NE,L)
3217 CALL CONCRE(E,WHICH,ET,ES,ELAST,SIG,EPLAST,CRK,ISSC,FINISH,
+      NWSTP,ICSTR,T,SREAL)
3218 EALL(NE,L)=ELAST
3219 STRE(NE,L)=SIG
3220 EPEM(NE,L)=EPLAST
3221 ICRACK(NE,L)=CRK
3222 40 CONTINUE
3223 IF (STEEL(NE,1).EQ.0) GO TO 10
3224 ET=STA(NE,NEL+1)
3225 ES=STST(NE,NEL+1)
3226 SIG=STRE(NE,NEL+1)
3227 ELAST=EALL(NE,NEL+1)
3228 YLD=IELD(NE,NEL+1)
3229 WHICH=2
3230 CALL RSTEEL(E,ET,ES,SIG,ELAST,YLD,WHICH,FINISH,NWSTP)
3231 STRE(NE,NEL+1)=SIG
3232 EALL(NE,NEL+1)=ELAST
3233 IELD(NE,NEL+1)=YLD
3234 10 CONTINUE
3235 RETURN
3236 END
C*****
      SUBROUTINE LAYER(DID,ICOMP,IATYPE,IGHAT,TYPE,NEL,EN,Y,T,NGL,NL)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION DID(NEL,8),Y(NL,3)
      INTEGER EN,TYPE
      DO 10 I=1,NL
        DO 20 J=1,3
          Y(I,J)=0
20 CONTINUE
10 CONTINUE
      TH=0
      IF (TYPE.EQ.1) GO TO 100
      IF (IGHAT.EQ.0.AND.IATYPE.EQ.1) THEN
        A=CIA(EN,3)
        TH=CIA(EN,4)
        TT=CIA(EN,6)
        WT=CIA(EN,7)
        BT=CIA(EN,8)
        Y(1,1)=BT*1/NGL
        Y(1,2)=(A-(TH-TT-BT)*WT)/(TT*BT)*BT/(NGL/6)
        Y(1,3)=Y(1,2)/BT/(NGL/6)
        DL=BT*6/NGL
        LIN=NEL/6
        DO 25 I=2,LIN
          Y(I,1)=Y(1,1)+DL
          Y(I,2)=Y(1,2)
          Y(I,3)=Y(1,3)
25 CONTINUE
        DL=(TH-TT-BT)/(NGL*2/3)
        Y(NGL/6+1,1)=BT+DL/2

```



```

Y(NGL/6+1,2)=DL*WT
Y(NGL/6+1,3)=WT
LIM1=NGL/6+2
LIMF=NGL/5+6
DO 30 I=LIM1,LIMF
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=DL*WT
Y(I,3)=WT
30 CONTINUE
Y(NGL/6+1,1)=(TH-TT)+TT*3/NGL
Y(NGL/6+1,2)=Y(I,2)*TT/BT
Y(NGL/6+1,3)=Y(I,3)
DL=TT*6/NGL
LIF=5*NGL/6+2
DO 35 I=LIM,NGL
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=Y(I-1,2)
Y(I,3)=Y(I-1,3)
35 CONTINUE
ELSE
IF (IATYPE.EQ.0) THEN
B=DIM(EN,3)
TH=DIM(EN,4)
DL=(TH*3)/(NGL*4)
Y(I,1)=DL/2
Y(I,2)=DL*8
Y(I,3)=8
LIM=NGL/3
DO 40 I=2,LIM
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=DL*8
Y(I,3)=8
40 CONTINUE
Y(LIM+1,1)=Y(LIM,1)+DL*1.5
Y(LIM+1,2)=DL*2*8
Y(LIM+1,3)=8
LIM1=LIM+2
LIMF=NGL/2
DO 41 I=LIM1,LIMF
Y(I,1)=Y(I-1,1)+DL*2
Y(I,2)=DL*2*8
Y(I,3)=8
41 CONTINUE
LIF=LIMF+1
DO 42 I=LIM,NGL
J=NGL-I+1
Y(I,1)=TH-Y(J,1)
Y(I,2)=Y(J,2)
Y(I,3)=8
42 CONTINUE
ELSE
TH=DIM(EN,3)
TT=DIM(EN,4)
WB=DIM(EN,5)
WT=DIM(EN,6)
EB=DIM(EN,7)
BT=DIM(EN,8)
TH=11*WT+BT
DL=BT/(NGL/4)
Y(I,1)=DL/2

```

3328
3329
3330
3331
3332
3333
3334
3335
3336
3337
3338
3339
3340
3341
3342
3343
3344
3345
3346
3347
3348
3349
3350
3351
3352
3353
3354
3355
3356
3357
3358
3359
3360
3361
3362
3363
3364
3365
3366
3367
3368
3369
3370
3371
3372
3373
3374
3375
3376
3377
3378
3379
3380
3381
3382
3383
3384
3385
3386
3387

```

Y(I,2)=80*DL
Y(I,3)=88
LIM=NGL/4
DO 45 I=2,LIM
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=Y(I,2)
Y(I,3)=Y(I,3)
45 CONTINUE
DL=WT/(NGL/2)
Y(NGL/4+1,1)=BT+DL/2
Y(NGL/4+1,2)=DL*WB
Y(NGL/4+1,3)=WB
LIM1=NGL/4+2
LIM2=3*NGL/4
DO 50 I=LIM1,LIM2
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=Y(NGL/4+1,2)
Y(I,3)=Y(NGL/4+1,3)
50 CONTINUE
DL=TT/(NGL/4)
Y(3*NGL/4+1,1)=BT+WT+DL/2
Y(3*NGL/4+1,2)=TB*DL
Y(3*NGL/4+1,3)=TB
LIF=3*NGL/4+2
DO 55 I=LIM,NGL
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=Y(3*NGL/4+1,2)
Y(I,3)=Y(3*NGL/4+1,3)
55 CONTINUE
END IF
END IF
100 IF (ICOMP.EQ.1) THEN
DL=DIM(EN,2)/(NL-NGL)
Y(NGL+1,1)=TH+DL/2
Y(NGL+1,2)=DL*DIM(EN,1)
Y(NGL+1,3)=DIM(EN,1)
LIM=NGL+2
DO 60 I=LIM,NL
Y(I,1)=Y(I-1,1)+DL
Y(I,2)=Y(NGL+1,2)
Y(I,3)=Y(NGL+1,3)
60 CONTINUE
END IF
RETURN
END
C .....
SUBROUTINE NUSTIF(NHOD,NNDISP,NBAND,NEL,IEL,
* KVAR,X,ST,JC,DID,AREA,YCABLE,CABL2,INCLUD,NODR)
C .....
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION IEL(NEL,3),ELST(6,6),KVAR(NNOD,3),ST(NNDISP,NBAND),
*X(NHOD,3),DID(NEL,3),AREA(NEL,3),YCABLE(NNOD),CABLE(NEL,7)
INITGEF EN,CISP
DO 700 I=1,NNDISP
DO 600 J=1,NBAND
ST(I,J)=0
600 CONTINUE
700 CONTINUE
DO 500 I=1,NEL

```

3388
3389
3390
3391
3392
3393
3394
3395
3396
3397
3398
3399
3400
3401
3402
3403
3404
3405
3406
3407
3408
3409
3410
3411
3412
3413
3414
3415
3416
3417
3418
3419
3420
3421
3422
3423
3424
3425
3426
3427
3428
3429
3430
3431
3432
3433
3434
3435
3436
3437
3438
3439
3440
3441
3442
3443
3444
3445
3446

```

      EM=11
      CALL ELSTIF(X,ELST,MMOD,WEL,IEL,EW,DIN,AREA,YCABLE,
      *      CABLE,INCLUD)
      DO 400 J1=1,2
      MODE1=IEL(I1,J1)
      DO 300 K1=1,3
      IVAR1=KVAR(MODE1,K1)
      IF (IVAR1.EQ.0) GO TO 300
      JK1=3*(J1-1)+K1
      DO 200 J2=J1,2
      MODE2=IEL(I1,J2)
      JK2=1
      IF (J2.EQ.J1) JK=K1
      DO 150 K2=JK,3
      IVAR2=KVAR(MODE2,K2)
      IF (IVAR2.EQ.0) GO TO 150
      JK2=3*(J2-1)+K2
      IV1=IVAR1
      IV2=IVAR2
      IF (IVAR2.GE.IVAR1) GO TO 100
      IV1=IVAR2
      IV2=IVAR1
100  IV2=IV2-IV1+1
      ST (IV1,IV2)=ST (IV1,IV2)+ELST (JK1,JK2)
150  CONTINUE
200  CONTINUE
300  CONTINUE
400  CONTINUE
500  CONTINUE
      ADD BEARING COEFFICIENT
      IF (BC.EQ.0) THEN
      GO TO 900
      END IF
      DO 600 I=1,NMOD
      IF (KVAR(I,2).EQ.0) THEN
      IF (1.EQ.MMOD) GO TO 800
      IF (KVAR(I,1).GT.0) THEN
      DISP=KVAR(I,1)
      ST (DISP,I)=ST (DISP,I)+BC
      END IF
      END IF
800  CONTINUE
900  CONTINUE
      RETURN
      END
      C*****
      SUBROUTINE FRACTM(NWSTP,AK12,DU,P2,P1,NNDISP,DENOM,ALPHA,
      *      SALPHA,AK22,DRIVIL)
      C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION AK12(1),DU(1),P1(1)
      IF (NWSTP.EQ.1) THEN
      DEACH=0
      DO 10 I=1,NNDISP
      DENOM=DENOM+AK12(I)*P1(I)
10  CONTINUE
      DEACH=F2-DENOM
      A=AK22*DRIVIL
      ELSE

```

```

3447  A=-P2
3448  END IF
3449  E=C
3450  DO 20 I=1,NNDISP
3451  B=B+AK12(I)*DU(I)
3452  20 CONTINUE
3453  ALPHA=(B+A)/DENOM
3454  SALPHA=SALPHA+ALPHA
3455  RETURN
3456  END
3457  C*****
3458  SUBROUTINE SPLIT(NEAND,NVAR,NOCR,NCISP,ST,MMOD,AK12,AK22)
3459  C*****
3460  IMPLICIT REAL*8(A-H,O-Z)
3461  DIMENSION ST(SDISP,NVAR),NVAR(NMOD,3),AK12(1)
3462  DO 10 I=1,NNDISP
3463  AK12(I)=0
3464  10 CONTINUE
3465  IDISP=NVAR(NOCR,2)
3466  AK22=ST(IDISP,1)
3467  IDISP1=IDISP-1
3468  IF (IDISP.GE.NDAND) THEN
3469  IBC=IDISP-NEAND+1
3470  ICCL=NEAND
3471  ELSE
3472  IBC=1
3473  ICCL=IDISP
3474  END IF
3475  DO 20 I=1,NMOD
3476  AK12(I)=ST(I,ICOL)
3477  ICCL=ICCL-1
3478  20 CONTINUE
3479  DO 30 ICOL=2,NEAND
3480  IDISP1=IDISP1+1
3481  AK12(IDISP1)=ST(IDISP,ICOL)
3482  30 CONTINUE
3483  RETURN
3484  END
3485  C*****
3486  SUBROUTINE CONCRC(E,WHICH,ET,ES,ELAST,SIG,EPLAST,CBK,ISSC,
3487  *      FINISH,NWSTP,ICSTR,T,SREAL)
3488  C*****
3489  IMPLICIT REAL*8(A-H,O-Z)
3490  DIMENSION E(4,6),T(6)
3491  C      CONCRETE AGE CORRECTION
3492  TO=T(WHICH-1)+28
3493  AGE=T(1)-TC
3494  A=2.00
3495  B=C.928571429
3496  FACT=AGE/(A+B*AGE)
3497  C
3498  ZO=E(WHICH,1)*DSQRT(FACT)
3499  ERU=-E(WHICH,6)
3500  ER=L(WHICH,3)
3501  TRS=LO*ER
3502  IF (ET.LE.ERU) FINISH=4
3503  SCV=0
3504  ECV=0
3505
3506
3507
3508
3509
3510
3511
3512
3513
3514
3515
3516
3517
3518
3519
3520
3521
3522
3523
3524
3525
3526
3527
3528
3529
3530
3531
3532
3533
3534
3535
3536
3537
3538
3539
3540
3541
3542
3543
3544
3545
3546
3547
3548
3549
3550
3551
3552
3553
3554
3555
3556
3557
3558
3559
3560
3561
3562
3563

```

```

IF (ISSC.EQ.0) THEN
CALL HCGMES(E,ET,WHICH,SCV,ECV,FACT)
END IF
IF (ISSC.EQ.1) THEN
CALL BILINR(E,ET,WHICH,SCV,ECV,FACT)
END IF
IF (CRK.WE.0) THEN
IF (WSTP.EQ.1.AND.ES.GT.0) ELAST=EO
SIG=SIG+ELAST*ES
IF (ISSC.EQ.1.AND.ELAST.GT.0) ELAST=EO
IF (ISSC.EQ.0.AND.ICSTR.EQ.1) THEN
CALL HOGSTR(E,WHICH,SIG,ELAST,FACT,ES)
END IF
IF (SIG.LT.SCV.AND.ICSTR.EQ.0) THEN
SIG=SCV
ELAST=ECV
END IF
IF (ET.GE.ER.AND.ICSTR.EQ.0) THEN
SIG=0
ELAST=EO
EPLAST=ER
CRK=0
END IF
IF (SIG.GE.TRS.AND.SREAL.EQ.1) THEN
SIG=0
ELAST=EO
EPLAST=ET
CRK=0
END IF
ELSE
IF (E1.L1.EPLAST) THEN
ELAST=EO
SIG=SIG+ELAST*ES
IF (SIG.LT.SCV.AND.ICSTR.EQ.0) THEN
SIG=SCV
ELAST=ECV
END IF
IF (SIG.GT.0) SIG=0
ELSE
SIG=0
ELAST=0
END IF
END IF
IF (ICSTR.EQ.1) THEN
IF (SIG.LT.1.AND.SIG.GT.-1) SIG=0
END IF
RETURN
END

```

```

C.....
SUBROUTINE HCGMES(E,EPS,WHICH,SIG,ELAST,FACT)
C.....
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION E(4,6)
S11=0.85*E(WHICH,2)*FACT
EO=E(WHICH,1)*DSQRT(FACT)
EPC=2*S11/EO
EU=E(WHICH,6)
IF (EPS.GE.0) THEN
SIG=EO*EPS

```

```

3564 ELAST=EO
3565 ELSE
3566 IF (DABS(EPS)-LE.EPC) THEN
3567 RAT=EAES(EPS)/EPO
3568 SIG=-S11*RAT*(2-RAT)
3569 ELAST=EO*(1-RAT)
3570 ELSE
3571 RAT=(DABS(EPS)-EPO)/(EU-EPC)
3572 SIG=-S11*(1-0.15*RAT)
3573 ELAST=(-0.15*S11)/(2U-EPC)
3574 END IF
3575 END IF
3576 RETURN
3577 END
3578
3579 C.....
3580 SUBROUTINE HOGSTR(E,WHICH,SIG,ELAST,FACT,ES)
3581 C.....
3582 IMPLICIT REAL*8(A-H,O-Z)
3583 DIMENSION E(4,6)
3584 S11=0.85*E(WHICH,2)
3585 EO=E(WHICH,1)
3586 EU=E(WHICH,6)
3587 EPC=2*S11/EO
3588 IF (EABS(SIG).GT.S11) SIG=-S11
3589 IF (ELAST.GT.0) THEN
3590 ELAST=EO*DSQRT(1+SIG/S11)*DSQRT(FACT)
3591 GO TO 100
3592 END IF
3593 IF (ELAST.EQ.0.AND.ES.LT.0) THEN
3594 ELAST=(-0.15*S11)/(EU-EPC)
3595 SIG=SIG+ELAST*ES
3596 GO TO 100
3597 END IF
3598 IF (ELAST.LT.0) ELAST=(-0.15*S11)/(EU-EPO)
3599 100 CONTINUE
3600 RETURN
3601 END
3602 C.....
3603
3604 SUBROUTINE BILINR(E,EPS,WHICH,SIG,ELAST,FACT)
3605 C.....
3606 IMPLICIT REAL*8(A-H,O-Z)
3607 DIMENSION E(4,6)
3608 EO=E(WHICH,1)*DSQRT(FACT)
3609 FCI=E(WHICH,2)*FACT
3610 EPC=FCI/EO
3611 IF (EPS.GE.EPC) THEN
3612 SIG=EO*EPS
3613 ELAST=EO
3614 ELSE
3615 SIG=-FCI
3616 ELAST=C
3617 END IF
3618 RETURN
3619 END
3620 C.....
3621
3622 SUBROUTINE HSTEEL(E,ET,E3,SIG,ELAST,YLD,WHICH,FINISH,WSTP)
3623 C.....
3624
3625
3626
3627
3628
3629
3630
3631
3632
3633
3634
3635
3636
3637
3638
3639
3640
3641
3642
3643
3644
3645
3646
3647
3648
3649
3650
3651
3652
3653
3654
3655
3656
3657
3658
3659
3660
3661
3662
3663
3664
3665
3666
3667
3668
3669
3670
3671
3672
3673
3674
3675
3676
3677
3678
3679

```



```

IMPLICIT REAL*8(A-H,O-Z)
DIMENSION E(4,6)
SY=E(WHICH,1)*E(WHICH,2)
EO=E(WHICH,1)
EU=E(WHICH,6)
IF(DABS(ET).GE.EU) FINISH=3
IF(DABS(SIG).LT.SY) THEN
SIG=SIG+EO*ES
ELAST=EO
ELSE
IF(NWSTP.E..1) THEN
SIGNAL=SIG/DABS(SIG)
IF(SIGNAL*ES.LT.0) THEN
SIG=SY+EO*ES
ELAST=0
END IF
END IF
END IF
IF(DABS(SIG).GE.SY) THEN
SIGNAL=SIG/DABS(SIG)
SIG=SIGNAL*SY
ELAST=0
YLC=0
END IF
RETURN
END
C*****
SUBROUTINE ACRACK(NEL,AREA,STA,NS1,NS3,EALL,DIM,IATYPE,IGNAT,
* NGL,NL,IEL,ICOMP,ICRACK,IALPHA,ERG,ERD,Y,ICSTR)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION AREA(NEL,8),STA(NEL,NS1),DIM(NEL,8),IEL(NEL,3),
* Y(NEL,3),ICRACK(NEL,NL),IALPHA(NEL,NL),EALL(NEL,NS3)
DO 10 NE=1,NEL
ITYPE=IEL(NE,3)
IF(ITYPE.EQ.0) THEN
CHI=(AREA(NE,4)-AREA(NE,2)*AREA(NE,1))*2)
IF(CHI.GT.0.00001.AND.STA(NE,NS1).GT.1.E-15) THEN
CGAMA=STA(NE,NS1)*AREA(NE,8)/CHI
ELSE
CGAMA=0
END IF
END IF
CALL LAYER(DIM,ICOMP,IATYPE,IGNAT,ITYPE,NEL,NE,Y,TH,NGL,NL)
IF(ITYPE.EQ.0) THEN
SG=0
IF(ICOMP.EQ.0) LIN=NGL
IF(ICOMP.EQ.1) LIN=NL
DO 20 JL=1,LIN
L=LIN+1-JL
STAN=STA(NEL,L)
IF(STA(NE,L).LT.1.E-15) STAN=0
SG=SG+Y(L,2)*(Y(L,1)-AREA(NE,1))
IF(ICRACK(NE,L).EQ.0) GO TO 20
IF(IGNAT.EQ.0) THEN
IF(L.EE.NGL) GO TO 20
END IF
V=0.2
IF(EALL(NE,L).LE.0) THEN

```

3680
3681
3682
3683
3684
3685
3686
3687
3688
3689
3690
3691
3692
3693
3694
3695
3696
3697
3698
3699
3700
3701
3702
3703
3704
3705
3706
3707
3708
3709
3710
3711
3712
3713
3714
3715
3716
3717
3718
3719
3720
3721
3722
3723
3724
3725
3726
3727
3728
3729
3730
3731
3732
3733
3734
3735
3736
3737
3738

```

GXY=0
ELSE
GXY=CGAMA*SG*2*(1+V)/(Y(L,3)*EALL(NE,L))
END IF
RAD=STAN**2+GXY**2
A=SIAN
SG=DSQRT(RAD)
SP=(A+SG)/2
IF(L.LE.NGL) ER=ERG
IF(L.GT.NGL) ER=ERD
IF(EP.GE.ER) THEN
IF(STA(NE,L).GT.0) THEN
IF(ICSTR.EQ.0) ICRACK(NE,L)=0
D=GXY/(STAN*(1+V))
IALPHA(NE,L)=DATAN(B)*180/(2*3.141592654)
ELSE
ICRACK(NE,L)=-1
END IF
END IF
20 CONTINUE
ELSE
LIB=NGL+1
DO 30 L=LIB,NL
IF(STA(NE,L).GE.ERD.AND.ICSTR.EQ.0) ICRACK(NE,L)=0
30 CONTINUE
END IF
10 CONTINUE
RETURN
END
C*****
SUBROUTINE CRACKS(STRB,DIM,NEL,IGNAT,CRACK,ERG,ERD,ICOMP,Y,
* IEL,NMOD,ICRACK,NGL,NL)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION STRB(NEL,8),DIM(NEL,6),CRACK(NEL,8),CRACK(8),
* X(NMOD,2),IEL(NEL,3),ICRACK(NEL,NL)
DO 10 I=1,NEL
N1=IEL(I,1)
N2=IEL(I,2)
AL=X(N2,1)-X(N1,1)
DO 6 J=1,8
CRACK(J)=0
6 CONTINUE
IF(IGNAT.EQ.0) GO TO 100
HG=DIM(1,4)*DIM(1,6)+DIM(1,8)
IF(STRB(I,1).GE.ERG.AND.ICRACK(I,1).EQ.0) THEN
IF(STRB(I,2).GE.ERG) THEN
WRITE(3,1000)
1000 FORMAT(//,5('*****GIRDER FAILURE*****'),//)
END IF
CRACK(1)=(STRB(I,1)-ERG)*(STRB(I,1)-STRB(I,2))
CRACK(5)=(STRB(I,1)-ERG)*AL
END IF
IF(STRB(I,2).GE.ERG.AND.ICRACK(I,NGL).EQ.0) THEN
CRACK(2)=(STRB(I,2)-ERG)*HG/(STRB(I,2)-STRB(I,1))
CRACK(6)=(STRB(I,2)-ERG)*AL
END IF
100 IF(ICOMP.EQ.1) THEN
ND=DIM(1,2)

```

3739
3740
3741
3742
3743
3744
3745
3746
3747
3748
3749
3750
3751
3752
3753
3754
3755
3756
3757
3758
3759
3760
3761
3762
3763
3764
3765
3766
3767
3768
3769
3770
3771
3772
3773
3774
3775
3776
3777
3778
3779
3780
3781
3782
3783
3784
3785
3786
3787
3788
3789
3790
3791
3792
3793
3794
3795
3796
3797


```

      IF (STRB(I,3) .GE. ERD .AND. ICRACK(I,NGL+1) .EQ. 0) THEN
C      IF (STRB(I,4) .GE. ERD) THEN
C      WHITE(1,2000)
C2000 FOSBAT(1,5)('*****DECK FAILURE*****'),(1)
C      ENCL IF
      CRAST(3) = (STRB(I,3) - ERD) * HD / (STRB(I,3) - STRB(I,4))
      CRAST(7) = (STRB(I,3) - ERD) * AL
      ENCL IF
      IF (STRB(I,4) .GE. ERD .AND. ICRACK(I,NL) .EQ. 0) THEN
      CRAST(4) = (STRB(I,4) - ERD) * HD / (STRB(I,4) - STRB(I,3))
      CRAST(6) = (STRB(I,4) - ERD) * AL
      ENCL IF
      ENCL IF
      DO 20 K=1,8
      IF (CRAST(K) .GT. CRACK(I,K)) CRACK(I,K) = CRAST(K)
20 CONTINUE
10 CONTINUE
      RETURN
      ENCL
C*****
      SUBROUTINE PROTEN(YCABLE,CLOAD,X,CABLE,IEL,NEL,NMOD,NOWPRO,
      * NPS,FSEGN,ELCMG,FM,FK,E,FINCAB)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION YCABLE(NMOD),CLOAD(NMOD,3),X(NMOD,2),CABLE(NEL,7),
      * FINCAB(NEL,3),IEL(NEL,3),FSEGN(10,5),ELONG(10,2),E(4,6)
      IF (NOWPRO .EQ. 1) GO TO 1000
      DO 40 I=1,NPS
      NE1=FSEGN(I,1)
      NE2=FSEGN(I,2)
      DO 45 J=NE1,NE2
      CABLE(J,3)=FSEGN(I,4)
      CABLE(J,4)=FSEGN(I,3)
      CABLE(J,7)=E(I,1)
45 CONTINUE
40 CONTINUE
      DO 10 I=1,NEL
      IF (IEL(I,3) .EQ. 1) GO TO 10
      N1=IEL(I,1)
      N2=IEL(I,2)
      EL=X(N2,1)-X(N1,1)
      ALPHA=(YCABLE(N1)-YCABLE(N2))/EL
      ACCS=DCOS(ALPHA)
      CAELE(1,1)=ALPHA
      CAELE(1,2)=EL/ACOS
      CAELE(1,5)=CABLE(I,3)/CABLE(I,4)
      SIG=CAELE(1,5)
      EPS=CAELE(1,6)
      ENCD=CAELE(1,7)
      CALL FINDEE(E,SIG,EPS,ENCD)
      CAELE(1,6)=EPS
      CAELE(1,7)=ENCD
10 CONTINUE
      DO 50 I=1,NPS
      NE1=FSEGN(I,1)
      NE2=FSEGN(I,2)
      ELONG(1,1)=0
      ELONG(1,2)=0
      DO 55 J=NE1,NE2

```

```

3798      ELONG(I,1)=ELONG(I,1)+CABLE(J,2)
3799 55 CONTINUE
3800      ELCMG(I,2)=(FSEGN(I,4)*ELONG(I,1))/(CABLE(NEL,7)*FSEGN(I,3))
3801 50 CONTINUE
3802      FRICT=FM*FK
3803      IF (FRICT.NE.0) THEN
3804      CALL FBLOSS(CABLE2,NEL,NPS,FSEGN,FM,FK,ELONG,E)
3805      ENCL IF
3806      DO 20 I=1,NEL
3807      FINCAB(I,1)=CABLE(I,3)
3808 20 CONTINUE
3809 1000 DO 30 I=1,NEL
3810      IF (IEL(I,3) .EQ. 1) GO TO 30
3811      N1=IEL(I,1)
3812      N2=IEL(I,2)
3813      ALPHA=CABLE(I,1)
3814      ACCS=DCOS(ALPHA)
3815      ASIN=DSIN(ALPHA)
3816      F=CABLE(I,3)
3817      Y1=YCABLE(N1)+X(N1,2)
3818      Y2=YCABLE(N2)+X(N2,2)
3819      CLCAD(N1,1)=CLOAD(N1,1)+F*ACOS
3820      CLCAD(N1,2)=CLOAD(N1,2)+F*ASIN
3821      CLCAL(N1,3)=CLOAD(N1,3)-Y1+F*ACOS
3822      CLCAD(N2,1)=CLOAD(N2,1)+F*ACOS
3823      CLOAD(N2,2)=CLOAD(N2,2)+F*ASIN
3824      CLCAD(N2,3)=CLOAD(N2,3)+Y2+F*ACOS
3825 30 CONTINUE
3826      RETURN
3827      ENCL
C*****
      SUBROUTINE MODCAB(CABLE,YCABLE,D,NEL,IEL,NVAR,X,NMOD,E,CABSST,
      * NWSTF,NODE1)
C*****
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION CABLE(NEL,7),DISP(6),YCABLE(NMOD),D(1),
      * CABSST(NEL),NVAR(NMOD,1),X(NMOD,2),IEL(NEL,3),E(4,6)
      DO 500 I=1,NEL
      IF (IEL(I,3) .EQ. 1) GO TO 500
      DO 510 J=1,3
      NW1=IEL(I,1)
      JA=NVAR(NW1,J)
      IF (JA .EQ. 0) THEN
      DISP(J)=0
      ELSE
      DISP(J)=B(JA)
      ENCL IF
      NW2=IEL(I,2)
      JJ=J+3
      JA=NVAR(NW2,JJ)
      IF (JA .EQ. 0) THEN
      DISP(JJ)=0
      ELSE
      DISP(JJ)=B(JA)
      ENCL IF
510 CONTINUE
      ALPHA=CABLE(I,1)
      ACCS=DCOS(ALPHA)
      ASIN=DSIN(ALPHA)
3857
3858
3859
3860
3861
3862
3863
3864
3865
3866
3867
3868
3869
3870
3871
3872
3873
3874
3875
3876
3877
3878
3879
3880
3881
3882
3883
3884
3885
3886
3887
3888
3889
3890
3891
3892
3893
3894
3895
3896
3897
3898
3899
3900
3901
3902
3903
3904
3905
3906
3907
3908
3909
3910
3911
3912
3913
3914
3915

```

```

Y1=YCABLE(NW1)*X(NW1,2)
Y2=YCABLE(NW2)*X(NW2,2)
IF (CABLE(1,4).EQ.0) THEN
  STRAIN=0
ELSE
  STRAIN=(-DISP(1)*ACOS+DISP(2)*ASIN
+DISP(3)*Y1*ACOS+DISP(4)*ACOS
- -DISP(5)*ASIN-DISP(6)*Y2*ACOS)/CABLE(1,2)
END IF
CAESST(1)=STRAIN
CABLE(1,6)=CABLE(1,6)+STRAIN
ET=CABLE(1,6)
STE=CABLE(1,5)
ELAST=CABLE(1,7)
CALL PSTUEL(E,ET,STRAIN,STE,ELAST,NWSTP)
CABLE(1,5)=STE
CABLE(1,7)=ELAST
CABLE(1,3)=CABLE(1,5)*CABLE(1,4)
500 CONTINUE
RETURN
END
C*****
SUBROUTINE FALOSS(CABLE,NEL,NPS,PSEGN,PM,PK,ELONG,E)
C*****
IMPLICIT REAL*8(A-H,O-Z)
DIMENSION CABLE(NEL,7),PSEGN(10,5),ELONG(10,2),E(4,6)
DO 10 I=1,NPS
  IELEN=PSEGN(I,1)
  LELEN=PSEGN(I,2)
  F2=0
  ELONG(1,2)=0
  DO 20 L=1ELEN,LELEN
    J=1
    JA=J-1
    JP=J+1
    IF (PSEGN(I,5).EQ.2) THEN
      J=IELEN+LELEN-L
      JA=J+1
      JP=J-1
    END IF
    F1=F2
    IF (L.EQ.1ELEN) THEN
      F1=CABLE(J,3)
      TIJ=0
      GO TO 1
    END IF
    A=CABLE(JA,1)-CABLE(J,1)
    T=CABS(A)
    TIJ=T+CABLE(J,2)/(CABLE(JA,2)+CABLE(J,2))
    1 IF (L.EQ.LELEN) THEN
      TJK=0
      GO TO 2
    END IF
    A=CABLE(J,1)-CABLE(JP,1)
    T=CABS(A)
    TJK=T+CABLE(J,2)/(CABLE(L,2)+CABLE(JP,2))
    2 TJ=TIJ+TJK
    CL=CABLE(J,2)
    F2=F1/2.71828** (PM*TJ+PK*CL)

```

```

3916 CABLE(J,3)=(F1+F2)/2
3917 CABLE(J,5)=CABLE(J,3)/CABLE(J,4)
3918 SIG=CABLE(J,5)
3919 EPS=CABLE(J,6)
3920 ENCD=CABLE(J,7)
3921 CALL FINDSE(E,SIG,EPS,ENCD)
3922 CABLE(J,6)=EPS
3923 CABLE(J,7)=ENCD
3924 ELONG(1,2)=ELONG(1,2)+CABLE(J,6)*CABLE(J,2)
3925 20 CONTINUE
3926 10 CONTINUE
3927 RETURN
3928 END
3929 C*****
3930 SUBROUTINE ESTEL(E,ET,ES,STRE,ELAST,NWSTP)
3931 C*****
3932 IMPLICIT REAL*8(A-H,O-Z)
3933 DIMENSION E(4,6)
3934 IF (NWSTP.EQ.0) GO TO 100
3935 IF (ES.LT.0) THEN
3936   STE=STRE+E(1,1)*ES
3937   ELAST=E(1,1)
3938 ELSE
3939   100 STE=STRE+ELAST*ES
3940   SIG=0
3941   ENCD=0
3942   CALL FINDSE(E,ET,SIG,ENCD)
3943   IF (STRE.GT.SIG) THEN
3944     STE=SIG
3945     ELAST=ENCD
3946   END IF
3947 END IF
3948 RETURN
3949 END
3950 C*****
3951 SUBROUTINE FINDSE(E,EPS,SIG,ENCD)
3952 C*****
3953 IMPLICIT REAL*8(A-H,O-Z)
3954 DIMENSION E(4,6)
3955 E1=E(1,1)
3956 E2=E(1,2)
3957 E3=E(1,3)
3958 SY1=E(1,4)
3959 SY2=E(1,5)
3960 EY1=SY1/E1
3961 EY2=SY2/(SY2-SY1)/21
3962 EU=E(1,6)
3963 IF (EPS.GE.EU) THEN
3964   WRITE(3,1)
3965   1 POSMAT('*** PRESTRESSING CABLE RUPTURE ***')
3966 END IF
3967 IF (EPS.GT.EY2) THEN
3968   ENCD=22
3969   SIG=SY2*(EPS-EY2)*E2
3970 ELSE
3971   IF (EPS.GT.EY1) THEN
3972     ENCD=E1
3973     SIG=SY1*(EPS-EY1)*E1
3974
3975
3976
3977
3978
3979
3980
3981
3982
3983
3984
3985
3986
3987
3988
3989
3990
3991
3992
3993
3994
3995
3996
3997
3998
3999
4000
4001
4002
4003
4004
4005
4006
4007
4008
4009
4010
4011
4012
4013
4014
4015
4016
4017
4018
4019
4020
4021
4022
4023
4024
4025
4026
4027
4028
4029
4030
4031
4032

```

```

      ELSE
      ENCD=EC
      SIG=EPS*EO
      ENCL IF
      ENCL IF
      RETURN
      ENCL
C.....
      SUBROUTINE FINDEE(E,SIG,EPS,ENCD)
C.....
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION E(4,6)
      IO=E(1,1)
      I1=E(1,2)
      E2=E(1,3)
      SY1=E(1,4)
      SY2=E(1,5)
      EY1=SY1/EO
      EY2=EY1*(SY2-SY1)/E1
      EY=E(1,6)
      IF (SIG.GT.SY2) THEN
      ENCD=E2
      EPS=EY2*(SIG-SY2)/E2
      ELSE
      IF (SIG.GT.SY1) THEN
      ENCL=E1
      EPS=EY1*(SIG-SY1)/E1
      ELSE
      ENCD=EC
      EPS=SIG/EO
      ENCL IF
      ENCL IF
      IF (EPS.GE.EO) THEN
      WRITE(3,1)
      1 FORMAT('*** PRESTRESSING CABLE RUPTURE ***')
      ENCL IF
      RETURN
      ENCL
C.....
      SUBROUTINE REACT(NSUP,NNOD,NVAR,REAC,PREDIS,ITNST,RELIST,DCL)
C.....
      IMPLICIT REAL*8(A-H,O-Z)
      DIMENSION REAC(NSUP,3),RELIST(300,10)
      * ,NVAR(NNOD,3),PREDIS(NSUP,2),DCL(NNOD,3)
      NR=0
      DO 10 NS=1,NSUP
      NN=PREDIS(NS,1)
      DO 50 I=1,3
      REAC(NS,I)=DCL(NN,I)
C
C      STORE ALL REACTIONS
      IF (NVAR(NN,I).EQ.0) THEN
      NR=NR+1
      RELIST(ITNST,NN)=REAC(NS,I)
      ENCL IF
50 CONTINUE
10 CONTINUE
      RETURN

```

```

4033      END
4034 C.....
4035
4036      SUBROUTINE OUTPUT(NEL,ICOMF,AREA,NNOD,NVAR,FOPCE,SDISP,
4037 * ,IGMAT,CABLE,NOMPRO,FM,FK,KPS,PSEGN,ELONG,
4038 * ,ICHECK,NCHL,IATYPE,DIM,NGL,NL,STA,NS1,STRE,NS3,
4039 * ,EALL,STRB,ERG,ERC,CRACK,ICRACK,IALPHA,
4040 * ,IELD,NS4,IEL,Y,NSUP,NSUP),REAC,PREDIS,
* ,DISP,ISTEP,LC,NSTEPS,ITER,NTITER)
C.....
4041      IMPLICIT REAL*8(A-H,O-Z)
4042      DIMENSION AREA(NEL,6),NVAR(NNOD,3),DISP(NNOD,3),SDISP(NNOD,3)
4043 * ,CABLE(NEL,7),PSEGN(10,5),ELONG(10,2),
4044 * ,ICHECK(NCHL),DIM(NEL,6),Y(NL,3),STA(NEL,NS1),
4045 * ,STRE(NEL,NS3),EALL(NEL,NS3),STRB(NEL,8),CRACK(NEL,8),
4046 * ,ICRACK(NEL,3),IALPHA(NEL,NL),IELD(NEL,NS4),IEL(NEL,3),
4047 * ,REAC(NSUP,3),PREDIS(NSUP,2),FOPCE(NEL,3)
4048
4049 C
4050      WRITE(3,2222)
4051      WRITE(3,2001)LC,ISTEP,NSTEPS,ITER,NTITER
4052 2001 FORMAT(10X,'L C A C E #',13,10X,'STEP #',13,'/',13,
4053 * ,10X,'ITER. IN THE STEP= ',13,10X,'TOTAL # ITER.= ',15)
4054 C
4055      WRITE(3,2222)
4056 2222 FORMAT(/,130(' '),/)
4057      WRITE(3,29)
4058 29 FORMAT(10X,'N E W S E C T I O N P R O P E R T I E S',
4059 * ,10X,'( TRANSPARENT, TC BOTTOM )',/)
4060      IF (ICOMF.EQ.1) THEN
4061      WRITE(3,32)
4062 32 FORMAT(/,20X,'( COMPOSITE SECTION )')
4063      ELSE
4064      WRITE(3,33)
4065 33 FORMAT(/,20X,'( NON COMPOSITE SECTION )')
4066      ENCL IF
4067      WRITE(3,1111)
4068 1111 FORMAT(/,130(' '),/)
4069      WRITE(3,31)
4070 31 FORMAT(1X,'ELEM #',4X,'CENTROID',10X,'AREA',9X,'AREA NON.',
4071 * ,7X,'INERTIA',//)
      DO 41 I=1,NEL
      WRITE(3,50)I,(AREA(I,J),J=1,4)
4072 50 FORMAT(4X,13,4(2X,D13.6),/)
4073 41 CONTINUE
C
4074      WRITE(3,2222)
4075      WRITE(3,1650)
4076 1650 FORMAT(/,10X,'N O D A I D I S P L A C E M E N T S ( )R,UP,CC',
4077 * ,//,30X,'( THIS STEP )',45X,'( TOTAL )')
4078      WRITE(3,1111)
4079      WRITE(3,1670)
4080 1670 FORMAT(1X,'NODE #',10X,'X',10X,'Y',15X,'THETA',
4081 * ,15X,'X',10X,'Y',15X,'THETA',//)
      DO 200 I=1,NNOD
      WRITE(3,1700)I,DISP(I,1),DISP(I,2),DISP(I,3),
4082 * ,SDISP(I,1),SDISP(I,2),SDISP(I,3)
4083 1700 FORMAT(4X,13,6(5X,D13.6),/)
4084 200 CONTINUE
C
4085      WRITE(3,2222)
4086
4087
4088
4089
4090
4091
4092
4093
4094
4095
4096
4097
4098
4099
4100
4101
4102
4103
4104
4105
4106
4107
4108
4109
4110
4111
4112
4113
4114
4115
4116
4117
4118
4119
4120
4121
4122
4123
4124
4125
4126
4127
4128
4129
4130
4131
4132
4133
4134
4135
4136
4137
4138
4139
4140
4141
4142
4143
4144
4145
4146
4147
4148
4149

```



```

1000 WRITE(3,1000)
      FORMAT(10X,'ELEMENT RESULTANT FORCES',
      * 5X,'(*) TENSION,COMP.UF,LEFT UP',//
      * 30X,'( TOTAL )')
      WRITE(3,1111)
      WRITE(3,1100)
1100 FORMAT(1X,'ELEM #',9X,'AXIAL',12X,'MOMENT',13X,'SHEAR',//)
      DO 1200 I=1,NEL
        WRITE(3,1300)I,(FORCE(I,J),J=1,3)
1300 FORMAT(4X,I3,3(5X,D13.6),/)
1200 CONTINUE
C
      WRITE(3,2222)
      WRITE(3,2000)
7000 FORMAT(1X,10X,'MODAL EXTERNAL REACTIONS',
      * 3X,UP,CC',//,30X,'( TOTAL )')
      WRITE(3,1111)
      WRITE(3,2010)
7010 FORMAT(1X,'MODE #',11X,'RX',15X,'RY',16X,'RZ',//)
      DO 7030 J=1,NSUP
        I=PRDIS(J,1)
        WRITE(3,2020)I,(REAC(J,K),K=1,3)
7020 FORMAT(4X,I3,3(5X,D13.6),/)
7030 CONTINUE
C
      IF (ICMAT.EQ.1) THEN
        WRITE(3,2222)
        WRITE(3,2100)
2100 FORMAT(10X,'FIMIAL CABLE PROPERTIES',
      * 3X,'( UP TO THIS STEP )')
        WRITE(3,1111)
        WRITE(3,2200)
2200 FORMAT(1X,'ELEM #',6X,'FORCE',8X,'STRESS',8X,'STRAIN',
      * 8X,'E MOD',//)
        DO 700 K=1,NEL
          WRITE(3,2300)K,CABLE(K,3),CABLE(K,5),CABLE(K,6),CABLE(K,7)
2300 FORMAT(4X,I3,4(2X,D12.5),/)
700 CONTINUE
      END IF
C
      IF (ICWFBQ.EQ.1) THEN
        WRITE(3,2222)
        WRITE(3,2400)
2400 FORMAT(10X,'CABLE ELONGATION BY PRESTRESSING',
      * 3X,'( FRICTION INCLUDED )')
        WRITE(3,1111)
        WRITE(3,2450)FK
2450 FORMAT(1X,'CURVATURE FRICTION COEFFICIENT =',2X,D12.5,/)
        WRITE(3,2451)FK
2451 FORMAT(1X,'MOBILE FRICTION COEFFICIENT =',2X,D12.5,/)
        WRITE(3,1111)
        WRITE(3,2452)
2452 FORMAT(1X,'FROM ELEM # TO ELEM #',7X,'LENGHT',7X,
      * 'ELONGATION',//)
        DO 800 K=1,NPS
          NE1=PS1EM(K,1)
          NE2=PS1EM(K,2)
          WRITE(3,2600)NE1,NE2,ELONG(K,1),ELONG(K,2)
2600 FORMAT(9X,I3,9X,I3,4X,D12.5,3X,D12.5,/)
800 CONTINUE

```

```

4150
4151
4152
4153
4154
4155
4156
4157
4158
4159
4160
4161
4162
4163
4164
4165
4166
4167
4168
4169
4170
4171
4172
4173
4174
4175
4176
4177
4178
4179
4180
4181
4182
4183
4184
4185
4186
4187
4188
4189
4190
4191
4192
4193
4194
4195
4196
4197
4198
4199
4200
4201
4202
4203
4204
4205
4206
4207
4208
4209
      END IF
C
      WRITE(3,2222)
      WRITE(3,2510)
2510 FORMAT(30X,'STRAINS AT THE BORDERS',
      * 30X,'( UP TO THIS STEP )',41X,'( MAX. REACHED )')
      WRITE(3,1111)
      WRITE(3,2511)
2511 FORMAT(1X,'ELEM #',24,'BOTTOM GIRDER',2X,' TOP GIRDER ',
      * 2X,' BOTTOM DECK ',2X,' TOP DECK ',
      * 2X,' BOTTOM GIRDER ',2X,' TOP GIRDER ',
      * 2X,' BOTTOM DECK ',2X,' TOP DECK ',//)
      DO 2520 K=1,NEL
        WRITE(3,2521)K,(STRB(K,J),J=1,8)
2521 FORMAT(4X,I3,8(2X,D13.6),/)
2520 CONTINUE
C
      WRITE(3,2222)
      WRITE(3,3000)
3000 FORMAT(30X,'CRACKING LENGTH & WIDTH')
      WRITE(3,1111)
      WRITE(3,4000)EKG,ERD
4000 FORMAT(1X,'GIRDER RUPTURE STRAIN =',D12.5,/,
      * 1X,' DECK RUPTURE STRAIN =',D12.5)
      WRITE(3,1111)
      WRITE(3,5000)
5000 FORMAT(1X,'ELEM #',2X,'BOTTOM GIRDER',
      * 2X,' TOP GIRDER',
      * 2X,' BOTTOM DECK',
      * 2X,' TOP DECK ',
      * 2X,' BOTTOM GIRDER',
      * 2X,' TOP GIRDER',
      * 2X,' BOTTOM DECK',
      * 2X,' TOP DECK ',//)
      DO 30 I=1,NEL
        WRITE(3,6000)I,(CRACK(I,J),J=1,8)
6000 FORMAT(4X,I3,8(2X,D13.6),/)
30 CONTINUE
C
      WRITE(3,2222)
      WRITE(3,3100)
3100 FORMAT(30X,'CRACKING PATTERN')
      WRITE(3,1111)
      WRITE(3,3400)EKG,ERD
3400 FORMAT(1X,'GIRDER RUPTURE STRAIN =',D12.5,/,
      * 1X,' DECK RUPTURE STRAIN =',D12.5)
      WRITE(3,1111)
      WRITE(3,3500)
3500 FORMAT(1X,'ELEM #',20X,'LAYERS',//)
      IF (ICOMP.LV.0) LIM=NEL
      IF (ICOMP.EQ.1) LIM=NEL
      DO 35 I=1,NEL
        WRITE(3,3600)I,(CRACK(I,J),J=1,LIM)
3600 FORMAT(4X,I3,5X,40(I2),/)
35 CONTINUE
      WRITE(3,1111)
      WRITE(3,3800)
3800 FORMAT(20X,'CRACK ANGLES ( DEGREES )')
      WRITE(3,1111)
      DO 60 I=1,NEL

```

```

4210
4211
4212
4213
4214
4215
4216
4217
4218
4219
4220
4221
4222
4223
4224
4225
4226
4227
4228
4229
4230
4231
4232
4233
4234
4235
4236
4237
4238
4239
4240
4241
4242
4243
4244
4245
4246
4247
4248
4249
4250
4251
4252
4253
4254
4255
4256
4257
4258
4259
4260
4261
4262
4263
4264
4265
4266
4267
4268
4269

```



```

3900 WRITE(3,3900)I,(IALPHA(I,J),J=1,11M)
3900 FORMAT(4X,13,3X,40(13),/)
60 CONTINUE
C
WRITE(3,2222)
WRITE(3,5004)
5004 FORMAT(10X,'R E I N F. S T E E L S T R E S S E S ')
WRITE(3,1111)
WRITE(3,5001)
5001 FORMAT(1X,'ELEM #',4X,'DECK STEEL',5X,'TOP STEEL',
      4X,'BOTTOM STEEL',/)
DO 5002 I=1,NEL
WRITE(3,5003)I,(STRE(I,NL+J),J=1,3)
5003 FORMAT(4X,13,3(3X,D12.5),/)
5002 CONTINUE
C
WRITE(3,2222)
WRITE(3,1050)
1050 FORMAT(30X,'Y I E L D I N G { MGL+3 } ')
WRITE(3,1111)
WRITE(3,1150)
1150 FORMAT(1X,'ELEM #',15X,'WEINP. STEEL { D,T,B } & L A Y E R S',/)
LIM=MGL+1
DO 1250 I=1,NEL
WRITE(3,1350)I,(IELD(I,J),J=LIM,MS4),(IELD(I,J),J=1,MGL)
1350 FORMAT(4X,13,5X,3(12),2X,40(12),/)
1250 CONTINUE
C
IF(MCHEL.GT.0) THEN
WRITE(3,2222)
WRITE(3,3005)
3005 FORMAT(20X,'C H E C K I N G E L E M E N T S ')
DO 3010 MK=1,MCHL
WRITE(3,1111)
NEC=ICHECK(MK)
WRITE(3,3020)NEC
3020 FORMAT(20X,'ELEMEN1 #',2X,13,/)
WRITE(3,1111)
WRITE(3,3030)
3030 FORMAT(4X,'#',7X,'POSITION',6X,'LAYER AREA',8X,'STRAIN',12X,
      'STRESS',9X,'INST.MODULUS',/)
ITYPE=IEL(MK,3)
CALL LAYER(DIM,ICOMP,IATYPE,IGNAT,ITYPE,NEL,NEC,Y,TH,MGL,NL)
DO 3040 J=1,NL
L=NL+1-J
WRITE(3,3050)I,Y(L,1),Y(L,2),STA(MK,L),STBE(MK,L),EALL(MK,L)
3050 FORMAT(3X,12,5X,D12.5,3X,D12.5,3(3X,D15.8),/)
3040 CONTINUE
3010 CONTINUE
END IF
WRITE(3,2222)
RETURN
END
C*****
C DATA INPUT
C*****
C
C # OF EXEMPLES TO BE RUN
C NEL,NCEL,MNCD,MSUP,MLOCA,MGL(5/6,1/4,R/6),MGL,MCHL
C LIST ELEM.S TO BE CHECKED, IF ANY

```

```

4270 C BEARING COEFFICIENT
4271 C DRIVLI,MOCH,ALPLI
4272 C IGNAT, IATYPE, ICOMP, ISTEEL, ISSC
4273 C GAMAG,GAMAD
4274 C TIMES: TGC,TDC,TJFL,TDFL,TP (ALL >= 28 DAYS)
4275 C MATERIAL PROPERTIES : (ALL POSITIVE)
4276 C P/S : EO, EI, E2, SY1, SY2, EU
4277 C R/S : EO, EY, O, O, O, EU
4278 C G/S : EO, EY, O, O, O, EU
4279 C OR
4280 C G/C : EO, FC1, ER, O, O, EU
4281 C D/C : EO, FC1, ER, O, O, EU
4282 C IEL : NODE 1, NODE 2, TYPE 3 OR 1
4283 C ... ALL ELEMENTS ...
4284 C COORD X,Y,NODE COND 0 OR 1 IN X,Y,Z
4285 C ... ALL NODES ...
4286 C DIMENSIONS: STEEL GIRDER
4287 C BU, HU, A, H, M, TI, WT, BT
4288 C RECT. GIRDER
4289 C BD, HD, B, H, O, O, O, O
4290 C CTHEJ SHAPE
4291 C BD, HD, BT, HT, DW, HW, BD, HD
4292 C CONNECTION ELEMENT
4293 C BD, HD, H1, H2, O, O, O, O
4294 C ... ONE LINE IF CONSTANT CROSS SECTION
4295 C ALL ELEMENTS IF VARIABLE ...
4296 C STEEL: STEEL GIRDER OR CONNECTION ELEMENT
4297 C DSA, DSP, O, O, O, O
4298 C CONCRETE GIRDER
4299 C DSA, DSP, TSA, TSP, BSA, BSP
4300 C ... ONE LINE IF CONSTANT
4301 C ALL ELEMENTS IF VARIABLE...
4302 C L.C.#,ICOMP,# STEPS,PRINT,EFFECT,1.TIME,V.TIME,HINGED
4303 C ... ALL ...
4304 C MNCD #, PRESCRIBED DISPLACEMENT
4305 C ... ALL SUPPORTS ...
4306 C TEMP. VAN. : T1, T2, T3
4307 C APPLIED MODAL LOADS : X Y M
4308 C ... ALL NODES ...
4309 C APPLIED ELEM. LOADS : Q, P, AP
4310 C ... ALL ELEMENTS ...
4311 C PRESIRASSING ( IF USED )
4312 C IPHET,IPHOF,NPS,FM,PA,IST
4313 C ELEM# TO ELEM#,AREA,FO,IPULL
4314 C ... ALL SEGMENTS ...
4315 C NCDE,FCG,NCDE,FCG,NODE,POS
4316 C ... ALL SEGMENTS ...
4317 C OR
4318 C CABLE POSITION
4319 C ... ALL NODES ...
4320 C
4321 C*****
4322
4323
4324
4325
4326
4327
4328
4329
4330
4331
4332
4333
4334
4335
4336
4337
4338
4339
4340
4341
4342
4343
4344
4345
4346
4347
4348
4349
4350
4351
4352
4353
4354
4355
4356
4357
4358
4359
4360
4361
4362
4363
4364
4365
4366
4367
4368
4369
4370
4371
4372
4373
4374
4375
4376
4377
4378
4379
4380
4381

```

8.3 Sample Input

Input for the deck-continuous beam shown in Figs. 5.16 and 5.17 and loaded as in Fig. 5.23.

1.	1	76.	6.75, 57, 2, 51, 0, 0
2.	24, 2, 25, 5, 4, 20, 10, 2	77.	6.75, 57, 2, 51, 0, 0
3.	6, 18	78.	6.75, 57, 0, 0, 0, 0
4.	23000	79.	6.75, 57, 0, 0, 0, 0
5.	-0.05, 6, 5	80.	6.75, 57, 0, 0, 0, 0
6.	1, 1, 0, 1, 1	81.	6.75, 57, 0, 0, 0, 0
7.	0.0868, 0.0868	82.	6.75, 57, 0, 0, 0, 0
8.	0, 0, 0, 0, 0	83.	6.75, 57, 2, 51, 0, 0
9.	280000000, 3100000, 120000, 240000, 260000, 0.1	84.	6.75, 57, 2, 51, 0, 0
10.	29000000, 0.001724, 0.0, 0, 0, 0.01	85.	11.25, 57, 2, 51, 2, 2
11.	4500000, 6000, 0.00013, 0.0, 0, 0.003	86.	11.25, 57, 2, 51, 2, 2
12.	3500000, 3500, 0.00012, 0.0, 0, 0.003	87.	1, 0, 1, 0, 0, 0, 0, 0
13.	1, 2, 0	88.	2, 0, 1, 0, 0, 0, 0, 0
14.	2, 3, 0	89.	3, 0, 1, 0, 0, 0, 0, 0
15.	3, 4, 0	90.	5, 1, 1000, 0, 0, 0, 0, 0
16.	4, 5, 0	91.	1, 0
17.	5, 6, 0	92.	12, 0
18.	6, 7, 0	93.	13, 0
19.	7, 8, 0	94.	24, 0
20.	8, 9, 0	95.	25, 0
21.	9, 10, 0	96.	0, 0, 0, 0
22.	10, 11, 0	97.	0, 0, 0, 0
23.	11, 12, 0	98.	0, 0, 0, 0
24.	12, 13, 1	99.	0, 0, 0, 0
25.	13, 14, 0	100.	0, 0, 0, 0
26.	14, 15, 0	101.	0, 0, 0, 0
27.	15, 16, 0	102.	0, 0, 0, 0
28.	16, 17, 0	103.	0, 0, 0, 0
29.	17, 18, 0	104.	0, 0, 0, 0
30.	18, 19, 0	105.	0, 0, 0, 0
31.	19, 20, 0	106.	0, 0, 0, 0
32.	20, 21, 0	107.	0, 0, 0, 0
33.	21, 22, 0	108.	0, 0, 0, 0
34.	22, 23, 0	109.	0, 0, 0, 0
35.	23, 24, 0	110.	0, 0, 0, 0
36.	24, 25, 1	111.	0, 0, 0, 0
37.	0, 0, 0, 1, 0	112.	0, 0, 0, 0
38.	72, 0, 0, 0, 0, 0	113.	0, 0, 0, 0
39.	144, 0, 0, 0, 0, 0	114.	0, 0, 0, 0
40.	216, 0, 0, 0, 0, 0	115.	0, 0, 0, 0
41.	288, 0, 0, 0, 0, 0	116.	0, 0, 0, 0
42.	360, 0, 0, 0, 0, 0	117.	0, 0, 0, 0
43.	432, 0, 0, 0, 0, 0	118.	0, 0, 0, 0
44.	504, 0, 0, 0, 0, 0	119.	0, 0, 0, 0
45.	576, 0, 0, 0, 0, 0	120.	0, 0, 0, 0
46.	648, 0, 0, 0, 0, 0	121.	0, 0, 0, 0
47.	720, 0, 0, 0, 0, 0	122.	1000, 0, 0, 0
48.	786, 0, 0, 1, 0	123.	1000, 0, 0, 0
49.	798, 0, 0, 1, 0	124.	1000, 0, 0, 0
50.	864, 0, 0, 0, 0, 0	125.	1000, 0, 0, 0
51.	936, 0, 0, 0, 0, 0	126.	1000, 0, 0, 0
52.	1008, 0, 0, 0, 0, 0	127.	1000, 0, 0, 0
53.	1080, 0, 0, 0, 0, 0	128.	1000, 0, 0, 0
54.	1152, 0, 0, 0, 0, 0	129.	1000, 0, 0, 0
55.	1224, 0, 0, 0, 0, 0	130.	1000, 0, 0, 0
56.	1296, 0, 0, 0, 0, 0	131.	1000, 0, 0, 0
57.	1368, 0, 0, 0, 0, 0	132.	1000, 0, 0, 0
58.	1440, 0, 0, 0, 0, 0	133.	1000, 0, 0, 0
59.	1512, 0, 0, 0, 0, 0	134.	0, 0, 0, 0
60.	1578, 0, 0, 1, 0	135.	0, 0, 0, 0
61.	1584, 0, 1, 1, 1	136.	0, 0, 0, 0
62.	72, 6, 20, 11, 8, 30, 26, 13	137.	0, 0, 0, 0
63.	6.75, 57, 0, 0, 0, 0	138.	0, 0, 0, 0
64.	6.75, 57, 0, 0, 0, 0	139.	0, 0, 0, 0
65.	6.75, 57, 0, 0, 0, 0	140.	0, 0, 0, 0
66.	6.75, 57, 0, 0, 0, 0	141.	0, 0, 0, 0
67.	6.75, 57, 0, 0, 0, 0	142.	0, 0, 0, 0
68.	6.75, 57, 0, 0, 0, 0	143.	0, 0, 0, 0
69.	6.75, 57, 0, 0, 0, 0	144.	0, 0, 0, 0
70.	6.75, 57, 0, 0, 0, 0	145.	0, 0, 0, 0
71.	6.75, 57, 2, 51, 0, 0	146.	1, 0, 2, 0, 0, 0
72.	6.75, 57, 2, 51, 0, 0	147.	1, 11, 2, 72, 516000, 1
73.	11.25, 57, 2, 51, 2, 2	148.	13, 23, 2, 72, 516000, 1
74.	11.25, 57, 2, 51, 2, 2	149.	1, 3, 6, 3, 12, 3
75.	11.25, 57, 2, 51, 2, 2	150.	13, 3, 18, 3, 24, 3

8.4 Sample Output

Output for the deck-continuous beam shown in Figs. 5.16 and 5.17 and loaded as in Fig. 5.23.

```

.....
.....
EXAMPLE # 1
.....
STORAGE PROVIDED = 20000
.....
INPUT DATA
.....
NUMBER OF ELEMENTS = 24
NUMBER OF CONNECTION ELEMENTS = 2
NUMBER OF NODES = 25
NUMBER OF SUPPORTS = 5
.....
PROPERTIES
.....
0 1 2
GIRDER MATERIAL STEEL PREST. CONC REINF. CONC
GIRDER TYPE RECTANGULAR 1st OR BOX
SECTION DIMENSIONS CONSTANT VARIABLE
STEEL DISTRIBUTION CONSTANT VARIABLE
COMPOSITE SECTION NON COMP. COMPOSITE
STRESS-STRAIN CURVE HOGNESTAD BILINEAR
.....
DRAWING CUEP, = 0.230000 05
GIRDER MAT. UNIT HEIGHT = 0.860000000-01
DECK MAT. UNIT HEIGHT = 0.460000000-01
GIRDER MATERIAL= 1
SECTION TYPE= 1
SECTION DIMENSIONS= 0
STEEL DISTRIBUTION= 1
STRESS-STRAIN CURVE= 1
TIME LIST 1 GIRDER CASTING 0.0000 00 DAYS
" 1ST LOADING 0.0000 00 "
DECK CASTING 0.0000 00 "
" 1ST LOADING 0.0000 00 "
PRESTRESSING 0.0000 00 "
.....
MATERIAL PROPERTIES
.....
P/S 1 EQ: A1: E2: SY1: SY2: EU
R/S 1 EQ: EY: 0: 0: 0: EU
S/S 1 EQ: EY: 0: 0: 0: EU
S/C 1 EQ: FC1: ER: 0: 0: EU
D/C 1 EQ: FC1: ER: 0: 0: EU
.....
PREST. STEEL: 0.280000 06 0.310000 07 0.120000 06 0.240000 06 0.280000 06 0.100000 05
REINF. STEEL: 0.290000 08 0.172400-02 0.000000 00 0.000000 00 0.000000 00 0.100000-01
GIRDER MAT.: 0.450000 07 0.800000 04 0.120000-03 0.000000 00 0.000000 00 0.200000-02
DECK CONCR.: 0.350000 07 0.350000 04 0.130000-03 0.000000 00 0.000000 00 0.200000-02
.....

```

ELEMENT INCIDENCE & TYPE

ELM #	N1	N2	TYPE
1	1	2	0
2	2	3	0
3	3	4	0
4	4	5	0
5	5	6	0
6	6	7	0
7	7	8	0
8	8	9	0
9	9	10	0
10	10	11	0
11	11	12	0
12	12	13	1
13	13	14	0
14	14	15	0
15	15	16	0
16	16	17	0
17	17	18	0
18	18	19	0
19	19	20	0
20	20	21	0
21	21	22	0
22	22	23	0
23	23	24	0
24	24	25	1

NODAL COORDINATES

NODE #	X	Y
1	0.000000 00	0.000000 00
2	0.720000 02	0.000000 00
3	0.144000 03	0.000000 00
4	0.216000 03	0.000000 00
5	0.288000 03	0.000000 00
6	0.360000 03	0.000000 00
7	0.432000 03	0.000000 00
8	0.504000 03	0.000000 00
9	0.576000 03	0.000000 00
10	0.648000 03	0.000000 00
11	0.720000 03	0.000000 00
12	0.786000 03	0.000000 00
13	0.798000 03	0.000000 00
14	0.864000 03	0.000000 00
15	0.936000 03	0.000000 00
16	0.100800 04	0.000000 00
17	0.108000 04	0.000000 00
18	0.115200 04	0.000000 00
19	0.122400 04	0.000000 00
20	0.129600 04	0.000000 00
21	0.136800 04	0.000000 00
22	0.144000 04	0.000000 00
23	0.151200 04	0.000000 00
24	0.157800 04	0.000000 00
25	0.168400 04	0.000000 00

LOAD CASES

1) GIRDER DEAD LOAD
2) PRESTRESSING
3) DECK DEAD LOAD
4) SUPPORT DISPLACEMENT
5) LIVE LOAD
6) TEMPERATURE
7) CREEP, SHRINKAGE AND RELAXATION

EFFECT LABEL

0 NONE
1 CREEP
2 SHRINKAGE
3 RELAXATION
4 ALL

LOAD CASE #	TYPE	COMP. SECTION	# STEPS	PRINT STEP	EFFECT	F. GAY	L. GAY	MINGED
1	1	0	1	0	0	0	0	0
2	2	0	1	0	0	0	0	0
3	3	0	1	0	0	0	0	0
4	4	1	00	0	0	0	0	0

LOCA (1) 2 3 4 5 6 7 8

PRESCRIBED DISPLACEMENTS

SUP #	NODE #	DISP. VALUE
1	1	0.0000 00
2	12	0.0000 00
3	13	0.0000 00
4	24	0.0000 00
5	25	0.0000 00

TEMPERATURE VARIATION (F)

TOP DECK	TOP GIRDER	BOTTOM GIRDER
0	0	0

LIVE LOAD

NODAL APPLIED LOADS (+)IN UP, CC

NODE #	PX	PY	PZ
1	0.00000000 00	0.00000000 00	0.00000000 00
2	0.00000000 00	0.00000000 00	0.00000000 00
3	0.00000000 00	0.00000000 00	0.00000000 00
4	0.00000000 00	0.00000000 00	0.00000000 00
5	0.00000000 00	0.00000000 00	0.00000000 00
6	0.00000000 00	0.00000000 00	0.00000000 00
7	0.00000000 00	0.00000000 00	0.00000000 00
8	0.00000000 00	0.00000000 00	0.00000000 00
9	0.00000000 00	0.00000000 00	0.00000000 00
10	0.00000000 00	0.00000000 00	0.00000000 00
11	0.00000000 00	0.00000000 00	0.00000000 00
12	0.00000000 00	0.00000000 00	0.00000000 00
13	0.00000000 00	0.00000000 00	0.00000000 00
14	0.00000000 00	0.00000000 00	0.00000000 00
15	0.00000000 00	0.00000000 00	0.00000000 00
16	0.00000000 00	0.00000000 00	0.00000000 00
17	0.00000000 00	0.00000000 00	0.00000000 00
18	0.00000000 00	0.00000000 00	0.00000000 00
19	0.00000000 00	0.00000000 00	0.00000000 00
20	0.00000000 00	0.00000000 00	0.00000000 00
21	0.00000000 00	0.00000000 00	0.00000000 00
22	0.00000000 00	0.00000000 00	0.00000000 00
23	0.00000000 00	0.00000000 00	0.00000000 00
24	0.00000000 00	0.00000000 00	0.00000000 00
25	0.00000000 00	0.00000000 00	0.00000000 00

.....

E L E M E N T A P P L I E D L U A S (+100cm)

.....

ELEM #	U.DIST.	CONC.	PR.L.NUDE
1	0.10000000 04	0.00000000 00	0.00000000 00
2	0.10000000 04	0.00000000 00	0.00000000 00
3	0.10000000 04	0.00000000 00	0.00000000 00
4	0.10000000 04	0.00000000 00	0.00000000 00
5	0.10000000 04	0.00000000 00	0.00000000 00
6	0.10000000 04	0.00000000 00	0.00000000 00
7	0.10000000 04	0.00000000 00	0.00000000 00
8	0.10000000 04	0.00000000 00	0.00000000 00
9	0.10000000 04	0.00000000 00	0.00000000 00
10	0.10000000 04	0.00000000 00	0.00000000 00
11	0.10000000 04	0.00000000 00	0.00000000 00
12	0.00000000 00	0.00000000 00	0.00000000 00
13	0.00000000 00	0.00000000 00	0.00000000 00
14	0.00000000 00	0.00000000 00	0.00000000 00
15	0.00000000 00	0.00000000 00	0.00000000 00
16	0.00000000 00	0.00000000 00	0.00000000 00
17	0.00000000 00	0.00000000 00	0.00000000 00
18	0.00000000 00	0.00000000 00	0.00000000 00
19	0.00000000 00	0.00000000 00	0.00000000 00
20	0.00000000 00	0.00000000 00	0.00000000 00
21	0.00000000 00	0.00000000 00	0.00000000 00
22	0.00000000 00	0.00000000 00	0.00000000 00
23	0.00000000 00	0.00000000 00	0.00000000 00
24	0.00000000 00	0.00000000 00	0.00000000 00

.....

DISPLACEMENT DRIVEN METHOD FOR L.L.

NODE # u AT -0.500000000-01

L.L. UPPER LIMIT = 0.5000 01 x

.....

P R E S T R E S S I N G

.....

PRESTRESSING AREA AND INITIAL FORCE

(PRE-TENSIONED CABLE)
(LOW-RELAXATION STEEL)

.....

FROM ELEM #	TO ELEM #	AREA	INITIAL FORCE	JACKING SIDE
1	11	0.272000 01	0.5160000 06	1
13	23	0.272000 01	0.5160000 06	1

.....

C A B L E P R O F I L E

(STRAIGHT)

.....

NODE # DIST. TO BASE

1	0.300000 01
2	0.300000 01
3	0.300000 01
4	0.300000 01
5	0.300000 01
6	0.300000 01
7	0.300000 01
8	0.300000 01
9	0.300000 01
10	0.300000 01
11	0.300000 01
12	0.300000 01
13	0.300000 01
14	0.300000 01
15	0.300000 01
16	0.300000 01
17	0.300000 01
18	0.300000 01
19	0.300000 01
20	0.300000 01
21	0.300000 01
22	0.300000 01
23	0.300000 01
24	0.300000 01
25	0.000000 00

ESCOLA DE ENGENHARIA
EQUITECA

 RESULTS

 NUNDO 6

 GLOBAL DISPLACEMENT

 NUDO # X Y IMETA

1	1	0	2
2	3	4	5
3	6	7	8
4	9	10	11
5	12	13	16
6	15	16	17
7	18	19	20
8	21	22	23
9	24	25	26
10	27	28	29
11	30	31	32
12	33	0	34
13	36	0	36
14	37	38	39
15	40	41	42
16	43	44	45
17	46	47	48
18	49	50	51
19	52	53	54
20	55	56	57
21	58	59	60
22	61	62	63
23	64	65	66
24	67	0	68
25	0	0	0

 STORAGE NEEDED = 17212

 DEAD LOAD

MEM #	WINDR	DECK
1	0.692664000 02	0.374976000 02
2	0.692664000 02	0.374976000 02
3	0.692664000 02	0.374976000 02
4	0.692664000 02	0.374976000 02
5	0.692664000 02	0.374976000 02
6	0.692664000 02	0.374976000 02
7	0.692664000 02	0.374976000 02
8	0.692664000 02	0.374976000 02
9	0.692664000 02	0.374976000 02
10	0.692664000 02	0.374976000 02
11	0.692664000 02	0.374976000 02
12	0.000000000 00	0.374976000 02
13	0.692664000 02	0.374976000 02
14	0.692664000 02	0.374976000 02
15	0.692664000 02	0.374976000 02
16	0.692664000 02	0.374976000 02
17	0.692664000 02	0.374976000 02
18	0.692664000 02	0.374976000 02
19	0.692664000 02	0.374976000 02
20	0.692664000 02	0.374976000 02
21	0.692664000 02	0.374976000 02
22	0.692664000 02	0.374976000 02
23	0.692664000 02	0.374976000 02
24	0.000000000 00	0.374976000 02

***** ORIGINAL SECTION PROPERTIES (TRANSFORMED) *****

(NON-COMPOSITE SECTION)

(COMPOSITE SECTION)

ELEM #	CENTROID	AREA	AREA MOM.	INERTIA	CENTROID	AREA	AREA MOM.	INERTIA
1	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
4	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
3	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
6	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
5	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
8	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
7	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
8	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
9	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
10	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
11	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06	0.3534480 02	0.1232280 04	0.4355460 05	0.5672850 06
12	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.4085000 03	0.0000000 00	0.0000000 00
13	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06	0.3534480 02	0.1232280 04	0.4355460 05	0.5672850 06
14	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
15	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
16	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
17	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
18	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
19	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
20	0.2454510 02	0.7980000 03	0.1958700 05	0.4641490 06	0.3500510 02	0.1177500 04	0.4121850 05	0.5380900 06
21	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
22	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06	0.3517830 02	0.1190390 04	0.4187580 05	0.5393220 06
23	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06	0.3534480 02	0.1232280 04	0.4355460 05	0.5672850 06
24	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.4085000 03	0.0000000 00	0.0000000 00

***** LOAD CASE # 1 STEP # 1/ 1 ITER. IN THE STEP# 2 TOTAL # ITER.# 4 *****

***** NEW SECTION PROPERTIES (TRANSFORMED TO ROTION) *****

(NON-COMPOSITE SECTION)

ELEM #	CENTROID	AREA	AREA MOM.	INERTIA
1	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
2	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
3	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
4	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
5	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
6	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
7	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
8	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
9	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
10	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
11	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
12	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00
13	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
14	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
15	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
16	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
17	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
18	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
19	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
20	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
21	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
22	0.2496560 02	0.8108890 03	0.2024430 05	0.7784380 06
23	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
24	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

MODAL DISPLACEMENTS (1)HUP:CC
(THIS STEP)

(TOTAL)

NODE #	X	Y	THETA	X	Y	THETA
1	-0.2864770-01	0.0000000 00	-0.1188900-02	-0.2864770-01	0.0000000 00	-0.1188900-02
2	-0.2732190-01	-0.8340800-01	-0.1114880-02	-0.2732190-01	-0.8340800-01	-0.1114880-02
3	-0.2361180-01	-0.1591860 00	-0.9637300-03	-0.2361180-01	-0.1591860 00	-0.9637300-03
4	-0.1805230-01	-0.2211300 00	-0.7372270-03	-0.1805230-01	-0.2211300 00	-0.7372270-03
5	-0.1117810-01	-0.2645980 00	-0.4571620-03	-0.1117810-01	-0.2645980 00	-0.4571620-03
6	-0.3523950-02	-0.2665140 00	-0.1453240-03	-0.3523950-02	-0.2665140 00	-0.1453240-03
7	0.4375270-02	-0.2653860 00	0.1765010-03	0.4375270-02	-0.2653860 00	0.1765010-03
8	0.1198480-01	-0.2612670 00	0.4865240-03	0.1198480-01	-0.2612670 00	0.4865240-03
9	0.1876990-01	-0.2157980 00	0.7629570-03	0.1876990-01	-0.2157980 00	0.7629570-03
10	0.2410900-01	-0.1524430 00	0.9768130-03	0.2410900-01	-0.1524430 00	0.9768130-03
11	0.2756430-01	-0.7614890-01	0.1116020-02	0.2756430-01	-0.7614890-01	0.1116020-02
12	0.2864770-01	0.0000000 00	0.1159240-02	0.2864770-01	0.0000000 00	0.1159240-02
13	-0.2784420-01	0.0000000 00	-0.1130350-02	-0.2784420-01	0.0000000 00	-0.1130350-02
14	-0.2683970-01	-0.7424340-01	-0.1087490-02	-0.2683970-01	-0.7424340-01	-0.1087490-02
15	-0.2339540-01	-0.1485230 00	-0.9495320-03	-0.2339540-01	-0.1485230 00	-0.9495320-03
16	-0.1810930-01	-0.2099750 00	-0.7377980-03	-0.1810930-01	-0.2099750 00	-0.7377980-03
17	-0.1140040-01	-0.2537370 00	-0.4864670-03	-0.1140040-01	-0.2537370 00	-0.4864670-03
18	-0.3889260-02	-0.2764020 00	-0.1586540-03	-0.3889260-02	-0.2764020 00	-0.1586540-03
19	0.3889260-02	-0.2764020 00	0.1586540-03	0.3889260-02	-0.2764020 00	0.1586540-03
20	0.1140040-01	-0.2537370 00	0.4864670-03	0.1140040-01	-0.2537370 00	0.4864670-03
21	0.1810930-01	-0.2099750 00	0.7377980-03	0.1810930-01	-0.2099750 00	0.7377980-03
22	0.2339540-01	-0.1485230 00	0.9495320-03	0.2339540-01	-0.1485230 00	0.9495320-03
23	0.2683970-01	-0.7424340-01	0.1087490-02	0.2683970-01	-0.7424340-01	0.1087490-02
24	0.2784420-01	0.0000000 00	0.1130350-02	0.2784420-01	0.0000000 00	0.1130350-02
25	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

ELEMENT RESULTANT FORCES (1) TENSION=COMP, UP=LEFT UP
(TOTAL)

ELEM #	AXIAL	MOMENT	SHEAR
1	-0.4701920-01	0.8902100 06	0.2472810 05
2	-0.4701920-01	0.2491100 07	0.1974090 05
3	-0.4701920-01	0.3732900 07	0.1476370 05
4	-0.4701920-01	0.4618630 07	0.0766560 04
5	-0.4701920-01	0.5139290 07	0.4779360 04
6	-0.4701920-01	0.5303870 07	-0.2077990 03
7	-0.4701920-01	0.5109370 07	-0.5194980 04
8	-0.4701920-01	0.4555790 07	-0.1016220 05
9	-0.4701920-01	0.3642130 07	-0.1816930 05
10	-0.4701920-01	0.2371400 07	-0.2015850 05
11	-0.4701920-01	0.8228830 06	-0.2493590 05
12	0.0000000 00	0.0000000 00	0.0000000 00
13	-0.4475270-01	0.8160260 06	0.2472810 05
14	-0.4475270-01	0.2350210 07	0.1994870 05
15	-0.4475270-01	0.3606980 07	0.1496190 05
16	-0.4475270-01	0.4604670 07	0.0974360 04
17	-0.4475270-01	0.5043290 07	0.4087180 04
18	-0.4475270-01	0.5222820 07	0.3627150-12
19	-0.4475270-01	0.5043290 07	-0.4087180 04
20	-0.4475270-01	0.4604670 07	-0.0974360 04
21	-0.4475270-01	0.3606980 07	-0.1496190 05
22	-0.4475270-01	0.2350210 07	-0.1994870 05
23	-0.4475270-01	0.8160260 06	-0.2472810 05
24	0.0000000 00	0.0000000 00	0.0000000 00

MODAL EXTERNAL REACTIONS (1)HUP:CC
(TOTAL)

NODE #	RX	RY	RZ
1	0.4701920-01	0.2472810 05	0.2940320 00
12	-0.4701920-01	0.2493590 05	-0.2750510 00
14	0.4475270-01	0.2472810 05	0.2654770 00
24	-0.4475270-01	0.2472810 05	-0.2654770 00
25	0.0000000 00	0.0000000 00	0.0000000 00

SERIAL #	DECK STEEL	TOP STEEL	BOTTOM STEEL
1	0.000000 00	0.000000 00	0.000000 00
2	0.000000 00	0.000000 00	0.000000 00
3	0.000000 00	0.000000 00	0.000000 00
4	0.000000 00	0.000000 00	0.000000 00
5	0.000000 00	0.000000 00	0.000000 00
6	0.000000 00	0.000000 00	0.000000 00
7	0.000000 00	0.000000 00	0.000000 00
8	0.000000 00	0.000000 00	0.000000 00
9	0.000000 00	=0.224230 04	0.000000 00
10	0.000000 00	=0.145970 04	0.000000 00
11	0.000000 00	=0.501210 03	=0.429290 03
12	0.000000 00	0.000000 00	0.000000 00
13	0.000000 00	=0.497030 03	0.425710 03
14	0.000000 00	=0.144670 04	0.000000 00
15	0.000000 00	=0.222030 04	0.000000 00
16	0.000000 00	0.000000 00	0.000000 00
17	0.000000 00	0.000000 00	0.000000 00
18	0.000000 00	0.000000 00	0.000000 00
19	0.000000 00	0.000000 00	0.000000 00
20	0.000000 00	0.000000 00	0.000000 00
21	0.000000 00	=0.222030 04	0.000000 00
22	0.000000 00	=0.144670 04	0.000000 00
23	0.000000 00	=0.497030 03	0.425710 03
24	0.000000 00	0.000000 00	0.000000 00

T I E L O I N G (N O L + 3)

[illegible]

CHECKING ELEMENTS

ELEMENT # 8						
#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS	
30	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
29	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
28	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
27	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
25	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
23	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
22	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
21	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07	
20	0.320000 02	0.440000 02	=0.126740300=03	=0.370331330 03	0.450000000 07	
19	0.507000 02	0.440000 02	=0.116067700=03	=0.526080450 03	0.450000000 07	
18	0.465000 02	0.440000 02	=0.107073240=03	=0.461626570 03	0.450000000 07	
17	0.463000 02	0.440000 02	=0.072397070=04	=0.437576680 03	0.450000000 07	
16	0.461000 02	0.440000 02	=0.874061760=06	=0.393277800 03	0.450000000 07	
15	0.461000 02	0.240000 02	=0.757847340=04	=0.341031300 03	0.450000000 07	
14	0.385000 02	0.240000 02	=0.623753750=04	=0.280669190 03	0.450000000 07	
13	0.335000 02	0.240000 02	=0.489660170=06	=0.220347070 03	0.450000000 07	
12	0.325000 02	0.240000 02	=0.355566580=04	=0.160004960 03	0.450000000 07	
11	0.295000 02	0.240000 02	=0.221472950=04	=0.996626460 02	0.450000000 07	
10	0.265000 02	0.240000 02	=0.873794100=05	=0.393207340 02	0.450000000 07	
9	0.235000 02	0.240000 02	0.467141760=05	0.210213790 02	0.450000000 07	
8	0.205000 02	0.240000 02	0.160677600=04	0.813634920 02	0.450000000 07	
7	0.175000 02	0.240000 02	0.314901380=04	0.141705610 03	0.450000000 07	
6	0.145000 02	0.240000 02	0.466694930=04	0.202047720 03	0.450000000 07	
5	0.115000 02	0.076000 02	0.574148940=04	0.259367020 03	0.450000000 07	
4	0.910000 01	0.076000 02	0.690363380=04	0.310663520 03	0.450000000 07	
3	0.680000 01	0.076000 02	0.806577830=04	0.362460020 03	0.450000000 07	
2	0.390000 01	0.076000 02	0.922792270=04	0.415256520 03	0.450000000 07	
1	0.130000 01	0.076000 02	0.103400670=03	0.467593020 03	0.450000000 07	

ELEMENT # 10

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
30	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
29	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
28	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
27	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
25	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
23	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
22	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
21	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
20	0.529000 02	0.440000 02	-0.124803740-03	-0.561818820 03	0.45000000 07
19	0.507000 02	0.440000 02	-0.115120480-03	-0.518042080 03	0.45000000 07
18	0.483000 02	0.440000 02	-0.105437140-03	-0.474467340 03	0.45000000 07
17	0.463000 02	0.440000 02	-0.095753910-04	-0.430492800 03	0.45000000 07
16	0.441000 02	0.440000 02	-0.886706350-04	-0.387317860 03	0.45000000 07
15	0.415000 02	0.240000 04	-0.746267830-04	-0.335420430 03	0.45000000 07
14	0.383000 02	0.240000 02	-0.614222980-04	-0.276400330 03	0.45000000 07
13	0.355000 02	0.240000 04	-0.482178290-04	-0.216480230 03	0.45000000 07
12	0.325000 02	0.240000 02	-0.350133810-04	-0.157560130 03	0.45000000 07
11	0.295000 02	0.240000 04	-0.218088940-04	-0.081400240 04	0.45000000 07
10	0.265000 02	0.240000 04	-0.860444720-05	-0.387199220 02	0.45000000 07
9	0.235000 02	0.240000 02	0.460000400-05	0.207001800 02	0.45000000 07
8	0.205000 02	0.240000 02	0.178045070-04	0.801202820 02	0.45000000 07
7	0.178000 02	0.240000 02	0.310086740-04	0.139540380 03	0.45000000 07
6	0.143000 02	0.240000 02	0.442134410-04	0.198900490 03	0.45000000 07
5	0.117000 02	0.676000 02	0.565376110-04	0.234414250 03	0.45000000 07
4	0.910000 01	0.676000 02	0.679814820-04	0.305916670 03	0.45000000 07
3	0.850000 01	0.676000 02	0.794253540-04	0.357414080 03	0.45000000 07
2	0.380000 01	0.676000 02	0.908692250-04	0.408411510 03	0.45000000 07
1	0.130000 01	0.676000 02	0.102313100-03	0.460408940 03	0.45000000 07

LOAD CASE # 2 STEP # 1/ 1 ITEM IN THE STEP 3 TOTAL # ITEM = 5

NAME SECTION PROPERTIES (TRANSDUCED TO BOTTOM)

(NON COMPOSITE SECTION)

BLK#	CENTROID	AREA	AREA MOM.	INERTIA
1	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
2	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
3	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
4	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
5	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
6	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
7	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
8	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
9	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
10	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
11	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
12	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00
13	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
14	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
15	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
16	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
17	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
18	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
19	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
20	0.2454510 02	0.7980000 03	0.1958700 05	0.7449140 06
21	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
22	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
23	0.2406560 02	0.8108890 03	0.2024430 05	0.7784380 06
24	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

NUAL DISPLACEMENTS (IN:UP:CC)						
(THIS STEP)						
(TOTAL)						
NODE #	X	Y	THETA	X	Y	THETA
1	0.1391350 00	0.0000000 00	0.3499020-02	0.1104870 00	0.0000000 00	0.2330130-02
2	0.1135370 00	0.2288240 00	0.2897190-02	0.8621510-01	0.1456180 00	0.1742310-02
3	0.8791930-01	0.4114360 00	0.2215360-02	0.8432750-01	0.2522500 00	0.1251630-02
4	0.6234170-01	0.5678360 00	0.1573530-02	0.4428940-01	0.3267050 00	0.8363000-03
5	0.3674400-01	0.6360240 00	0.4316950-03	0.2556600-01	0.3734250 00	0.4745340-03
6	0.1114640-01	0.6820000 00	0.2898620-03	0.7622410-02	0.3954820 00	0.1445340-03
7	-0.1449130-01	0.6797840 00	-0.3519700-03	-0.1007800-01	0.3943780 00	-0.1756700-03
8	-0.4004900-01	0.6213160 00	-0.9938030-03	-0.2806410-01	0.3700490 00	-0.5072790-03
9	-0.9364660-01	0.5386560 00	-0.1635640-02	-0.4687670-01	0.3208610 00	-0.8746780-03
10	-0.9114250-01	0.3960970 00	-0.2288790-02	-0.6703360-01	0.4436320 00	-0.1291970-02
11	-0.1166380 00	0.2098510 00	-0.2901940-02	-0.4905420-01	0.1338020 00	-0.1785920-02
12	-0.1391350 00	0.0000000 00	-0.3499020-02	-0.1104870 00	0.0000000 00	-0.2330130-02
13	0.1374820 00	0.0000000 00	0.3499020-02	0.1104870 00	0.0000000 00	0.2330130-02
14	0.1146860 00	0.2079010 00	0.2870880-02	0.8614630-01	0.1336590 00	0.1783390-02
15	0.8949010-01	0.3918110 00	0.2237730-02	0.8609470-01	0.2432880 00	0.1488400-02
16	0.6399420-01	0.5301350 00	0.1604580-02	0.4588480-01	0.3261590 00	0.8667630-03
17	0.3839650-01	0.6225590 00	0.4627490-03	0.2699610-01	0.3688220 00	0.4942620-03
18	0.1279880-01	0.6687710 00	0.3209160-03	0.8909570-02	0.3923980 00	0.1624630-03
19	-0.1279880-01	0.6687710 00	-0.3209160-03	-0.8909570-02	0.3923980 00	-0.1624630-03
20	-0.3839650-01	0.6225590 00	-0.4627490-03	-0.2699610-01	0.3688220 00	-0.4942620-03
21	-0.6399420-01	0.5301350 00	-0.1604580-02	-0.4588480-01	0.3261590 00	-0.8667630-03
22	-0.8949010-01	0.3918110 00	-0.2237730-02	-0.8609470-01	0.2432880 00	-0.1488400-02
23	-0.1146860 00	0.2079010 00	-0.2870880-02	-0.8614630-01	0.1336590 00	-0.1783390-02
24	-0.1374820 00	0.0000000 00	-0.3499020-02	-0.1104870 00	0.0000000 00	-0.2330130-02
25	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

ELEMENT RESULTANT PUNCHES			
(TOTAL)			
(+) TENSION, COMP, UP, LEFT UP			
ELM #	AXIAL	MOMENT	SHEAR
1	-0.4909600 06	-0.9687580 07	0.2472810 05
2	-0.4909600 06	-0.8086600 07	0.1974090 05
3	-0.4909600 06	-0.8644890 07	0.1475370 05
4	-0.4909600 06	-0.5962160 07	0.9766560 04
5	-0.4909600 06	-0.5638500 07	0.4779360 04
6	-0.4909600 06	-0.5273920 07	-0.2077990 03
7	-0.4909600 06	-0.5688420 07	-0.5194960 04
8	-0.4909600 06	-0.6022000 07	-0.1018220 05
9	-0.4910400 06	-0.7142860 07	-0.1518930 05
10	-0.4910400 06	-0.8614590 07	-0.2018680 05
11	-0.4919730 06	-0.9806830 07	-0.2493890 05
12	0.0000000 00	0.0000000 00	0.0000000 00
13	-0.4919730 06	-0.9813690 07	-0.2472810 05
14	-0.4910400 06	-0.8635790 07	0.1994870 05
15	-0.4910400 06	-0.7179020 07	0.1496150 05
16	-0.4909600 06	-0.6073120 07	0.9974360 04
17	-0.4909600 06	-0.5534590 07	0.4987180 04
18	-0.4909600 06	-0.5354970 07	-0.2964140-11
19	-0.4909600 06	-0.5534590 07	-0.4987180 04
20	-0.4909600 06	-0.6073120 07	-0.9974360 04
21	-0.4910400 06	-0.7179020 07	-0.1496150 05
22	-0.4910400 06	-0.8635790 07	-0.1994870 05
23	-0.4919730 06	-0.9813690 07	-0.2472810 05
24	0.0000000 00	0.0000000 00	0.0000000 00

NUAL EXTERNAL REACTIONS			
(TOTAL)			
(+) R:UP:CC			
NODE #	RX	RY	RZ
1	-0.1492130-02	0.2472810 05	-0.9818900-02
12	0.1492130-02	0.2493590 05	0.9178540-02
13	-0.1423220-02	0.2472810 05	-0.8886180-02
24	0.1423220-02	0.2472810 05	0.8886180-02
25	0.0000000 00	0.0000000 00	0.0000000 00

CHACALING LENGTH 6 1/2 FT

BIRDS RUPTRU STRAIN = 0.130000-03
DELE RUPTRU STRAIN = 0.130000-03

[illegible]

CRACKING PATTERN

BINDER RUPTURE STRAIN = 0.130000-03
DECK RUPTURE STRAIN = 0.130000-03

[illegible]

CRACK ANGLES (DEGREES)

[illegible]

ITEM #	ORCA STEEL	TUM STEEL	WCTUM STEEL
1	0.000000 00	0.000000 00	0.000000 00
4	0.000000 00	0.000000 00	0.000000 00
5	0.000000 00	0.000000 00	0.000000 00
6	0.000000 00	0.000000 00	0.000000 00
8	0.000000 00	0.000000 00	0.000000 00
9	0.000000 00	0.000000 00	0.000000 00
7	0.000000 00	0.000000 00	0.000000 00
8	0.000000 00	0.000000 00	0.000000 00
9	0.000000 00	0.000000 00	0.000000 00
10	0.000000 00	0.127710 03	0.000000 00
11	0.000000 00	0.128750 04	0.000000 00
12	0.000000 00	0.000000 00	0.000000 00
13	0.000000 00	0.128750 04	0.000000 00
14	0.000000 00	0.129010 04	0.000000 00
15	0.000000 00	0.128750 03	0.000000 00
16	0.000000 00	0.000000 00	0.000000 00
17	0.000000 00	0.000000 00	0.000000 00
18	0.000000 00	0.000000 00	0.000000 00
19	0.000000 00	0.000000 00	0.000000 00
20	0.000000 00	0.000000 00	0.000000 00
21	0.000000 00	0.128750 03	0.000000 00
22	0.000000 00	0.129010 04	0.000000 00
23	0.000000 00	0.128750 04	0.000000 00
24	0.000000 00	0.000000 00	0.000000 00

FIELDING (INGL03)

[illegible]

CHECKING ELEMENTS

ELEMENT # 6					
ID	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
30	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
29	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
28	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
27	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
25	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
23	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
22	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
21	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
20	0.000000 02	0.000000 02	-0.100947940-04	-0.481465710 02	0.45000000 07
19	0.007000 02	0.000000 02	-0.206728110-04	-0.921274510 02	0.45000000 07
18	0.045000 02	0.000000 02	-0.302350240-04	-0.136126730 03	0.45000000 07
17	0.063000 02	0.000000 02	-0.400284670-04	-0.101129810 03	0.45000000 07
16	0.081000 02	0.000000 02	-0.498084650-04	-0.224130840 03	0.45000000 07
15	0.018000 02	0.200000 02	-0.613627040-04	-0.276132170 03	0.45000000 07
14	0.395000 02	0.200000 02	-0.748688440-04	-0.336133440 03	0.45000000 07
13	0.395000 02	0.200000 02	-0.860300230-04	-0.396135110 03	0.45000000 07
12	0.325000 02	0.200000 02	-0.101363840-02	-0.456136580 03	0.45000000 07
11	0.295000 02	0.200000 02	-0.114697350-02	-0.516138400 03	0.45000000 07
10	0.265000 02	0.200000 02	-0.126031010-02	-0.576139520 03	0.45000000 07
9	0.235000 02	0.200000 02	-0.141364670-02	-0.636141000 03	0.45000000 07
8	0.205000 02	0.200000 02	-0.154688230-02	-0.696142470 03	0.45000000 07
7	0.175000 02	0.200000 02	-0.168031940-02	-0.756143930 03	0.45000000 07
6	0.145000 02	0.200000 02	-0.181363650-02	-0.816145420 03	0.45000000 07
5	0.117000 02	0.676000 02	-0.193810400-02	-0.872146790 03	0.45000000 07
4	0.061000 01	0.676000 02	-0.205368240-02	-0.924148070 03	0.45000000 07
3	0.030000 01	0.676000 02	-0.216922080-02	-0.978149350 03	0.45000000 07
2	0.390000 01	0.676000 02	-0.228677940-02	-0.102815060 04	0.45000000 07
1	0.130000 01	0.676000 02	-0.240033760-02	-0.108015180 04	0.45000000 07

ELEMENT # 16

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
27	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
23	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
22	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
21	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
20	0.029000 02	0.440000 02	-0.875023400-03	-0.304120570 02	0.45000000 07
19	0.507000 02	0.440000 02	-0.190800000-04	-0.040092790 02	0.45000000 07
18	0.409000 02	0.440000 02	-0.280147780-04	-0.124760500 03	0.45000000 07
17	0.403000 02	0.440000 02	-0.305304400-04	-0.173443720 03	0.45000000 07
16	0.441000 02	0.440000 02	-0.484713210-04	-0.218120940 03	0.45000000 07
15	0.415000 02	0.440000 02	-0.602047330-04	-0.270921300 03	0.45000000 07
14	0.385000 02	0.440000 02	-0.737328300-04	-0.331044780 03	0.45000000 07
13	0.355000 02	0.440000 02	-0.872818370-04	-0.394760270 03	0.45000000 07
12	0.325000 02	0.440000 02	-0.100820390-03	-0.453091750 03	0.45000000 07
11	0.295000 02	0.440000 02	-0.114350940-03	-0.514615240 03	0.45000000 07
10	0.265000 02	0.440000 02	-0.127097400-03	-0.575538720 03	0.45000000 07
9	0.235000 02	0.440000 02	-0.141430050-03	-0.636462200 03	0.45000000 07
8	0.205000 02	0.440000 02	-0.154974000-03	-0.697385000 03	0.45000000 07
7	0.175000 02	0.440000 02	-0.168013150-03	-0.758309170 03	0.45000000 07
6	0.145000 02	0.440000 02	-0.182051700-03	-0.819232000 03	0.45000000 07
5	0.117000 02	0.470000 02	-0.194087680-03	-0.876094500 03	0.45000000 07
4	0.091000 01	0.470000 02	-0.206421100-03	-0.924094930 03	0.45000000 07
3	0.063000 01	0.470000 02	-0.218154510-03	-0.961095280 03	0.45000000 07
2	0.039000 01	0.470000 02	-0.229087920-03	-0.1034450 04	0.45000000 07
1	0.130000 01	0.470000 02	-0.241021330-03	-0.108729600 04	0.45000000 07

LOAD CASE # J STEP # 1/ 1 ITER. IN THE STEP= 3 TOTAL # ITER.= 8

NEW SECTION PROPERTIES (TRANSFORMED TO BOTTOM)

(NON COMPOSITE SECTION)

ELEM #	CENTROID	AREA	AREA MOM.	INERTIA
1	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
2	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
3	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
4	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
5	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
6	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
7	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
8	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
9	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
10	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
11	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
12	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00
13	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
14	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
15	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
16	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
17	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
18	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
19	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
20	0.2454510 02	0.7980000 03	0.1958700 08	0.7449140 06
21	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
22	0.2490560 02	0.8108890 03	0.2024430 05	0.7784380 06
23	0.2460630 02	0.8237780 03	0.2027010 05	0.7784900 06
24	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

 NODAL DISPLACEMENTS (+)IN:UP:CC
 (THIS STEP)

(TOTAL)

NODE #	X	Y	THETA	X	Y	THETA
1	-0.1478490-01	0.0000000 00	-0.6148490-03	0.9569200-01	0.0000000 00	0.1715240-02
2	-0.1411030-01	-0.4387660-01	-0.5864330-03	0.7210490-01	0.1015410 00	0.1155880-02
3	-0.1219430-01	-0.8374130-01	-0.5089250-03	0.5213340-01	0.1665000 00	0.7447050-03
4	-0.9323230-02	-0.1163270 00	-0.3877830-03	0.3496620-01	0.2103780 00	0.4445170-03
5	-0.8773260-02	-0.1391930 00	-0.2604670-03	0.1979270-01	0.2344240 00	0.2340930-03
6	-0.1820560-02	-0.1507240 00	-0.7643750-04	0.5801860-02	0.2447560 00	0.6810080-04
7	0.2256750-02	-0.1501280 00	0.9284660-04	-0.7617280-02	0.2442500 00	-0.8264490-04
8	0.6188460-02	-0.1374400 00	0.2889190-03	-0.2187570-01	0.2320090 00	-0.2513600-03
9	0.9692400-02	-0.1135190 00	0.4013250-03	-0.3718430-01	0.2073140 00	-0.4713530-03
10	0.1244980-01	-0.8019390-01	0.5137960-03	-0.3458380-01	0.1634560 00	-0.7781770-03
11	0.1424470-01	-0.4005890-01	0.5870060-03	-0.7480950-01	0.0374310-01	-0.1198910-02
12	0.1478490-01	0.0000000 00	0.6087720-03	-0.9569200-01	0.0000000 00	-0.1691200-02
13	-0.1440650-01	0.0000000 00	-0.5869740-03	0.9516140-01	0.0000000 00	0.1704230-02
14	-0.1286090-01	-0.3405740-01	-0.5719980-03	0.7426550-01	0.9459450-01	0.1211390-02
15	-0.1208200-01	-0.7813040-01	-0.4894630-03	0.5401260-01	0.1651960 00	0.7887570-03
16	-0.9352000-02	-0.1104570 00	-0.3860870-03	0.3453280-01	0.2097020 00	0.4786950-03
17	-0.5887370-02	-0.1334780 00	-0.2643130-03	0.2110870-01	0.2353440 00	0.2539600-03
18	-0.2008460-02	-0.1454010 00	-0.8336780-04	0.4901080-02	0.2449660 00	0.7911480-04
19	0.2008460-02	-0.1454010 00	0.8336780-04	-0.4901080-02	0.2449660 00	-0.7911480-04
20	0.5887370-02	-0.1334780 00	0.2643130-03	-0.2110870-01	0.2353440 00	-0.2539600-03
21	0.9352000-02	-0.1104570 00	0.3860870-03	-0.3453280-01	0.2097020 00	-0.4786950-03
22	0.1208200-01	-0.7813020-01	0.4894630-03	-0.5401260-01	0.1651960 00	-0.7887570-03
23	0.1286090-01	-0.3405740-01	0.5719980-03	-0.7426550-01	0.9459450-01	-0.1211390-02
24	0.1440650-01	0.0000000 00	0.5869740-03	-0.9516140-01	0.0000000 00	-0.1704230-02
25	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

 ELEMENT RESULTANT FORCES (+) TENSION=COMP,UP=DOWN
 (TOTAL)

ELEM #	AXIAL	MOMENT	SHEAR
1	-0.4909800 06	-0.9205660 07	0.3811470 05
2	-0.4909800 06	-0.6738130 07	0.3042770 05
3	-0.4909800 06	-0.4824070 07	0.2274070 05
4	-0.4909800 06	-0.3463470 07	0.1505370 05
5	-0.4909800 06	-0.2656330 07	0.7366720 04
6	-0.4909800 06	-0.2402660 07	-0.3202920 03
7	-0.4909800 06	-0.2702450 07	-0.8007300 04
8	-0.4909800 06	-0.3955710 07	-0.1566430 05
9	-0.4910400 06	-0.5170640 07	-0.2338130 05
10	-0.4910400 06	-0.7130820 07	-0.3106830 05
11	-0.4919730 06	-0.9361360 07	-0.3843500 05
12	0.0000000 00	0.0000000 00	0.0000000 00
13	-0.4919730 06	-0.9371930 07	0.3811470 05
14	-0.4910400 06	-0.7183490 07	0.3074800 05
15	-0.4910400 06	-0.5226370 07	0.2306100 05
16	-0.4909800 06	-0.3634500 07	0.1527400 05
17	-0.4909800 06	-0.2804300 07	0.7687010 04
18	-0.4909800 06	-0.2527570 07	0.6344270-13
19	-0.4909800 06	-0.2804300 07	-0.7687010 04
20	-0.4909800 06	-0.3634500 07	-0.1527400 05
21	-0.4910400 06	-0.5226370 07	-0.2306100 05
22	-0.4910400 06	-0.7183490 07	-0.3074800 05
23	-0.4919730 06	-0.9371930 07	-0.3811470 05
24	0.0000000 00	0.0000000 00	0.0000000 00

 NODAL EXTERNAL REACTIONS
 (TOTAL)

(+)IN:UP:CC

NODE #	RX	RY	RZ
1	0.1734000-03	0.3811470 05	-0.9637400-01
12	-0.1734000-03	0.3843500 05	0.7830970-01
13	0.1831800-03	0.3811470 05	-0.7766610-01
24	-0.1831800-03	0.3811470 05	0.7766610-01
25	0.0000000 00	0.0000000 00	0.0000000 00

ELEM #	DECK STEEL	TOP STEEL	BOTTOM STEEL
1	0.000000 00	0.000000 00	0.000000 00
2	0.000000 00	0.000000 00	0.000000 00
3	0.000000 00	0.000000 00	0.000000 00
4	0.000000 00	0.000000 00	0.000000 00
5	0.000000 00	0.000000 00	0.000000 00
6	0.000000 00	0.000000 00	0.000000 00
7	0.000000 00	0.000000 00	0.000000 00
8	0.000000 00	0.000000 00	0.000000 00
9	0.000000 00	-0.703460 03	0.000000 00
10	0.000000 00	0.496150 03	0.000000 00
11	0.000000 00	0.163610 04	-0.874300 04
12	0.000000 00	0.000000 00	0.000000 00
13	0.000000 00	0.186250 04	-0.874830 04
14	0.000000 00	0.516170 03	0.000000 00
15	0.000000 00	-0.671290 03	0.000000 00
16	0.000000 00	0.000000 00	0.000000 00
17	0.000000 00	0.000000 00	0.000000 00
18	0.000000 00	0.000000 00	0.000000 00
19	0.000000 00	0.000000 00	0.000000 00
20	0.000000 00	0.000000 00	0.000000 00
21	0.000000 00	-0.671290 03	0.000000 00
22	0.000000 00	0.516170 03	0.000000 00
23	0.000000 00	0.186250 04	-0.874830 04
24	0.000000 00	0.000000 00	0.000000 00

YIELDING (NGL#3)

ELEM #	HEIMP. STEEL (U-TIE) & LAYERS																							
1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
2	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
3	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
4	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
5	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
6	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
7	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
8	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
9	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
10	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
11	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
12	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
13	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
14	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
15	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
16	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
17	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
18	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
19	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
20	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
21	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
22	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
23	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	
24	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	1	

CHECKING ELEMENTS

ELEMENT

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
34	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
29	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
28	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
27	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
26	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
25	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
24	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
23	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
22	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
21	0.000000 00	0.000000 00	0.000000000 00	0.000000000 00	0.350000000 07
20	0.529000 02	0.440000 02	-0.784131530-04	-0.352859190 03	0.450000000 07
19	0.507000 02	0.440000 02	-0.830186610-04	-0.373583970 03	0.450000000 07
18	0.485000 02	0.440000 02	-0.876241680-04	-0.394308760 03	0.450000000 07
17	0.463000 02	0.440000 02	-0.922296760-04	-0.415033540 03	0.450000000 07
16	0.441000 02	0.440000 02	-0.968351830-04	-0.435758320 03	0.450000000 07
15	0.419000 02	0.240000 02	-0.102270060-03	-0.460251250 03	0.450000000 07
14	0.397000 02	0.240000 02	-0.106558290-03	-0.488512340 03	0.450000000 07
13	0.375000 02	0.240000 02	-0.114836530-03	-0.516773340 03	0.450000000 07
12	0.353000 02	0.240000 02	-0.121118770-03	-0.545034460 03	0.450000000 07
11	0.331000 02	0.240000 02	-0.127390010-03	-0.573295530 03	0.450000000 07
10	0.309000 02	0.240000 02	-0.13367240-03	-0.601556600 03	0.450000000 07
9	0.287000 02	0.240000 02	-0.139959480-03	-0.629817670 03	0.450000000 07
8	0.265000 02	0.240000 02	-0.146236720-03	-0.658078730 03	0.450000000 07
7	0.175000 02	0.240000 02	-0.152519980-03	-0.686339800 03	0.450000000 07
6	0.153000 02	0.240000 02	-0.158800190-03	-0.714600870 03	0.450000000 07
5	0.131000 02	0.240000 02	-0.165080400-03	-0.742861940 03	0.450000000 07
4	0.109000 01	0.240000 02	-0.171360610-03	-0.771123010 03	0.450000000 07
3	0.087000 01	0.240000 02	-0.177640820-03	-0.799384080 03	0.450000000 07
2	0.065000 01	0.240000 02	-0.183921030-03	-0.827645150 03	0.450000000 07
1	0.110000 01	0.240000 02	-0.188433240-03	-0.834944500 03	0.450000000 07

ELEMENT 9 18

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
30	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
29	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
28	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
27	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
26	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
25	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
24	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
23	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
22	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
21	0.000000 00	0.000000 00	0.00000000 00	0.00000000 00	0.35000000 07
20	0.329000 02	0.440000 02	-0.75441676D-04	-0.33948844D 03	0.45000000 07
19	0.307000 02	0.440000 02	-0.80276672D-04	-0.38124302D 03	0.45000000 07
18	0.445000 02	0.440000 02	-0.83111486D-04	-0.38300160D 03	0.45000000 07
17	0.463000 02	0.440000 02	-0.89946284D-04	-0.40475419D 03	0.45000000 07
16	0.441000 02	0.440000 02	-0.94741059D-04	-0.42651471D 03	0.45000000 07
15	0.419000 02	0.440000 02	-0.10049491D-03	-0.45222709D 03	0.45000000 07
14	0.389000 02	0.440000 02	-0.10746781D-03	-0.46189516D 03	0.45000000 07
13	0.389000 02	0.440000 02	-0.11368072D-03	-0.51156322D 03	0.45000000 07
12	0.325000 02	0.440000 02	-0.14027364D-03	-0.54123129D 03	0.45000000 07
11	0.295000 02	0.440000 02	-0.14666520D-03	-0.57069935D 03	0.45000000 07
10	0.269000 02	0.440000 02	-0.13345440D-03	-0.60058742D 03	0.45000000 07
9	0.239000 02	0.440000 02	-0.14005233D-03	-0.63023540D 03	0.45000000 07
8	0.209000 02	0.440000 02	-0.14664523D-03	-0.65990355D 03	0.45000000 07
7	0.179000 02	0.440000 02	-0.15323814D-03	-0.68957162D 03	0.45000000 07
6	0.149000 02	0.440000 02	-0.15983104D-03	-0.71923968D 03	0.45000000 07
5	0.119000 02	0.440000 02	-0.16538442D-03	-0.74892986D 03	0.45000000 07
4	0.910000 01	0.676000 02	-0.17169827D-03	-0.77264220D 03	0.45000000 07
3	0.680000 01	0.676000 02	-0.17741212D-03	-0.79835453D 03	0.45000000 07
2	0.390000 01	0.676000 02	-0.18312597D-03	-0.82406685D 03	0.45000000 07
1	0.130000 01	0.676000 02	-0.18883482D-03	-0.84977917D 03	0.45000000 07

 LOAD CASE # 4 STEP #123/444 ITER. IN THE STEP 0 TOTAL # ITER. 1290

 NEW SECTION PROPERTIES (TRANSFORMED TO BOTTOM)
 (COMPOSITE SECTION)

ELEM #	CENTROID	AREA	AREA MOM.	INERTIA
1	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
2	0.3800510 02	0.1177500 04	0.4121850 05	0.1978920 07
3	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
4	0.3260070 02	0.3995000 03	0.3230150 05	0.1753720 07
5	0.5657400 02	0.4235000 03	0.2395910 05	0.1357150 07
6	0.5700000 02	0.3795000 03	0.2163150 05	0.1234000 07
7	0.5687400 02	0.4235000 03	0.2395910 05	0.1357150 07
8	0.5388070 02	0.3995000 03	0.3230150 05	0.1753720 07
9	0.2917630 02	0.1190390 04	0.4187580 05	0.4012440 07
10	0.3817630 02	0.1190390 04	0.4187580 05	0.4012440 07
11	0.2934480 02	0.1232280 04	0.4355460 05	0.4106710 07
12	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00
13	0.2934480 02	0.1232280 04	0.4355460 05	0.4106710 07
14	0.3817630 02	0.1190390 04	0.4187580 05	0.4012440 07
15	0.3817630 02	0.1190390 04	0.4187580 05	0.4012440 07
16	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
17	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
18	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
19	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
20	0.3500510 02	0.1177500 04	0.4121850 05	0.1978920 07
21	0.3817630 02	0.1190390 04	0.4187580 05	0.4012440 07
22	0.2917630 02	0.1190390 04	0.4187580 05	0.4012440 07
23	0.2934480 02	0.1232280 04	0.4355460 05	0.4106710 07
24	0.0000000 00	0.0000000 00	0.0000000 00	0.0000000 00

279

 FINAL CABLE MOMENTIES (UP TO THIS STEP)

ELEM #	FORCE	STRESS	STRAIN	E MOD
1	0.496000 06	0.182570 06	0.652040-02	0.280000 06
2	0.506740 06	0.186300 06	0.653370-02	0.280000 06
3	0.516620 06	0.189900 06	0.655710-02	0.280000 06
4	0.526580 06	0.231370 06	0.627040-02	0.280000 06
5	0.536570 06	0.253360 06	0.124440-01	0.310000 07
6	0.707600 06	0.260150 06	0.184250-01	0.120000 06
7	0.686520 06	0.252400 06	0.125700-01	0.310000 07
8	0.623100 06	0.229080 06	0.618140-02	0.280000 06
9	0.514080 06	0.184000 06	0.675000-02	0.280000 06
10	0.506030 06	0.180040 06	0.664440-02	0.280000 06
11	0.496930 06	0.182700 06	0.652510-02	0.280000 06
12	0.000000 00	0.000000 00	0.000000 00	0.000000 00
13	0.492520 06	0.181080 06	0.646700-02	0.280000 06
14	0.492690 06	0.181140 06	0.646920-02	0.280000 06
15	0.492570 06	0.181480 06	0.646800-02	0.280000 06
16	0.494170 06	0.181880 06	0.646800-02	0.280000 06
17	0.494530 06	0.181820 06	0.646360-02	0.280000 06
18	0.494660 06	0.181870 06	0.646530-02	0.280000 06
19	0.494530 06	0.181820 06	0.646360-02	0.280000 06
20	0.494170 06	0.181880 06	0.646800-02	0.280000 06
21	0.493970 06	0.181480 06	0.646800-02	0.280000 06
22	0.492690 06	0.181140 06	0.646920-02	0.280000 06
23	0.492520 06	0.181080 06	0.646700-02	0.280000 06
24	0.000000 00	0.000000 00	0.000000 00	0.000000 00

 STRAINS AT T-M MOMENTS

(UP TO THIS STEP)

(MAX. REACHED)

ELEM #	BOTTOM GIRDER	TOP GIRDER	BOTTOM DECK	TOP DECK	BOTTOM GIRDER	TOP GIRDER	BOTTOM DECK	TOP DECK
1	-0.255880-03	0.314280-04	-0.4053080-04	-0.3302430-04	-0.3371000-03	0.1037540-03	-0.4053080-04	-0.3302430-04
2	-0.7593380-04	-0.8245130-04	-0.1134480-03	-0.1484350-03	-0.3039940-03	-0.8245130-04	-0.1134480-03	-0.1484350-03
3	0.6350240-04	-0.1864970-03	-0.1700060-03	-0.222440-03	-0.2783070-03	-0.1864970-03	-0.1700060-03	-0.222440-03
4	0.1887420-02	-0.2637940-03	-0.2128900-03	-0.485620-03	0.1887420-02	-0.2637940-03	-0.2128900-03	-0.485620-03
5	0.6636230-02	-0.9735920-04	-0.2755560-04	-0.7495780-03	0.6636230-02	-0.9735920-04	-0.2755560-04	-0.7495780-03
6	0.1013970-01	0.7486960-04	0.1509800-03	0.9798940-03	0.1013970-01	0.7486960-04	0.1509800-03	0.9798940-03
7	0.6240700-02	-0.1127470-03	-0.4404280-04	-0.7640430-03	0.6240700-02	-0.1127470-03	-0.4404280-04	-0.7640430-03
8	0.151800-02	-0.2594720-03	-0.2118470-03	-0.356770-03	0.151800-02	-0.2594720-03	-0.2118470-03	-0.356770-03
9	0.5266650-04	-0.1749400-03	-0.1623360-03	-0.2142570-03	-0.2794570-03	-0.1749400-03	-0.1623360-03	-0.2142570-03
10	-0.8937280-04	-0.7171430-04	-0.1063530-03	-0.1394530-03	-0.3058420-03	-0.7171430-04	-0.1063530-03	-0.1394530-03
11	-0.2528930-03	0.3159210-04	-0.3478910-04	-0.4571140-04	-0.3247390-03	0.3159210-04	-0.3478910-04	-0.4571140-04
12	0.000000 00	0.000000 00	-0.3498080-02	0.432440-02	0.000000 00	0.000000 00	-0.3498080-02	0.432440-02
13	0.316060-03	0.8662960-04	0.2029020-08	0.4332100-08	-0.3248730-03	0.8662960-04	0.2029020-08	0.4332100-08
14	0.2813680-03	0.3541100-04	0.2130470-08	0.2451340-08	-0.3042730-03	0.3541100-04	0.2130470-08	0.2451340-08
15	-0.2427760-03	-0.1024670-04	0.2129150-08	0.2449080-08	-0.2806920-03	-0.1024670-04	0.2129150-08	0.2449080-08
16	-0.2142240-03	-0.4567630-04	0.2163330-08	0.2487260-08	-0.2643430-03	-0.4567630-04	0.2163330-08	0.2487260-08
17	-0.1973290-03	-0.6618580-04	0.2161590-08	0.2484980-08	-0.2512020-03	-0.6618580-04	0.2161590-08	0.2484980-08
18	-0.1916970-03	-0.7302230-04	0.2159450-08	0.2482700-08	-0.2474880-03	-0.7302230-04	0.2159450-08	0.2482700-08
19	-0.1973290-03	-0.6618580-04	0.2158110-08	0.2480420-08	-0.2512040-03	-0.6618580-04	0.2158110-08	0.2480420-08
20	-0.2142240-03	-0.4567630-04	0.2156370-08	0.2478150-08	-0.2643430-03	-0.4567630-04	0.2156370-08	0.2478150-08
21	-0.2427760-03	-0.1024670-04	0.2118450-08	0.2435990-08	-0.2806920-03	-0.1024670-04	0.2118450-08	0.2435990-08
22	-0.2813680-03	0.3541100-04	0.2117140-08	0.2433340-08	-0.3042730-03	0.3541100-04	0.2117140-08	0.2433340-08
23	-0.2813680-03	0.3541100-04	0.2012970-08	0.2311010-08	-0.3248730-03	0.3541100-04	0.2012970-08	0.2311010-08
24	0.000000 00	0.000000 00	0.1352490-07	-0.7044710-08	0.000000 00	0.000000 00	0.1352490-07	-0.7044710-08

CHACKING ELEMENTS

ELEMENT # 8

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
30	0.597000 02	0.432000 02	-0.923350020-03	-0.323172510 04	0.350000000 07
29	0.591000 02	0.432000 02	-0.810262440-03	-0.283591930 04	0.350000000 07
28	0.585000 02	0.432000 02	-0.697175270-03	-0.244011340 04	0.350000000 07
27	0.579000 02	0.432000 02	-0.584087400-03	-0.204430760 04	0.350000000 07
26	0.573000 02	0.432000 02	-0.471000520-03	-0.164950180 04	0.350000000 07
25	0.567000 02	0.432000 02	-0.357913150-03	-0.125484630 04	0.350000000 07
24	0.561000 02	0.432000 02	-0.244825740-03	-0.086990220 04	0.350000000 07
23	0.555000 02	0.432000 02	-0.131736410-03	-0.048044420 04	0.350000000 07
22	0.549000 02	0.432000 02	-0.186510320-04	-0.052786120 04	0.350000000 07
21	0.543000 02	0.432000 02	0.944363410-04	0.330527190 03	0.350000000 07
20	0.529000 02	0.440000 02	0.279643710-03	0.000000000 00	0.000000000 00
19	0.507000 02	0.440000 02	0.889441920-03	0.000000000 00	0.000000000 00
18	0.485000 02	0.440000 02	0.109990010-02	0.000000000 00	0.000000000 00
17	0.463000 02	0.440000 02	0.151003830-02	0.000000000 00	0.000000000 00
16	0.441000 02	0.440000 02	0.172008650-02	0.000000000 00	0.000000000 00
15	0.419000 02	0.240000 02	0.240468890-02	0.000000000 00	0.000000000 00
14	0.397000 02	0.240000 02	0.296384550-02	0.000000000 00	0.000000000 00
13	0.375000 02	0.240000 02	0.352300220-02	0.000000000 00	0.000000000 00
12	0.353000 02	0.240000 02	0.408215880-02	0.000000000 00	0.000000000 00
11	0.331000 02	0.240000 02	0.464131540-02	0.000000000 00	0.000000000 00
10	0.309000 02	0.240000 02	0.520047210-02	0.000000000 00	0.000000000 00
9	0.287000 02	0.240000 02	0.575962670-02	0.000000000 00	0.000000000 00
8	0.265000 02	0.240000 02	0.631878530-02	0.000000000 00	0.000000000 00
7	0.243000 02	0.240000 02	0.687794190-02	0.000000000 00	0.000000000 00
6	0.221000 02	0.240000 02	0.743709860-02	0.000000000 00	0.000000000 00
5	0.199000 02	0.240000 02	0.799625710-02	0.000000000 00	0.000000000 00
4	0.177000 02	0.240000 02	0.855541560-02	0.000000000 00	0.000000000 00
3	0.155000 02	0.240000 02	0.911457410-02	0.000000000 00	0.000000000 00
2	0.133000 02	0.240000 02	0.967373260-02	0.000000000 00	0.000000000 00
1	0.111000 02	0.240000 02	0.020000000 00	0.000000000 00	0.000000000 00

ELEMENT # 18

#	POSITION	LAYER AREA	STRAIN	STRESS	INST. MODULUS
30	0.597000 02	0.432000 02	0.246656180-02	0.863298600-02	0.350000000 07
29	0.591000 02	0.432000 02	0.243427640-02	0.851496750-02	0.350000000 07
28	0.585000 02	0.432000 02	0.240199100-02	0.840648840-02	0.350000000 07
27	0.579000 02	0.432000 02	0.236970550-02	0.829396920-02	0.350000000 07
26	0.573000 02	0.432000 02	0.233742000-02	0.818097010-02	0.350000000 07
25	0.567000 02	0.432000 02	0.230513460-02	0.806797100-02	0.350000000 07
24	0.561000 02	0.432000 02	0.227284910-02	0.795497180-02	0.350000000 07
23	0.555000 02	0.432000 02	0.224056360-02	0.784197270-02	0.350000000 07
22	0.549000 02	0.432000 02	0.220827840-02	0.772897360-02	0.350000000 07
21	0.543000 02	0.432000 02	0.217599270-02	0.761597440-02	0.350000000 07
20	0.529000 02	0.440000 02	-0.754397750-04	-0.339478900 03	0.450000000 07
19	0.507000 02	0.440000 02	-0.802746890-04	-0.361238100 03	0.450000000 07
18	0.485000 02	0.440000 02	-0.851096040-04	-0.382992220 03	0.450000000 07
17	0.463000 02	0.440000 02	-0.899445180-04	-0.404750330 03	0.450000000 07
16	0.441000 02	0.440000 02	-0.947796320-04	-0.426507450 03	0.450000000 07
15	0.419000 02	0.240000 02	-0.100693420-03	-0.492220400 03	0.450000000 07
14	0.397000 02	0.240000 02	-0.107086490-03	-0.481889190 03	0.450000000 07
13	0.375000 02	0.240000 02	-0.113679550-03	-0.511567940 03	0.450000000 07
12	0.353000 02	0.240000 02	-0.120272620-03	-0.541246780 03	0.450000000 07
11	0.331000 02	0.240000 02	-0.126865860-03	-0.570895570 03	0.450000000 07
10	0.309000 02	0.240000 02	-0.133458750-03	-0.600564360 03	0.450000000 07
9	0.287000 02	0.240000 02	-0.140051810-03	-0.630223150 03	0.450000000 07
8	0.265000 02	0.240000 02	-0.146644880-03	-0.659901940 03	0.450000000 07
7	0.243000 02	0.240000 02	-0.153237940-03	-0.689570740 03	0.450000000 07
6	0.221000 02	0.240000 02	-0.159831010-03	-0.719239530 03	0.450000000 07
5	0.199000 02	0.240000 02	-0.166424080-03	-0.748908320 03	0.450000000 07
4	0.177000 02	0.240000 02	-0.173017150-03	-0.778577110 03	0.450000000 07
3	0.155000 02	0.240000 02	-0.179610220-03	-0.808245900 03	0.450000000 07
2	0.133000 02	0.240000 02	-0.186203290-03	-0.837914690 03	0.450000000 07
1	0.111000 02	0.240000 02	-0.192796360-03	-0.867583480 03	0.450000000 07

.....
 M O M E N T - C U R V A T U R E - D E F L E C T I O N

E L E M E N T # 6

STEP #	MOMENT	CURVATURE	DEFLECTION	LOAD FACTOR	CURT. TIME	ITERATIONS
1	0.5300 07	0.4470-05	-0.2880 00	0.1000 01	0.0000 00	4
2	-0.5270 07	-0.4440-05	0.3450 00	0.1000 01	0.0000 00	3
3	-0.2400 07	-0.2040-05	0.2450 00	0.1000 01	0.0000 00	3
4	-0.4100 06	-0.1280-05	0.1950 00	0.2800-01	0.0000 00	4
5	0.1320 07	0.5160-06	0.1450 00	0.5120-01	0.0000 00	3
6	0.2440 07	0.4570-06	0.9480-01	0.7830-01	0.0000 00	6
7	0.5370 07	0.1030-05	0.4490-01	0.1010 00	0.0000 00	10
8	0.7490 07	0.1810-05	-0.5060-02	0.1470 00	0.0000 00	8
9	0.9220 07	0.2580-05	-0.5500-01	0.1920 00	0.0000 00	4
10	0.1110 08	0.3350-05	-0.1050 00	0.1770 00	0.0000 00	6
11	0.1310 08	0.4130-05	-0.1550 00	0.2020 00	0.0000 00	4
12	0.1500 08	0.4900-05	-0.2050 00	0.2270 00	0.0000 00	4
13	0.1690 08	0.5680-05	-0.2550 00	0.2520 00	0.0000 00	4
14	0.1890 08	0.6450-05	-0.3050 00	0.2780 00	0.0000 00	9
15	0.2080 08	0.7230-05	-0.3540 00	0.3030 00	0.0000 00	4
16	0.1810 08	0.1480-04	-0.4040 00	0.2880 00	0.0000 00	71
17	0.1880 08	0.1750-04	-0.4540 00	0.2770 00	0.0000 00	5
18	0.1940 08	0.2030-04	-0.5040 00	0.2850 00	0.0000 00	6
19	0.2000 08	0.2310-04	-0.5540 00	0.2920 00	0.0000 00	5
20	0.2060 08	0.2570-04	-0.6040 00	0.3020 00	0.0000 00	4
21	0.2130 08	0.2860-04	-0.6540 00	0.3100 00	0.0000 00	5
22	0.1930 08	0.2080-04	-0.7040 00	0.2820 00	0.0000 00	86
23	0.1980 08	0.2180-04	-0.7540 00	0.2870 00	0.0000 00	6
24	0.2000 08	0.2330-04	-0.8040 00	0.2920 00	0.0000 00	4
25	0.2020 08	0.2420-04	-0.8530 00	0.2950 00	0.0000 00	6
26	0.2060 08	0.2570-04	-0.9030 00	0.3000 00	0.0000 00	4
27	0.2090 08	0.2680-04	-0.9530 00	0.3040 00	0.0000 00	6
28	0.2120 08	0.2790-04	-1.0030 00	0.3080 00	0.0000 00	6
29	0.2150 08	0.2930-04	-1.0530 00	0.3120 00	0.0000 00	4
30	0.2180 08	0.3040-04	-1.1030 00	0.3160 00	0.0000 00	6
31	0.2210 08	0.3150-04	-1.1530 00	0.3200 00	0.0000 00	6
32	0.2250 08	0.3280-04	-1.2030 00	0.3250 00	0.0000 00	4
33	0.2270 08	0.3400-04	-1.2530 00	0.3280 00	0.0000 00	5
34	0.2310 08	0.3540-04	-1.3030 00	0.3330 00	0.0000 00	4
35	0.2340 08	0.3700-04	-1.3530 00	0.3370 00	0.0000 00	4
36	0.2370 08	0.3820-04	-1.4030 00	0.3400 00	0.0000 00	5
37	0.2400 08	0.3950-04	-1.4530 00	0.3450 00	0.0000 00	9
38	0.2430 08	0.4080-04	-1.5030 00	0.3490 00	0.0000 00	4
39	0.2460 08	0.4210-04	-1.5530 00	0.3530 00	0.0000 00	4
40	0.2470 08	0.4350-04	-1.6030 00	0.3540 00	0.0000 00	20
41	0.2490 08	0.4480-04	-1.6530 00	0.3560 00	0.0000 00	4
42	0.2500 08	0.4620-04	-1.7030 00	0.3580 00	0.0000 00	4
43	0.2500 08	0.4760-04	-1.7530 00	0.3580 00	0.0000 00	8
44	0.2520 08	0.4900-04	-1.8030 00	0.3600 00	0.0000 00	4
45	0.2530 08	0.5040-04	-1.8530 00	0.3620 00	0.0000 00	4
46	0.2540 08	0.5180-04	-1.9030 00	0.3630 00	0.0000 00	4
47	0.2560 08	0.5320-04	-1.9530 00	0.3650 00	0.0000 00	4
48	0.2550 08	0.5460-04	-2.0030 00	0.3650 00	0.0000 00	6
49	0.2580 08	0.5600-04	-2.0530 00	0.3660 00	0.0000 00	4
50	0.2560 08	0.5740-04	-2.1030 00	0.3680 00	0.0000 00	4
51	0.2580 08	0.5880-04	-2.1530 00	0.3680 00	0.0000 00	32
52	0.2590 08	0.5980-04	-2.2030 00	0.3690 00	0.0000 00	4
53	0.2600 08	0.6120-04	-2.2530 00	0.3710 00	0.0000 00	8
54	0.2600 08	0.6260-04	-2.3030 00	0.3710 00	0.0000 00	35
55	0.2610 08	0.6400-04	-2.3530 00	0.3720 00	0.0000 00	4
56	0.2620 08	0.6540-04	-2.4030 00	0.3730 00	0.0000 00	4
57	0.2620 08	0.6680-04	-2.4530 00	0.3740 00	0.0000 00	4
58	0.2630 08	0.6820-04	-2.5030 00	0.3750 00	0.0000 00	4
59	0.2630 08	0.6960-04	-2.5530 00	0.3750 00	0.0000 00	10
60	0.2630 08	0.7100-04	-2.5990 00	0.3750 00	0.0000 00	4

61	0.2640	08	0.9340-04	-0.2640	01	0.3760	00	0.0000	00	6
62	0.2650	08	0.9310-04	-0.2650	01	0.3770	00	0.0000	00	6
63	0.2640	08	0.9760-04	-0.2750	01	0.3760	00	0.0000	00	11
64	0.2650	08	0.9490-04	-0.2850	01	0.3770	00	0.0000	00	6
65	0.2650	08	0.1010-03	-0.2850	01	0.3780	00	0.0000	00	6
66	0.2630	08	0.9530-04	-0.2880	01	0.3750	00	0.0000	00	227
67	0.2640	08	0.9710-04	-0.2930	01	0.3760	00	0.0000	00	6
68	0.2640	08	0.9880-04	-0.2980	01	0.3770	00	0.0000	00	6
69	0.2650	08	0.1010-03	-0.3030	01	0.3770	00	0.0000	00	6
70	0.2650	08	0.1020-03	-0.3080	01	0.3780	00	0.0000	00	6
71	0.2660	08	0.1040-03	-0.3130	01	0.3790	00	0.0000	00	6
72	0.2670	08	0.1060-03	-0.3180	01	0.3790	00	0.0000	00	6
73	0.2670	08	0.1070-03	-0.3230	01	0.3800	00	0.0000	00	6
74	0.2680	08	0.1090-03	-0.3280	01	0.3810	00	0.0000	00	6
75	0.2680	08	0.1090-03	-0.3320	01	0.3810	00	0.0000	00	10
76	0.2680	08	0.1100-03	-0.3370	01	0.3810	00	0.0000	00	6
77	0.2690	08	0.1120-03	-0.3420	01	0.3820	00	0.0000	00	6
78	0.2690	08	0.1130-03	-0.3470	01	0.3830	00	0.0000	00	6
79	0.2700	08	0.1150-03	-0.3520	01	0.3830	00	0.0000	00	6
80	0.2700	08	0.1170-03	-0.3570	01	0.3840	00	0.0000	00	5
81	0.2700	08	0.1170-03	-0.3630	01	0.3840	00	0.0000	00	11
82	0.2700	08	0.1180-03	-0.3680	01	0.3850	00	0.0000	00	6
83	0.2690	08	0.1140-03	-0.3740	01	0.3830	00	0.0000	00	229
84	0.2700	08	0.1180-03	-0.3790	01	0.3840	00	0.0000	00	6
85	0.2700	08	0.1170-03	-0.3840	01	0.3840	00	0.0000	00	6
86	0.2710	08	0.1190-03	-0.3890	01	0.3850	00	0.0000	00	6
87	0.2710	08	0.1200-03	-0.3940	01	0.3860	00	0.0000	00	6
88	0.2720	08	0.1220-03	-0.3990	01	0.3860	00	0.0000	00	6
89	0.2720	08	0.1230-03	-0.4040	01	0.3870	00	0.0000	00	6
90	0.2730	08	0.1250-03	-0.4090	01	0.3870	00	0.0000	00	6
91	0.2730	08	0.1260-03	-0.4140	01	0.3880	00	0.0000	00	6
92	0.2730	08	0.1280-03	-0.4190	01	0.3890	00	0.0000	00	6
93	0.2740	08	0.1290-03	-0.4240	01	0.3900	00	0.0000	00	6
94	0.2740	08	0.1310-03	-0.4290	01	0.3900	00	0.0000	00	6
95	0.2750	08	0.1320-03	-0.4340	01	0.3900	00	0.0000	00	6
96	0.2750	08	0.1340-03	-0.4390	01	0.3910	00	0.0000	00	6
97	0.2760	08	0.1350-03	-0.4440	01	0.3920	00	0.0000	00	6
98	0.2760	08	0.1360-03	-0.4490	01	0.3920	00	0.0000	00	6
99	0.2760	08	0.1360-03	-0.4540	01	0.3920	00	0.0000	00	9
100	0.2770	08	0.1380-03	-0.4590	01	0.3930	00	0.0000	00	6
101	0.2770	08	0.1390-03	-0.4640	01	0.3930	00	0.0000	00	6
102	0.2780	08	0.1400-03	-0.4690	01	0.3940	00	0.0000	00	6
103	0.2780	08	0.1420-03	-0.4740	01	0.3940	00	0.0000	00	6
104	0.2780	08	0.1430-03	-0.4790	01	0.3950	00	0.0000	00	6
105	0.2780	08	0.1430-03	-0.4840	01	0.3950	00	0.0000	00	9
106	0.2790	08	0.1450-03	-0.4890	01	0.3960	00	0.0000	00	6
107	0.2790	08	0.1460-03	-0.4940	01	0.3960	00	0.0000	00	6
108	0.2800	08	0.1470-03	-0.4990	01	0.3970	00	0.0000	00	6
109	0.2800	08	0.1490-03	-0.5040	01	0.3970	00	0.0000	00	6
110	0.2810	08	0.1500-03	-0.5090	01	0.3980	00	0.0000	00	6
111	0.2810	08	0.1510-03	-0.5140	01	0.3980	00	0.0000	00	6
112	0.2810	08	0.1530-03	-0.5190	01	0.3990	00	0.0000	00	6
113	0.2810	08	0.1560-03	-0.5240	01	0.3990	00	0.0000	00	8
114	0.2820	08	0.1580-03	-0.5290	01	0.3990	00	0.0000	00	6
115	0.2820	08	0.1590-03	-0.5340	01	0.4000	00	0.0000	00	11
116	0.2830	08	0.1600-03	-0.5390	01	0.4010	00	0.0000	00	6
117	0.2830	08	0.1620-03	-0.5440	01	0.4010	00	0.0000	00	6
118	0.2830	08	0.1630-03	-0.5490	01	0.4020	00	0.0000	00	6
119	0.2840	08	0.1660-03	-0.5540	01	0.4020	00	0.0000	00	15
120	0.2840	08	0.1690-03	-0.5590	01	0.4020	00	0.0000	00	6
121	0.2840	08	0.1720-03	-0.5640	01	0.4040	00	0.0000	00	6
122	0.2840	08	0.1750-03	-0.5690	01	0.4040	00	0.0000	00	6
123	0.2840	08	0.1780-03	-0.5740	01	0.4030	00	0.0000	00	6
124	0.2840	08	0.1810-03	-0.5790	01	0.4030	00	0.0000	00	9
125	0.2850	08	0.1830-03	-0.5840	01	0.4030	00	0.0000	00	3
126	0.2850	08	0.1860-03	-0.5890	01	0.4030	00	0.0000	00	0

*** CONCRETE ULTIMATE STRAIN HAS BEEN REACHED ***

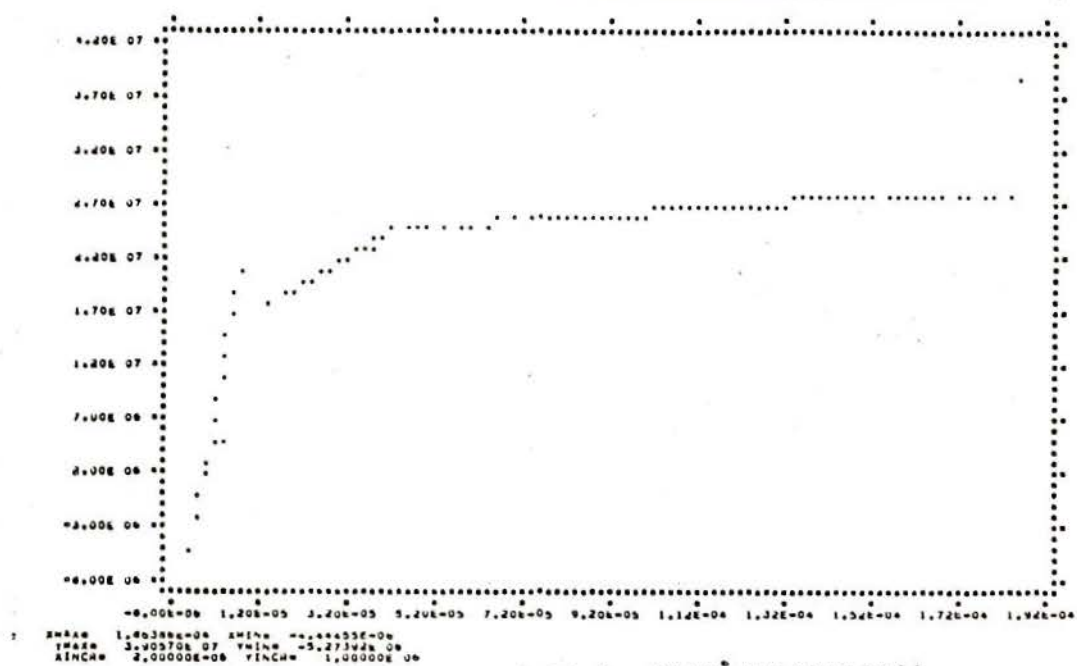
ELEMENT # 18

STEP #	MOMENT	CURVATURE	DISPLACEMENT	LOAD PRCTN	CURT. TIME	ITERATIONS
1	0.5220 07	0.4400-05	-0.2700 00	0.1000 01	0.0000 00	4
2	-0.5350 07	-0.4510-05	0.3440 00	0.1000 01	0.0000 00	3
3	-0.2530 07	-0.4400-05	0.2670 00	0.1000 01	0.0000 00	3
4	-0.2530 07	-0.2200-05	0.2490 00	0.2000-01	0.0000 00	4
5	-0.2530 07	-0.2200-05	0.2490 00	0.3120-01	0.0000 00	3
6	-0.2530 07	-0.2200-05	0.2490 00	0.7030-01	0.0000 00	6
7	-0.2530 07	-0.2200-05	0.2490 00	0.1010 00	0.0000 00	10
8	-0.2530 07	-0.2200-05	0.2490 00	0.1270 00	0.0000 00	8
9	-0.2530 07	-0.2200-05	0.2490 00	0.1520 00	0.0000 00	4
10	-0.2530 07	-0.2200-05	0.2490 00	0.1770 00	0.0000 00	8
11	-0.2530 07	-0.2200-05	0.2490 00	0.2020 00	0.0000 00	4
12	-0.2530 07	-0.2200-05	0.2490 00	0.2270 00	0.0000 00	4
13	-0.2530 07	-0.2200-05	0.2490 00	0.2520 00	0.0000 00	4
14	-0.2530 07	-0.2200-05	0.2490 00	0.2760 00	0.0000 00	9
15	-0.2530 07	-0.2200-05	0.2490 00	0.3010 00	0.0000 00	4
16	-0.2530 07	-0.2200-05	0.2490 00	0.2860 00	0.0000 00	71
17	-0.2530 07	-0.2200-05	0.2490 00	0.2770 00	0.0000 00	6
18	-0.2530 07	-0.2200-05	0.2490 00	0.2850 00	0.0000 00	6
19	-0.2530 07	-0.2200-05	0.2490 00	0.2930 00	0.0000 00	3
20	-0.2530 07	-0.2200-05	0.2490 00	0.3010 00	0.0000 00	4
21	-0.2530 07	-0.2200-05	0.2490 00	0.3100 00	0.0000 00	3
22	-0.2530 07	-0.2200-05	0.2490 00	0.2830 00	0.0000 00	46
23	-0.2530 07	-0.2200-05	0.2490 00	0.2870 00	0.0000 00	8
24	-0.2530 07	-0.2200-05	0.2490 00	0.2920 00	0.0000 00	4
25	-0.2530 07	-0.2200-05	0.2490 00	0.2950 00	0.0000 00	6
26	-0.2530 07	-0.2200-05	0.2490 00	0.3000 00	0.0000 00	4
27	-0.2530 07	-0.2200-05	0.2490 00	0.3040 00	0.0000 00	6
28	-0.2530 07	-0.2200-05	0.2490 00	0.3080 00	0.0000 00	6
29	-0.2530 07	-0.2200-05	0.2490 00	0.3120 00	0.0000 00	4
30	-0.2530 07	-0.2200-05	0.2490 00	0.3160 00	0.0000 00	9
31	-0.2530 07	-0.2200-05	0.2490 00	0.3200 00	0.0000 00	8
32	-0.2530 07	-0.2200-05	0.2490 00	0.3250 00	0.0000 00	4
33	-0.2530 07	-0.2200-05	0.2490 00	0.3280 00	0.0000 00	3
34	-0.2530 07	-0.2200-05	0.2490 00	0.3330 00	0.0000 00	4
35	-0.2530 07	-0.2200-05	0.2490 00	0.3370 00	0.0000 00	4
36	-0.2530 07	-0.2200-05	0.2490 00	0.3400 00	0.0000 00	3
37	-0.2530 07	-0.2200-05	0.2490 00	0.3450 00	0.0000 00	9
38	-0.2530 07	-0.2200-05	0.2490 00	0.3490 00	0.0000 00	4
39	-0.2530 07	-0.2200-05	0.2490 00	0.3530 00	0.0000 00	4
40	-0.2530 07	-0.2200-05	0.2490 00	0.3540 00	0.0000 00	20
41	-0.2530 07	-0.2200-05	0.2490 00	0.3560 00	0.0000 00	4
42	-0.2530 07	-0.2200-05	0.2490 00	0.3580 00	0.0000 00	4
43	-0.2530 07	-0.2200-05	0.2490 00	0.3580 00	0.0000 00	8
44	-0.2530 07	-0.2200-05	0.2490 00	0.3600 00	0.0000 00	4
45	-0.2530 07	-0.2200-05	0.2490 00	0.3620 00	0.0000 00	4
46	-0.2530 07	-0.2200-05	0.2490 00	0.3630 00	0.0000 00	4
47	-0.2530 07	-0.2200-05	0.2490 00	0.3650 00	0.0000 00	4
48	-0.2530 07	-0.2200-05	0.2490 00	0.3650 00	0.0000 00	8
49	-0.2530 07	-0.2200-05	0.2490 00	0.3680 00	0.0000 00	4
50	-0.2530 07	-0.2200-05	0.2490 00	0.3680 00	0.0000 00	4
51	-0.2530 07	-0.2200-05	0.2490 00	0.3680 00	0.0000 00	32
52	-0.2530 07	-0.2200-05	0.2490 00	0.3690 00	0.0000 00	4
53	-0.2530 07	-0.2200-05	0.2490 00	0.3710 00	0.0000 00	8
54	-0.2530 07	-0.2200-05	0.2490 00	0.3710 00	0.0000 00	33
55	-0.2530 07	-0.2200-05	0.2490 00	0.3720 00	0.0000 00	4
56	-0.2530 07	-0.2200-05	0.2490 00	0.3730 00	0.0000 00	4
57	-0.2530 07	-0.2200-05	0.2490 00	0.3740 00	0.0000 00	4
58	-0.2530 07	-0.2200-05	0.2490 00	0.3750 00	0.0000 00	4
59	-0.2530 07	-0.2200-05	0.2490 00	0.3750 00	0.0000 00	10
60	-0.2530 07	-0.2200-05	0.2490 00	0.3750 00	0.0000 00	4
61	-0.2530 07	-0.2200-05	0.2490 00	0.3760 00	0.0000 00	4
62	-0.2530 07	-0.2200-05	0.2490 00	0.3770 00	0.0000 00	4
63	-0.2530 07	-0.2200-05	0.2490 00	0.3780 00	0.0000 00	11
64	-0.2530 07	-0.2200-05	0.2490 00	0.3770 00	0.0000 00	4
65	-0.2530 07	-0.2200-05	0.2490 00	0.3780 00	0.0000 00	4
66	-0.2530 07	-0.2200-05	0.2490 00	0.3750 00	0.0000 00	227
67	-0.2530 07	-0.2200-05	0.2490 00	0.3760 00	0.0000 00	4
68	-0.2530 07	-0.2200-05	0.2490 00	0.3770 00	0.0000 00	4
69	-0.2530 07	-0.2200-05	0.2490 00	0.3770 00	0.0000 00	4
70	-0.2530 07	-0.2200-05	0.2490 00	0.3780 00	0.0000 00	4
71	-0.2530 07	-0.2200-05	0.2490 00	0.3790 00	0.0000 00	4
72	-0.2530 07	-0.2200-05	0.2490 00	0.3790 00	0.0000 00	4
73	-0.2530 07	-0.2200-05	0.2490 00	0.3800 00	0.0000 00	4
74	-0.2530 07	-0.2200-05	0.2490 00	0.3810 00	0.0000 00	4
75	-0.2530 07	-0.2200-05	0.2490 00	0.3810 00	0.0000 00	10
76	-0.2530 07	-0.2200-05	0.2490 00	0.3810 00	0.0000 00	4
77	-0.2530 07	-0.2200-05	0.2490 00	0.3820 00	0.0000 00	4

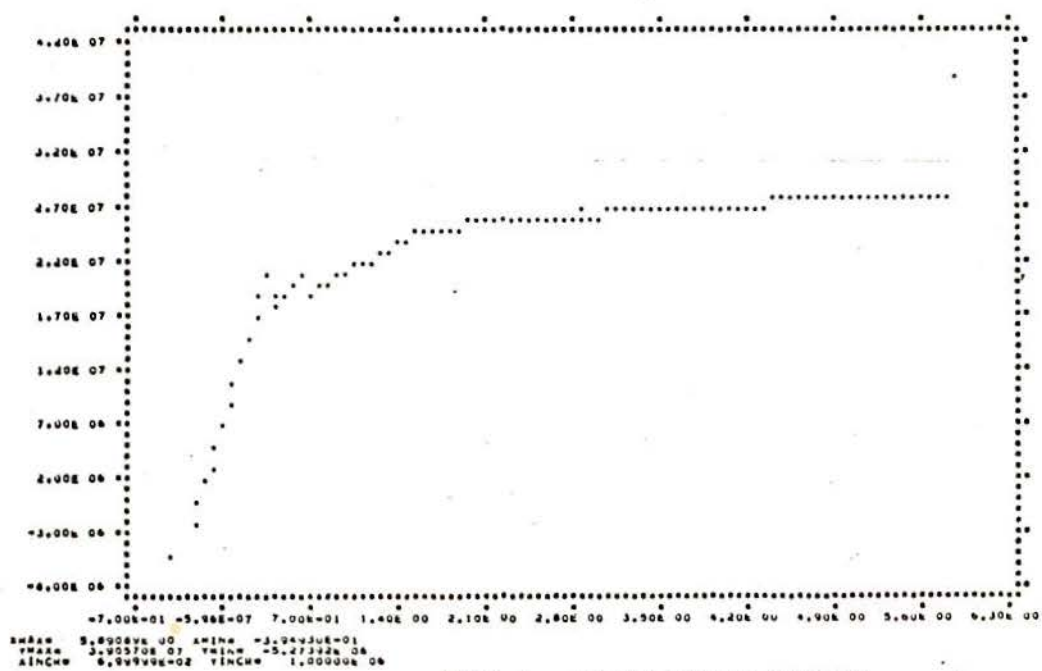
287

[illegible]

P L O T S



ELEMENT 4 MOMENT-CURVATURE



ELEMENT 4 MOMENT-DEFLECTION